
Towards LHC Phenomenology beyond Leading Order

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The LHC ...

... has been planned long time ago ...



Linear Colliders also seem to have been supported . . .



... so why do we say we are entering a
New Era in Particle Physics?

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... because instead of hunting buffaloes,
we are now hunting Higgs bosons ...

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 \Rightarrow **strong interactions play key role:**
enormous backgrounds !

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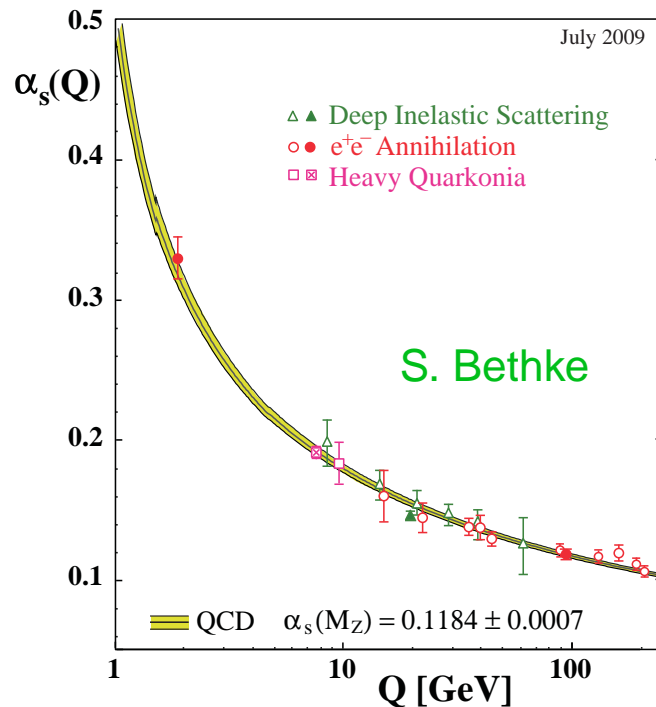
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process	events/sec	
QCD jets $E_T > 150$ GeV	100	background
$W \rightarrow e\nu$	15	background
$t\bar{t}$	1	background
Higgs, $m_H \sim 130$ GeV	0.02	signal
gluinos, $m \sim 1$ TeV	0.001	signal

strong interactions

basic principles of **Q**uantum **C**hromo-**D**ynamics (**QCD**):

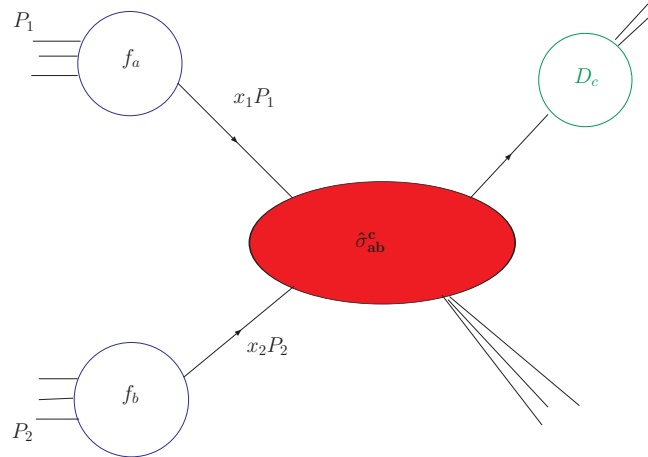
- **asymptotic freedom**: coupling $\alpha_s(Q^2) \rightarrow 0$ for $Q^2 \rightarrow \infty$



constituents of hadrons (quarks and gluons) can be considered as freely interacting at high energies (i.e. short distances)

- **factorisation**: systematic separation of **long-distance** effects (non-perturbative) and **short-distance** cross sections (“hard scattering”)

factorisation



$$\sigma_{pp \rightarrow X} = \sum_{a,b,c} f_a(x_1, \mu_f^2) f_b(x_2, \mu_f^2) \otimes \hat{\sigma}_{ab}(p_1, p_2, \frac{Q^2}{\mu_f^2}, \frac{Q^2}{\mu_r^2}, \alpha_s(\mu_r^2)) \otimes D_{c \rightarrow X}(z, \mu_f^2) + \mathcal{O}(1/Q^2)$$

f_a, f_b : parton distribution functions (universal), model proton structure

$\hat{\sigma}_{ab}$: partonic **hard scattering** cross section, **calculable order by order in perturbation theory**

$D_{c \rightarrow X}(z, \mu_f^2)$: describing the final state e.g. fragmentation function, jet observable, etc.

shortcomings of leading order predictions

$$\hat{\sigma} = \alpha_s^k(\mu) [\hat{\sigma}^{\text{LO}} + \alpha_s(\mu) \hat{\sigma}^{\text{NLO}}(\mu) + \alpha_s^2(\mu) \hat{\sigma}^{\text{NNLO}}(\mu) + \dots]$$

calculation at n -th order: $d\hat{\sigma}^{(n)}/d\ln(\mu^2) = \mathcal{O}(\alpha_s^{n+1})$

truncation of perturbative series at LO

⇒ large renormalisation/factorisation scale dependence

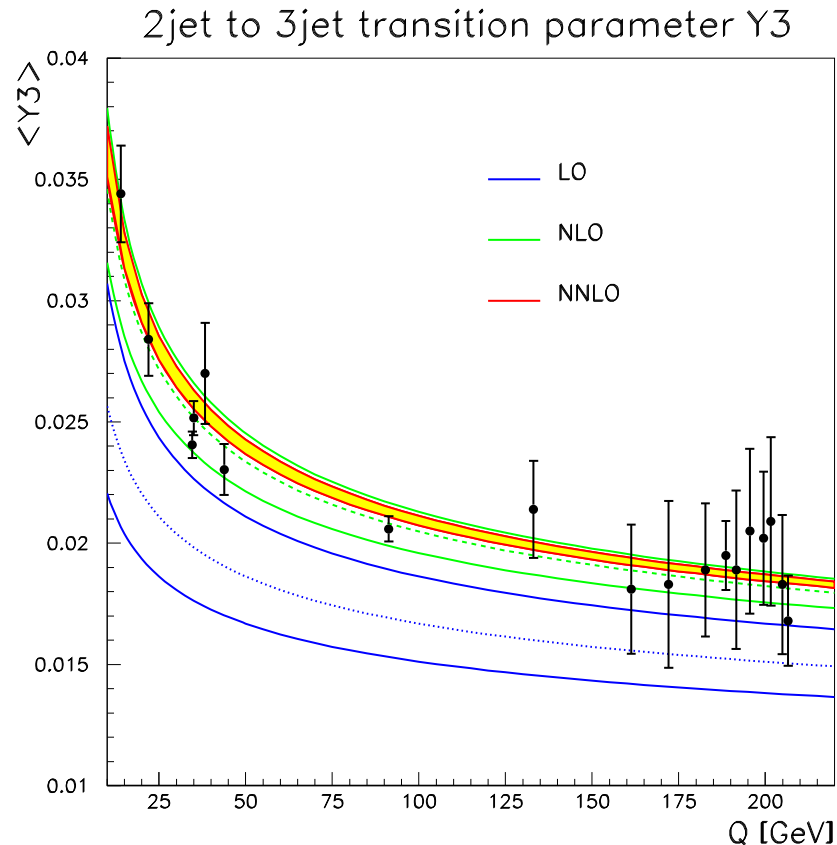
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example:

3-jet observable
in e^+e^- annihilation

[A. Gehrmann-De Ridder,
T. Gehrmann, N. Glover, GH '09]

uncertainty bands:

$$M_Z/2 < \mu < 2 M_Z$$

shortcomings of leading order predictions

- poor jet modelling



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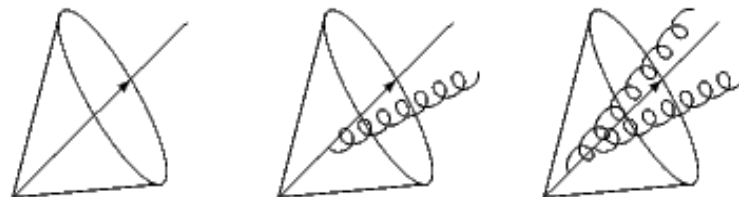


- cases where **shapes** of distributions are not well predicted by LO

(new partonic processes become possible beyond LO)

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- cases where **shapes** of distributions are not well predicted by LO

(new partonic processes become possible beyond LO)

- Minimal Supersymmetric Standard Model (MSSM):
would be **ruled out** already without radiative corrections:

mass of lightest Higgs boson at LO: $M_h \leq \min(M_A, M_Z) \cdot |\cos 2\beta|$

- ...

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shape in general well described by Monte Carlo tools combining
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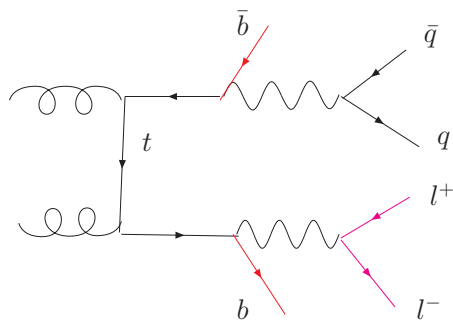
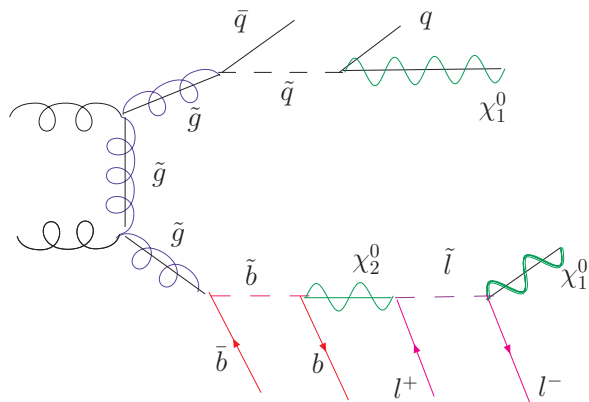
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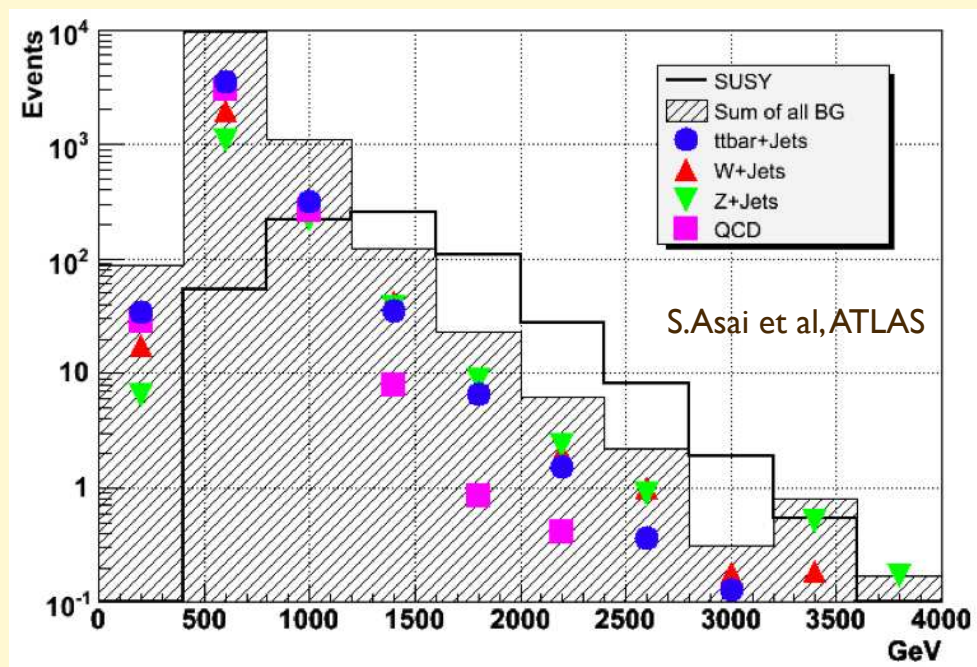
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- **now paradigm change:**
we are moving towards **automated NLO tools**

(heavy) SUSY particles:

- decay through cascades emitting quarks and leptons
- signatures: energetic jets and leptons, missing E_T
- QCD radiation generates additional hard jets



Overall result, after the complete detector simulation, etc...

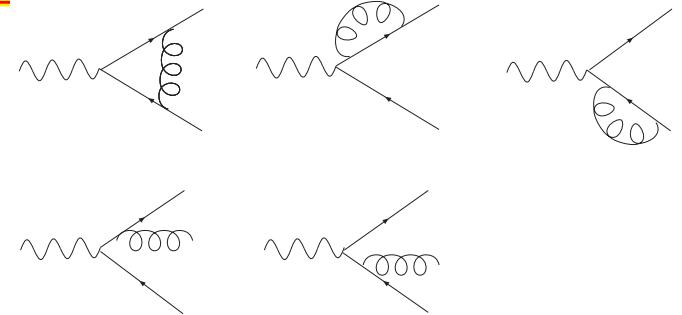


ingredients for m -particle observable at NLO

virtual part (one-loop integrals):

$$\mathcal{A}_{NLO}^V = A_2/\epsilon^2 + A_1/\epsilon + A_0$$

$$d\sigma^V \sim \text{Re} \left(\mathcal{A}_{LO}^\dagger \mathcal{A}_{NLO}^V \right)$$



real radiation part: soft/collinear emission of massless particles

⇒ need subtraction terms

$$\Rightarrow \int_{\text{sing}} d\sigma^S = -A_2/\epsilon^2 - A_1/\epsilon + B_0$$

$$\sigma^{NLO} = \underbrace{\int_{m+1} \left[d\sigma^R - d\sigma^S \right]_{\epsilon=0}}_{\text{numerically}} + \underbrace{\int_m \left[\underbrace{d\sigma^V}_{\text{cancel poles}} + \underbrace{\int_s d\sigma^S}_{\text{analytically}} \right]_{\epsilon=0}}_{\text{numerically}}$$

Modular structure

Tree Modules

One-Loop Module

IR Modules

$$|\mathcal{A}^{LO}|^2 \oplus$$

$$2 \operatorname{Re}(\mathcal{A}^{LO\dagger} \mathcal{A}^{NLO,V}) \oplus$$

$$\sum_j \int_j \mathcal{S}_j$$

$$|\mathcal{A}^{NLO,R}|^2$$

$$\ominus \sum_j \mathcal{S}_j$$

has been bottleneck so far

NLO complexity

calculations increasingly difficult for more particles in final state

- example for time scale to add one parton:

$pp \rightarrow 2$ jets at NLO (4-point process):

Ellis/Sexton 1986

$pp \rightarrow 3$ jets at NLO (5-point process):

Bern et al, Kunszt et al. 1993-95

$pp \rightarrow 4$ jets at NLO (6-point process):

not yet available

progress

- more **efficient** techniques to calculate **loop amplitudes**
 - unitarity-based methods
e.g. BlackHat, Rocket, CutTools, analytic, ...
 - improved methods based on Feynman diagrams
e.g. GOLEM, Denner et. al, ...

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- **use existing technology** from leading order tools
LO tools can provide:
 - event generation
 - phase space integration
 - histogramming tools
 - subtraction terms for soft/collinear radiation

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- **matching NLO** amplitudes with parton showers
e.g. MC@NLO, POWHEG, ...

2009 status of NLO wishlist for LHC

$pp \rightarrow W W \text{ jet}$	Denner et al.; Ellis et al.
$pp \rightarrow Z Z \text{ jet}$	Binoth/Gleisberg/Karg/Kauer/Sanguinetti
$pp \rightarrow t\bar{t} b\bar{b}$	Bredenstein et al.; Bevilacqua et al.
$pp \rightarrow t\bar{t} + 2 \text{ jets}$	
$pp \rightarrow Z Z Z$	Lazopoulos/Melnikov/Petriello; Hankele/Zeppenfeld
$pp \rightarrow V V V$	Binoth/Ossola/Papadopoulos/Pittau; Zeppenfeld et al.
$pp \rightarrow V V b\bar{b}$	
$pp \rightarrow W \gamma \text{ jet}$	Campanario/Englert/Spannowsky/Zeppenfeld
$pp \rightarrow V V + 2 \text{ jets}$	VBF: Bozzi/Jäger/Oleari/Zeppenfeld, VBFNLO coll.
$pp \rightarrow W + 3 \text{ jets}$	BlackHat coll.; Ellis/Giele/Kunszt/Melnikov/Zanderighi*
$pp \rightarrow Z + 3 \text{ jets}$	BlackHat collaboration
$pp \rightarrow b\bar{b}b\bar{b}$	Binoth/Guffanti/Guillet/Reiter/Reuter
$pp \rightarrow t\bar{t} \text{ jet}$	Dittmaier/Uwer/Weinzierl
$pp \rightarrow t\bar{t} Z$	Lazopoulos/McElmurry/Melnikov/Petriello
$pp \rightarrow b\bar{b} Z, b\bar{b} W$	Febres Cordero/Reina/Wackerroth

● done ● partial results * leading colour only

Interface

details worked out at Les Houches 2009 workshop on TeV colliders

Monte Carlo tool (MC)

One-Loop-Provider (OLP)

initialisation:

process info
CH summed
model parameters
fix scheme
...

order



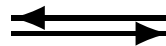
copy/confirm



contract

runtime:

events



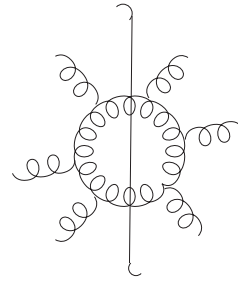
$A_2, A_1, A_0, |Born|^2$

standard interface

One-loop methods

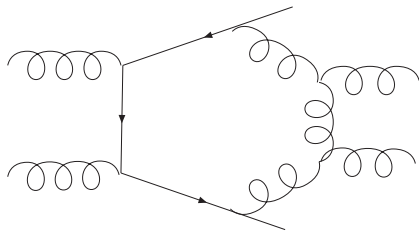
- unitarity based:

$$\mathcal{A} = \sum_{\text{cuts}} \int dPS$$

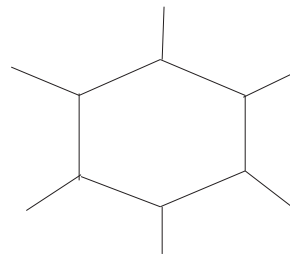


+ \mathcal{R}

- Feynman diagram based

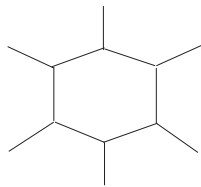


non-trivial tensor structure

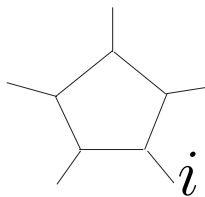


scalar 6-point function

+ integrals with less legs



$$= \sum_{i=1}^6 b_i$$



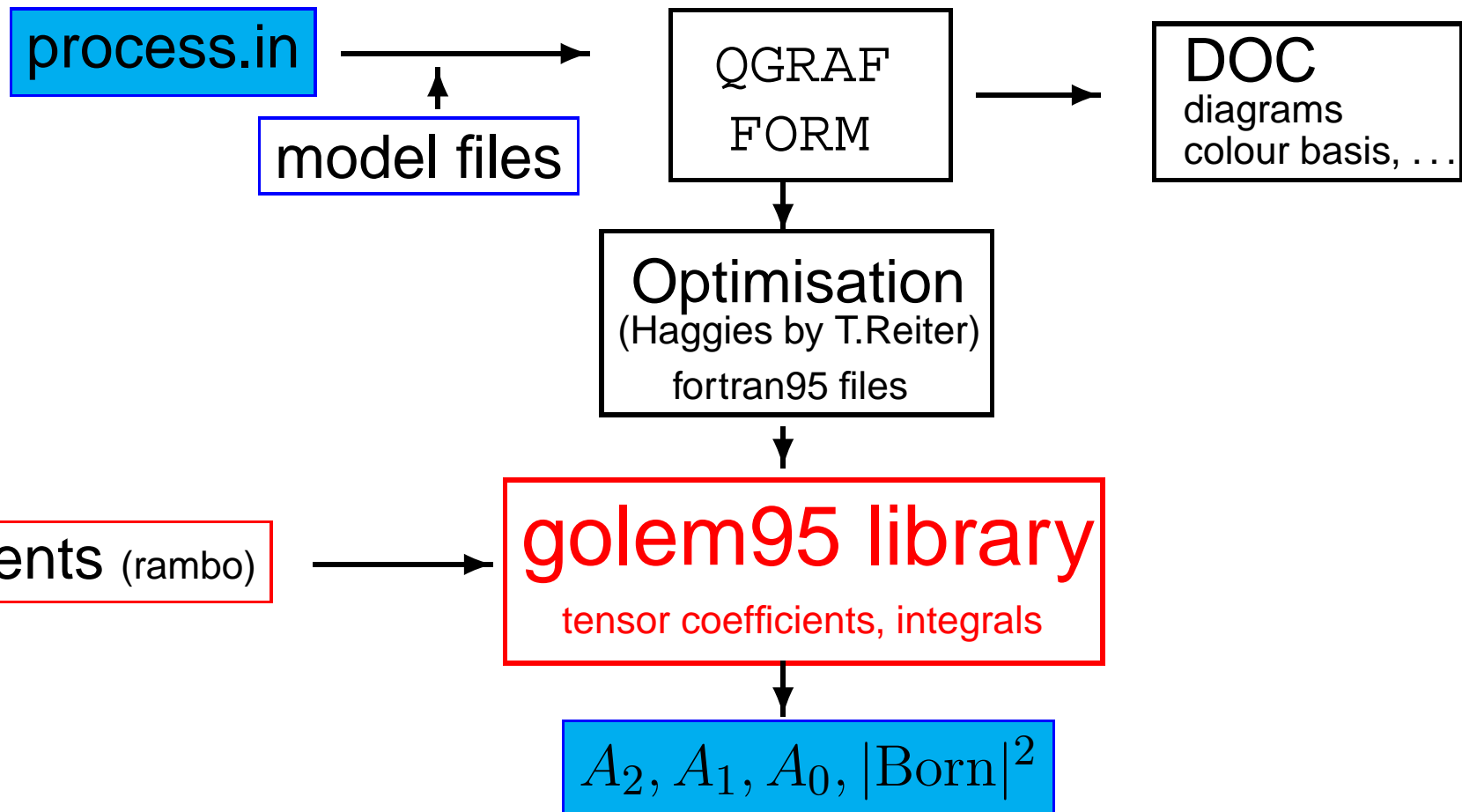
...

reduction to set of **basis integrals** (4-, 3- and 2-point functions)

GOLEM

General One-Loop Evaluator of Matrix elements

[Binoth, Cullen, Guillet, GH, Karg, Kauer, Pilon, Reiter, Rodgers, Wigmore]



Golem strong points

- can deal with an **arbitrary** number of **mass scales**
link [LoopTools](#) for finite massive boxes
- **colour** does not add additional complexity
- rational parts are **"for free"**
- efficient use of recursive structure
caching system
- projection onto **helicity** states
exploit spinor helicity techniques, gauge cancellations, smaller building blocks
- collaboration has several independent programs
⇒ strong checks
- can avoid spurious singularities from
Gram determinants ⇒ **numerically robust**

Golem development

- Golem results:

$pp \rightarrow WW, ZZ, \gamma\gamma j, HH, HHH, Hjj$ (interference)
 $ZZj, \bar{b}\bar{b}\bar{b}$

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 $ZZj, b\bar{b}b\bar{b}$

- **under construction:**

- allow for **complex masses** \Rightarrow deal with **unstable** particles
- validation for multi-leg calculations within **supersymmetric** models [GH, T. Kleinschmidt, M. Rodgers]
- interface to **FeynRules**, producing model files from arbitrary Lagrangians [C. Duhr et al.]
- user-friendly public interface, detailed documentation
- combination with **parton shower** [Sherpa, F. Krauss et al.]

six-photon amplitude

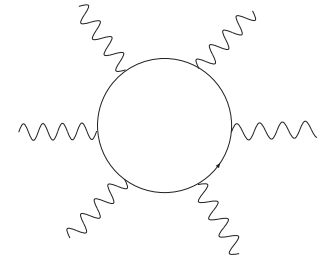
[Mahlon 94] (special helicity configurations only)

[Nagy, Soper 06; Gong, Nagy, Soper 08] (numerically)

[Binoth, Gehrmann, GH, Mastrolia 07]

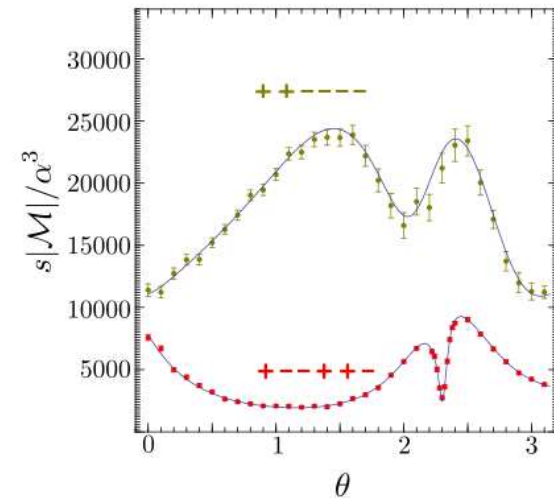
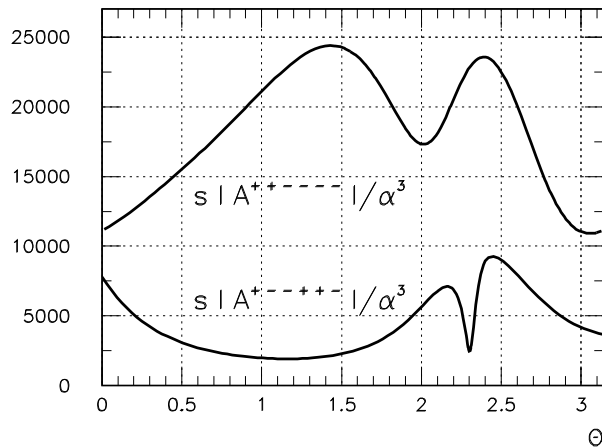
[Ossola, Pittau, Papadopoulos 07]

[Bernicot, Guillet 08]



● rational parts shown to be zero [Binoth, Guillet, GH 06]

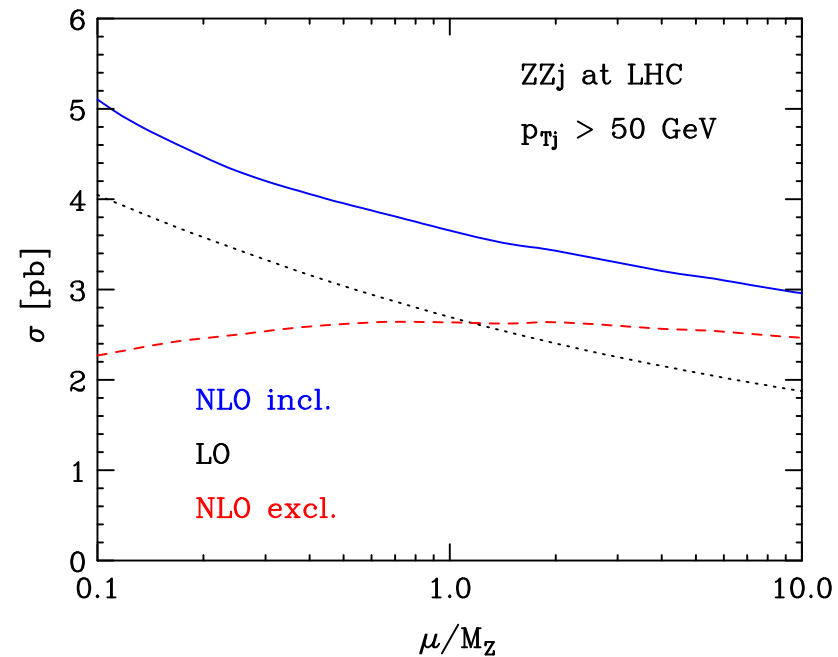
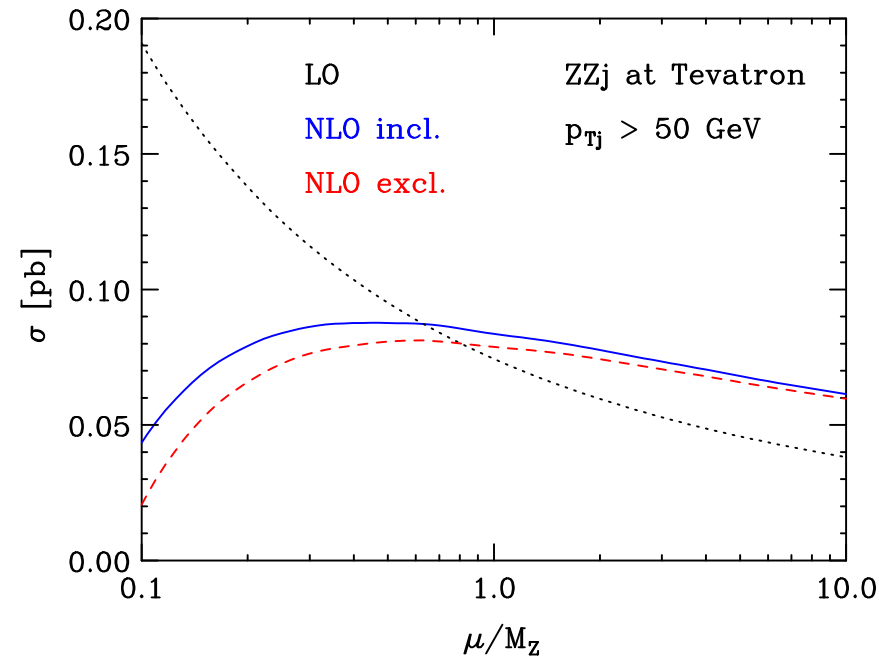
● used both **unitarity cuts** and **Golem**



Gong, Nagy, Soper

ZZ + jet production: scale dependence

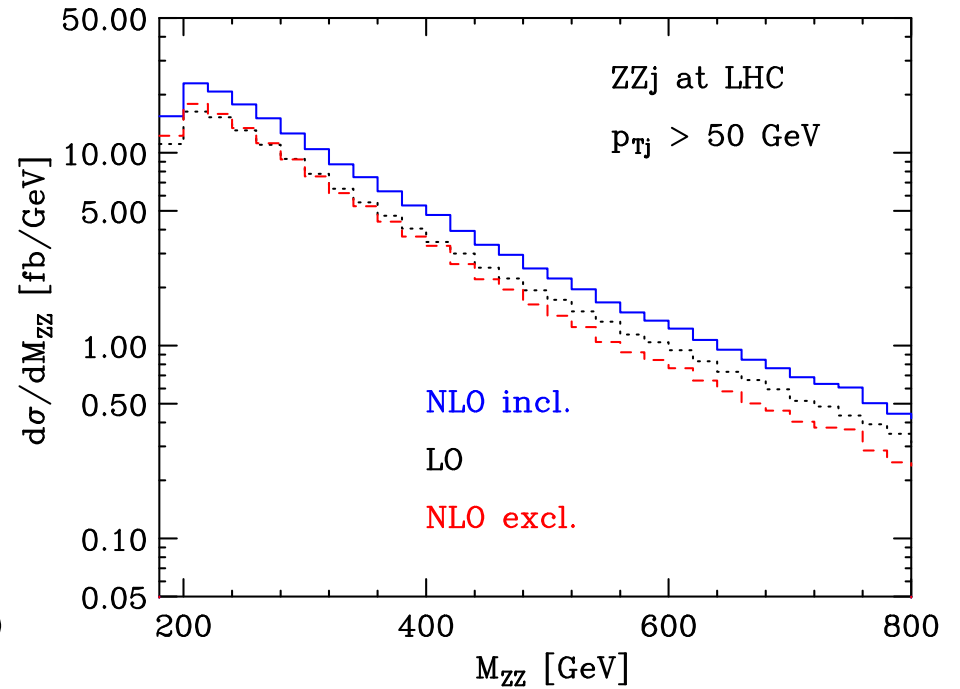
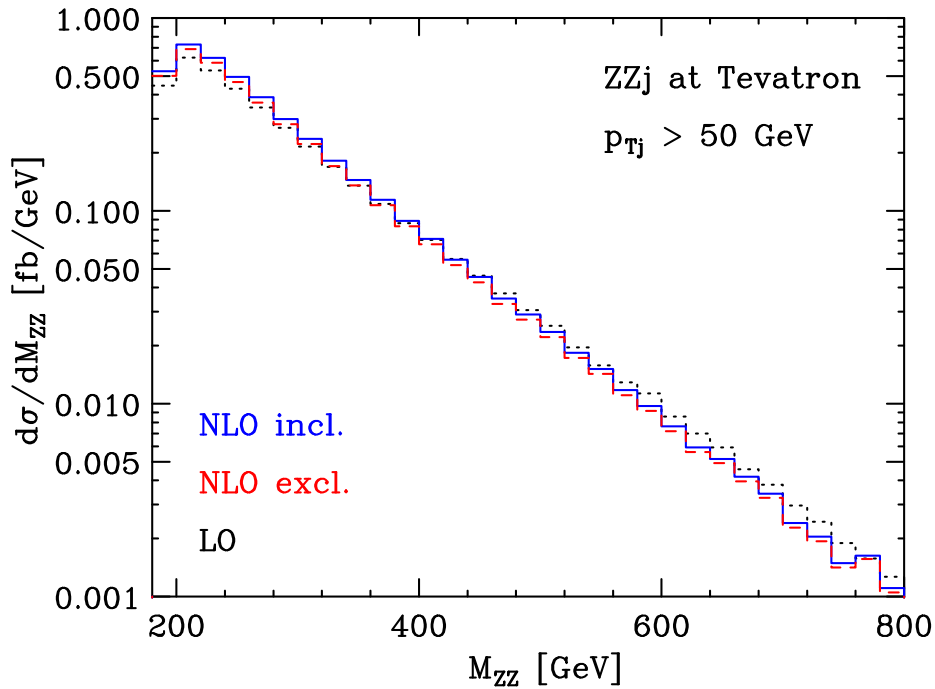
T. Binoth, T. Gleisberg, S. Karg, N. Kauer, G. Sanguinetti '09



NLO excl.: jet veto: no additional jets with $p_T > 50$ GeV

ZZ + jet production

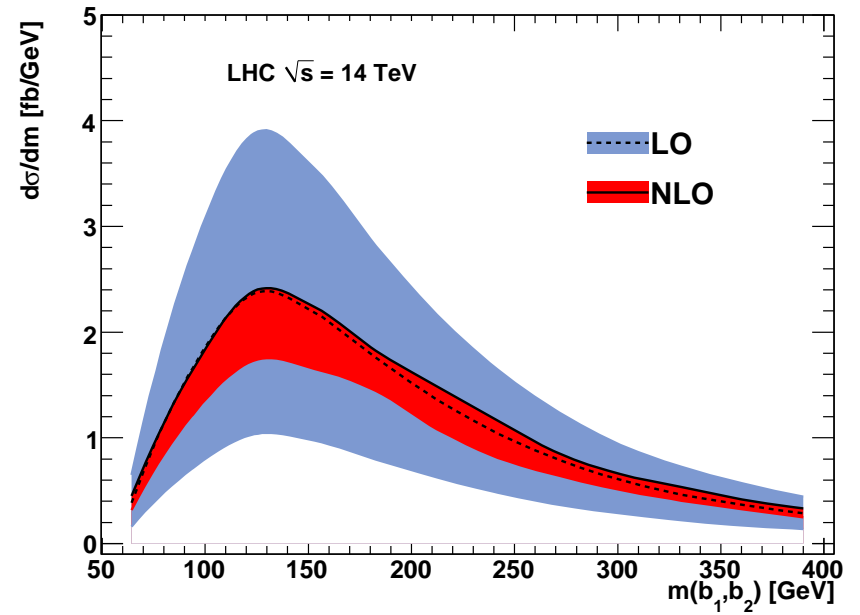
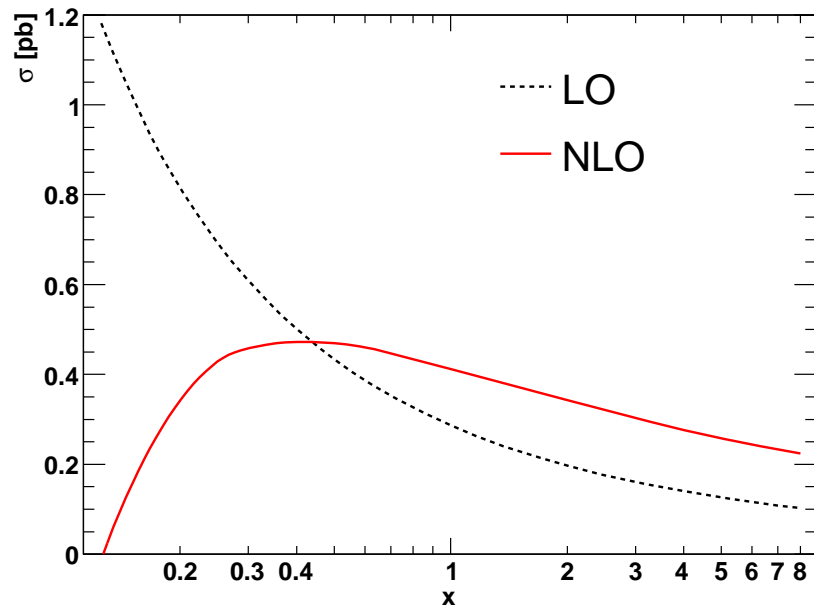
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$pp \rightarrow b\bar{b}b\bar{b}$ at NLO

$$q\bar{q} \rightarrow b\bar{b}b\bar{b}$$

[Binoth, Greiner, Guffanti, Guillet, Reiter, Reuter '09]



prompt photons

The PHOX Family

NLO Monte Carlo programs (**partonic** event generators) to calculate cross sections for the production of large- p_T **photons, hadrons and jets**

http://wwwlapp.in2p3.fr/lapth/PHOX_FAMILY/main.html

F. Arleo, P. Aurenche, T. Binoth, M. Fontannaz, J.Ph. Guillet,
GH, E. Pilon, M. Werlen

● DIPHOX

$$h_1 h_2 \rightarrow \gamma \gamma + X, \quad h_1 h_2 \rightarrow \gamma h_3 + X, \quad h_1 h_2 \rightarrow h_3 h_4 + X$$

● JETPHOX

$$h_1 h_2 \rightarrow \gamma \text{ jet} + X, \quad h_1 h_2 \rightarrow \gamma + X$$
$$h_1 h_2 \rightarrow h_3 \text{ jet} + X, \quad h_1 h_2 \rightarrow h_3 + X$$

● EPHOX

$$\gamma p \rightarrow \gamma \text{ jet} + X, \quad \gamma p \rightarrow \gamma + X$$
$$\gamma p \rightarrow h \text{ jet} + X, \quad \gamma p \rightarrow h + X$$

● TWINPHOX

$$\gamma \gamma \rightarrow \gamma \text{ jet} + X, \quad \gamma \gamma \rightarrow \gamma + X$$



PHOX programs

partonic event generators

- produce **ntuples** (PAW) or histograms
- **fragmentation** component included **fully at NLO**
- **new: Frixione isolation** criterion is being implemented
designed to suppress fragmentation component

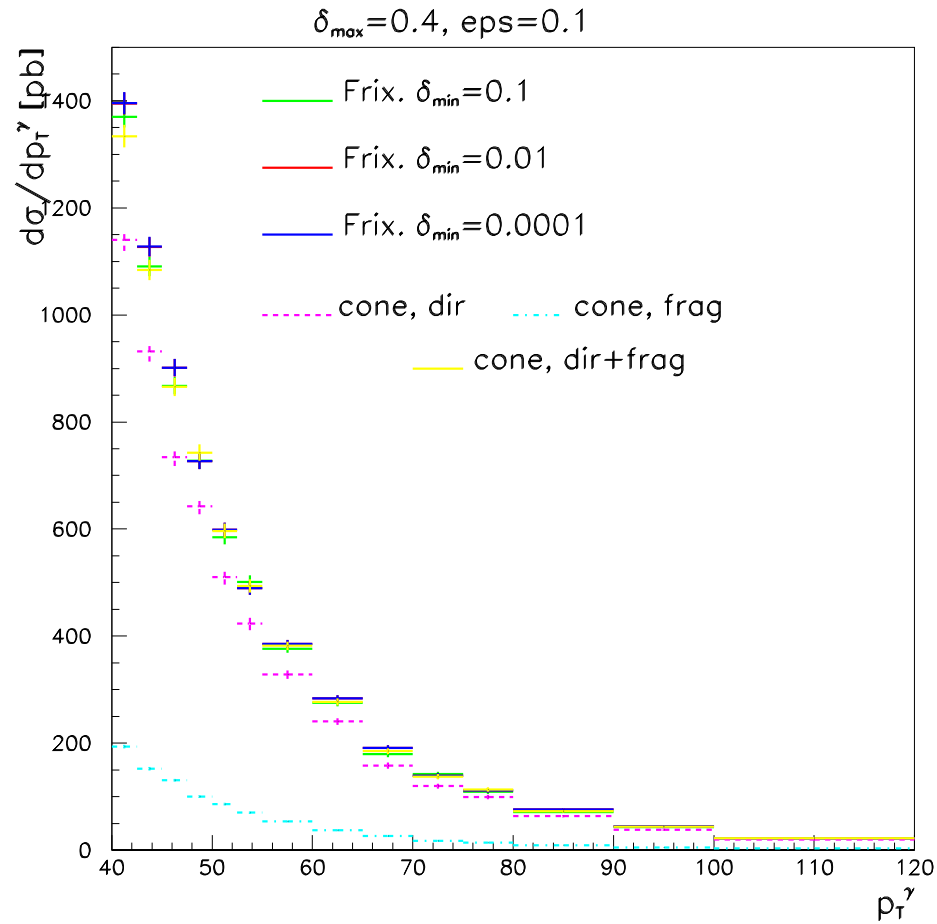
$$E_{T,\max} = \epsilon_\gamma p_T^\gamma \underbrace{\left(\frac{1 - \cos \delta}{1 - \cos \delta_{\max}} \right)^n}_{f(\delta)}$$

$$\lim_{\delta \rightarrow 0} f(\delta) = 0$$

but: no hadronic energy in isolation cone experimentally never realised \Rightarrow **better:**

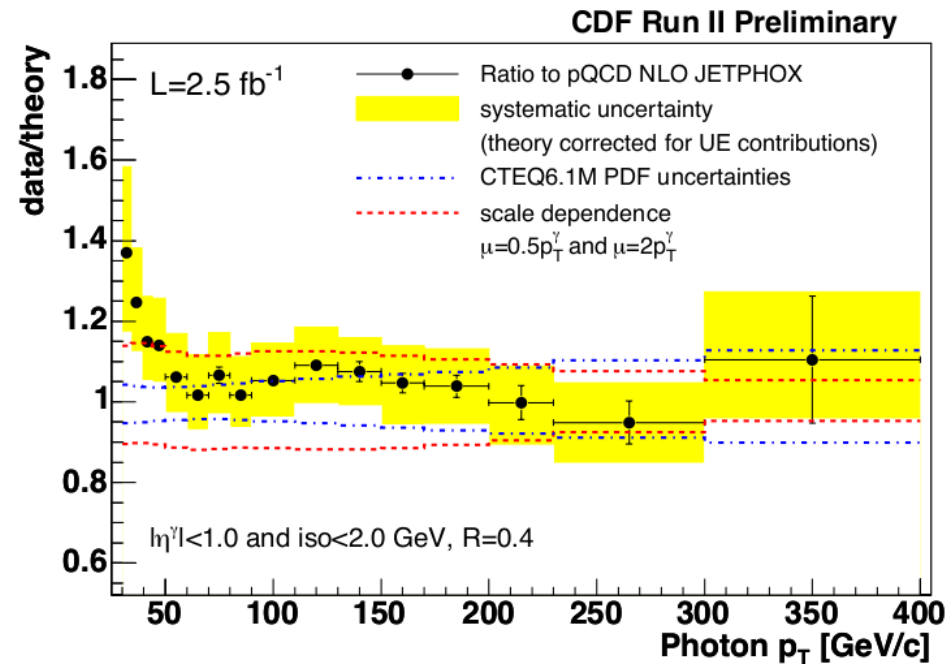
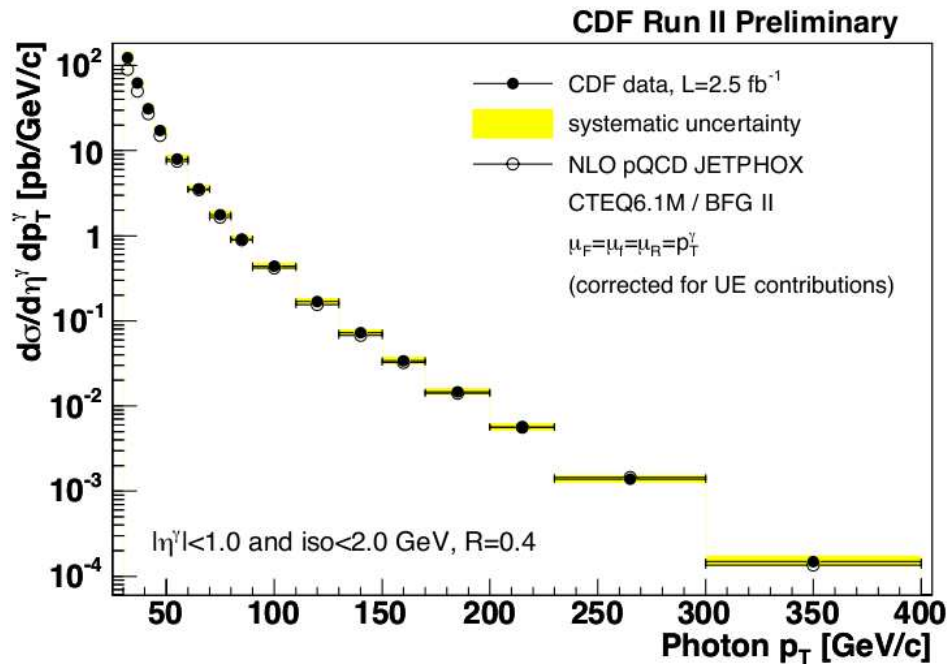
$$f(\delta) = \begin{cases} f(\delta) & \text{for } \delta > \delta_{\min} \\ f(\delta_{\min}) & \text{for } \delta \leq \delta_{\min} \end{cases}$$

Frixione isolation



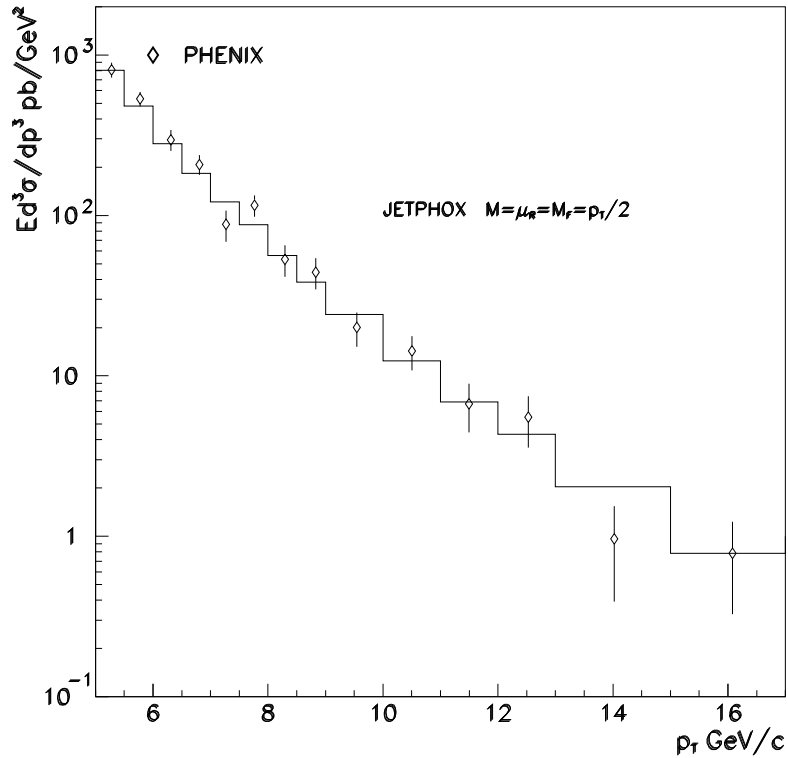
even better: "onion type cones" (now being implemented)
six cones of radius 0.1 to 0.4 in steps of 0.05

Prompt photons at CDF



$$p_T^\gamma > 30 \text{ GeV}, E_{T,\text{max}} = 2 \text{ GeV}, R = 0.4$$

Prompt photons at RHIC



two different methods
of photon isolation

(a) cone: $\epsilon_\gamma = 0.1, R = 0.5$

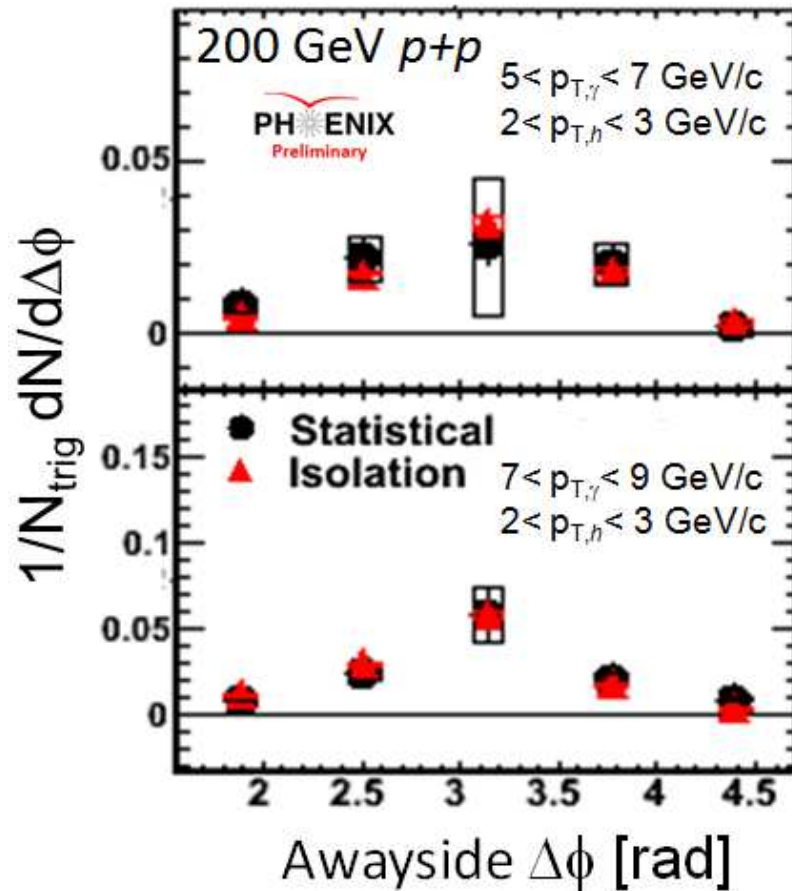
(b) statistical:

direct photon yield Y_{dir}

$$Y_{dir} = \frac{r_\gamma Y_{incl} - Y_{decay}}{r_\gamma - 1}$$

$$r_\gamma = \frac{(\gamma/\pi^0)_{data}}{(\gamma/\pi^0)_{sim}}$$

photon isolation at RHIC



$\Delta\phi$: azimuthal angle between photon and charged hadrons

Summary

- in order to understand "New Physics" at TeV colliders: theory predictions for signals and backgrounds must be well under control

need accuracy beyond Leading Order

Summary

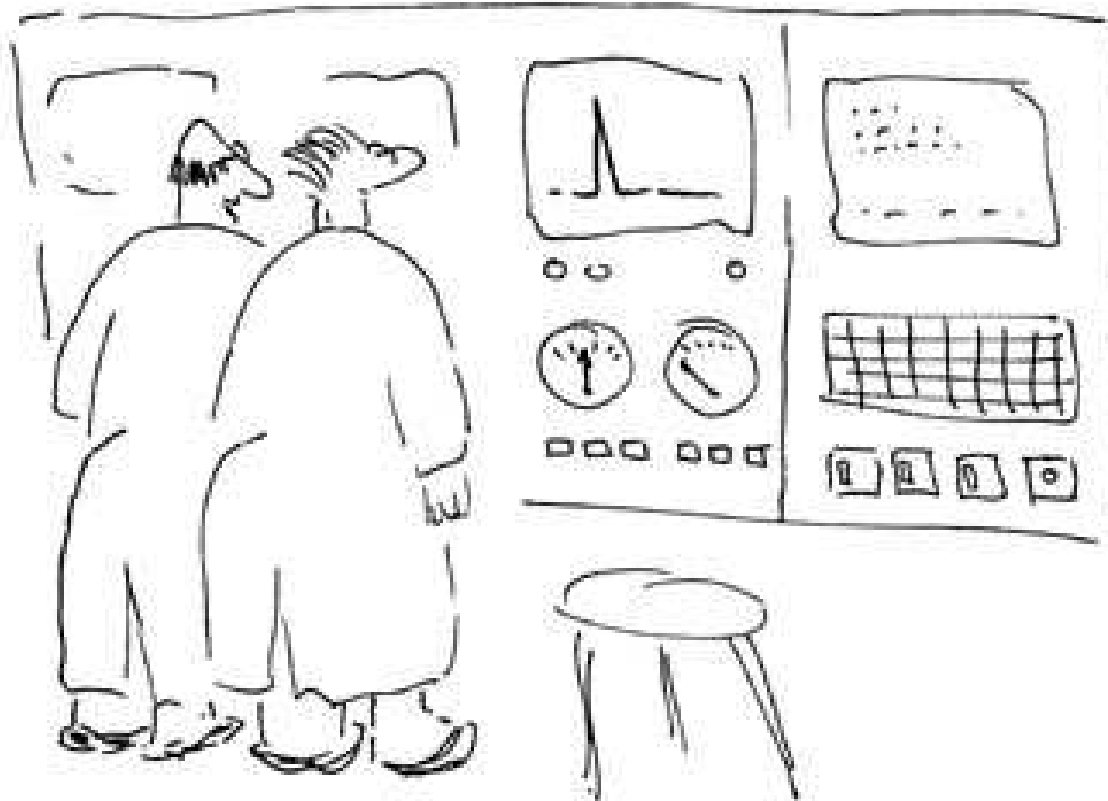
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need accuracy beyond Leading Order

- we are moving towards automated tools for NLO predictions

GOLEM approach:

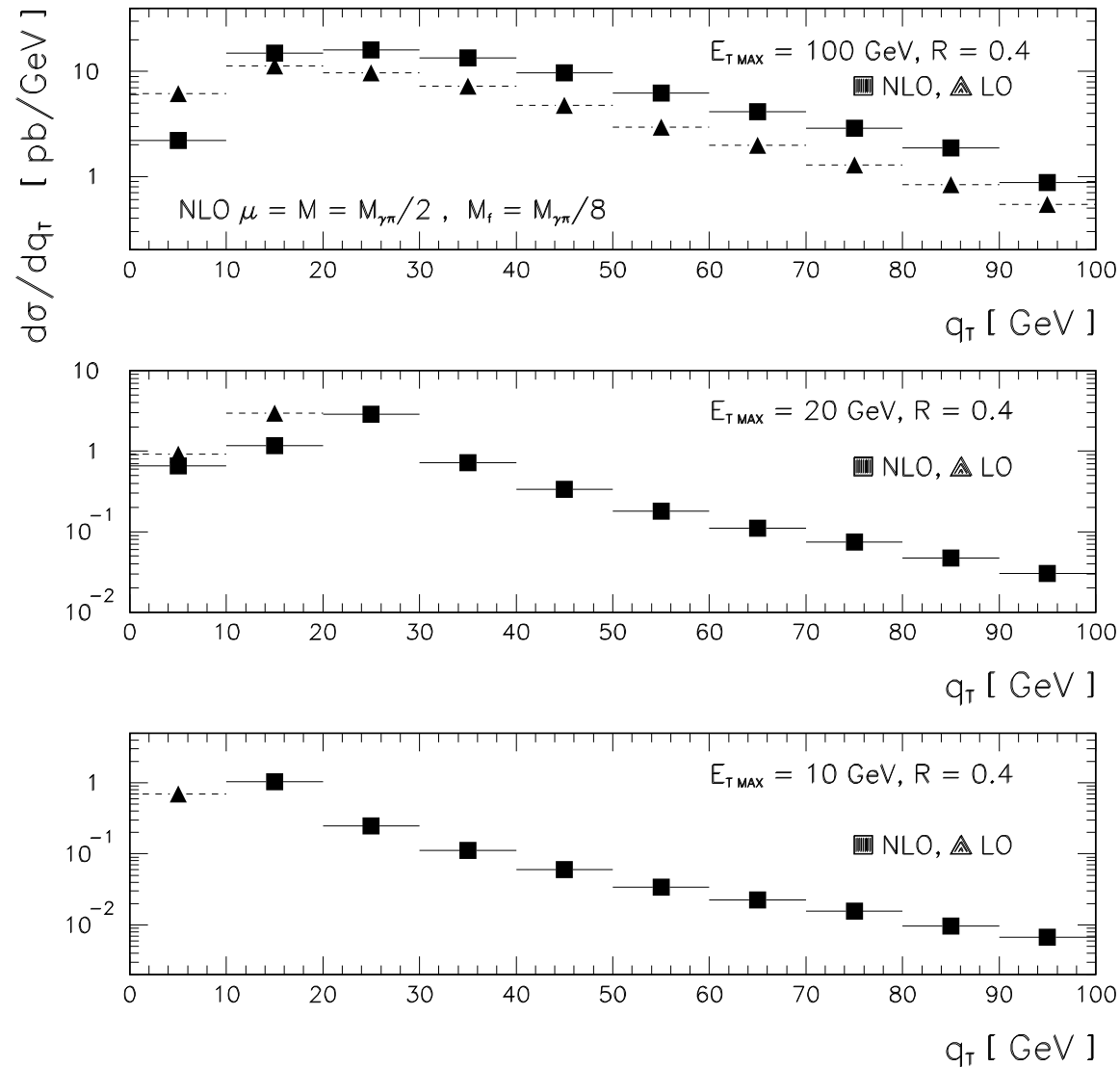
- setup valid for massive and massless particles
- keeps spin information
- combination with parton shower in progress
- tensor integral library publicly available at <http://lappweb.in2p3.fr/lapth/Golem/golem95.html>



“Well, either we’ve found the Higgs boson, or Fred’s just put the kettle on”

backup slides

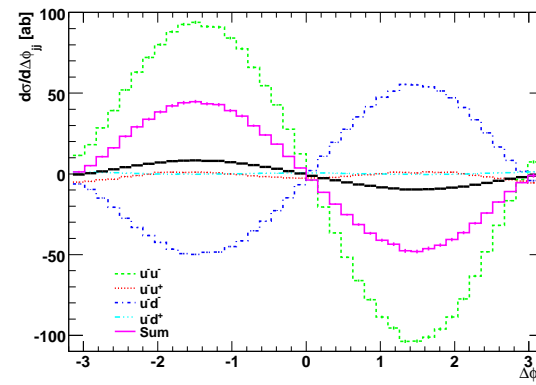
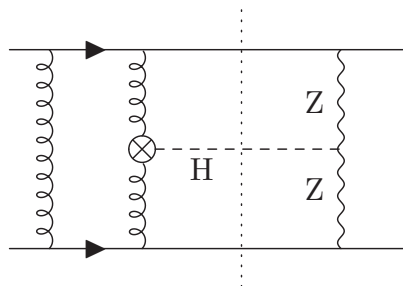
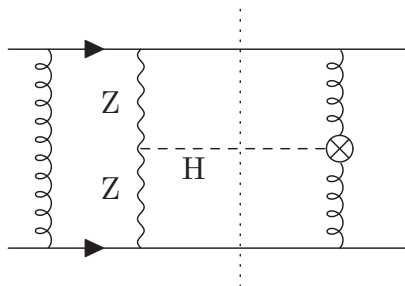
phase space effects enhanced by cuts



Higgs+2 jet one-loop interference

- semi-numerical approach does best
- example: one-loop interference between vector-boson fusion and gluon fusion in Higgs+2 jet production

[Andersen, Binoth, GH, Smillie 07]



- investigate impact of interference on extraction of HZZ coupling from Higgs+2jet events
- calculation of new master integrals involving several mass scales

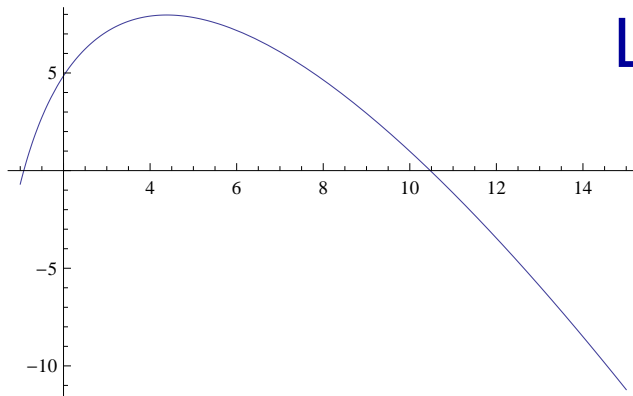
asymptotic complexity

- unitarity based methods:
complexity of **colour ordered** amplitudes:

$$\tau_{\text{tree}} \times \tau_{\text{cuts}} \sim N^4 \times \binom{N}{5} \xrightarrow{N \text{ large}} N^9$$

- Feynman diagram reduction:

$$\tau_{\text{diagrams}} \times \tau_{\text{form factors}} \sim 2^N \times \Gamma(N)$$



$$\text{Log}(N^9 / (\Gamma(N) 2^N))$$

comparison to unitarity methods

NLO results presented at the **RADCOR 2009** conference:

number of talks presenting results:

Unitarity methods: 4

($W + 3$ jets, $Z + 3$ jets, $t\bar{t}b\bar{b}$, cut constructible part of $H + 2$ jets)

Feynman diagrams: 8 + all SUSY/BSM (4) + all electroweak corrections (3)

(WWj , ZZj , $t\bar{t}b\bar{b}$, $b\bar{b}b\bar{b}$, $WW\gamma$, $ZZ\gamma$, $W\gamma j$, $W\gamma\gamma$, $Wb\bar{b}$, $Zb\bar{b}$, $VVjj$ + EW + BSM)

note:

unitarity methods prefer low number of mass scales

Future: expect to discover new heavy particles \Rightarrow rather need more mass scales ...