Tests of Lorentz and CPT Violation with Neutrino Oscillation Experiments

Teppei Katori
Queen Mary University of London
Particle Physics seminar, Univ. of Birmingham, Birmingham, UK, Mar. 11, 2015

Physics of Neutrino Interactions

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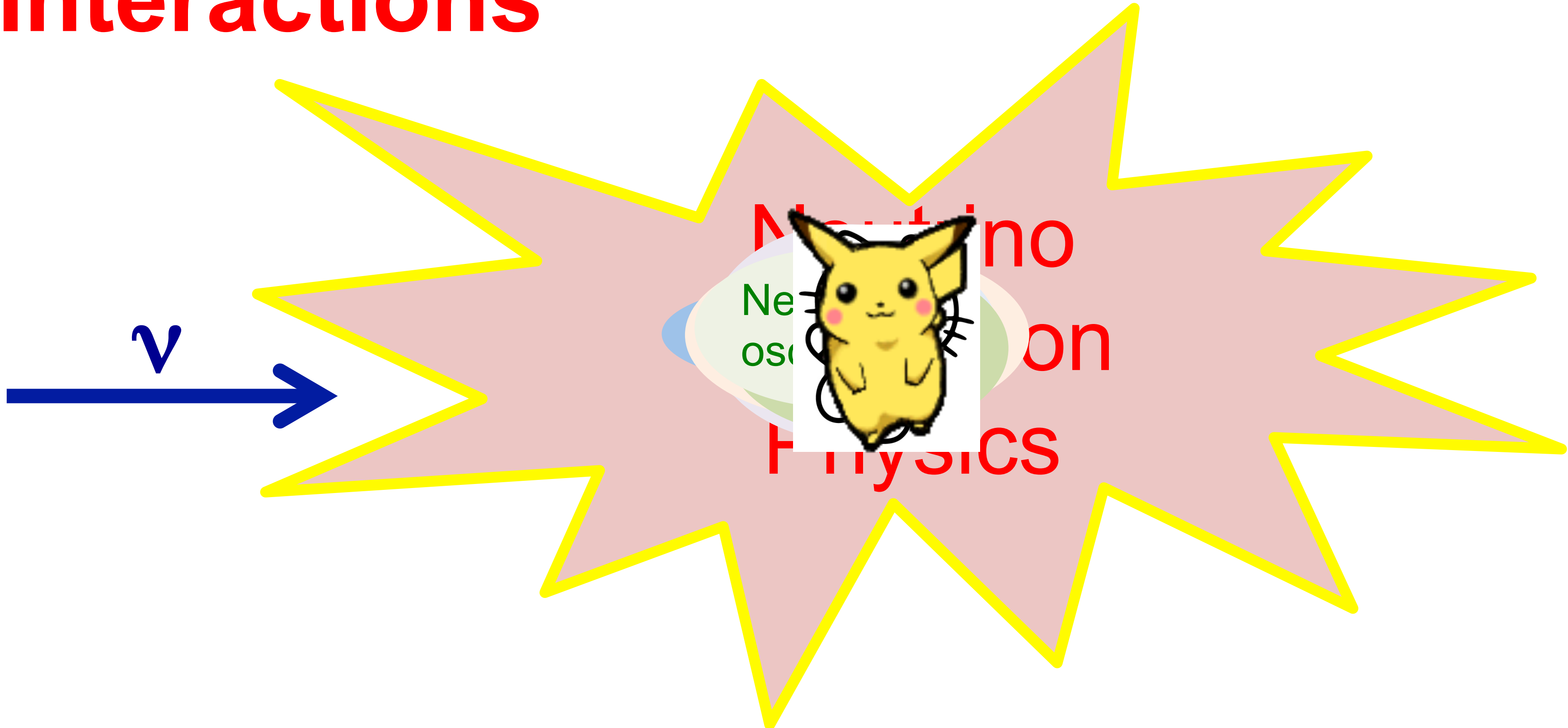

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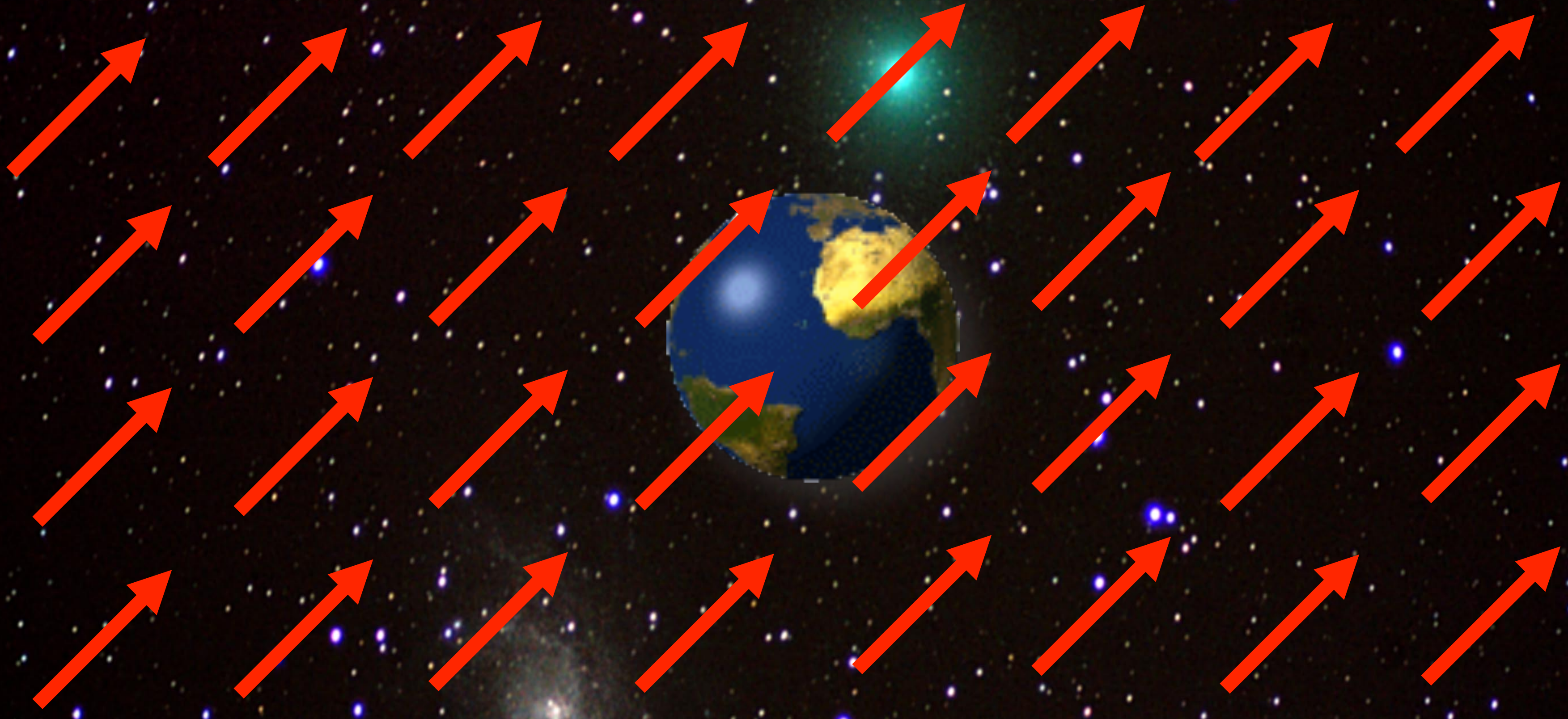

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Tests of Lorentz and CPT Violation with Neutrino Oscillation Experiments

outline

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern test of Lorentz violation
4. Lorentz violating neutrino oscillations
5. Test for Lorentz violation with MiniBooNE data
6. Test for Lorentz violation with Double Chooz data
7. Double Chooz spectrum fit analysis
8. Extra-terrestrial neutrinos
9. Conclusion

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1. **Spontaneous Lorentz symmetry breaking**

2. What is Lorentz and CPT violation?

3. Modern test of Lorentz violation

4. Lorentz violating neutrino oscillation

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1. Spontaneous Lorentz symmetry breaking (SLSB)

Every fundamental symmetry needs to be tested, including Lorentz symmetry.

After the recognition of theoretical processes that create Lorentz violation, testing Lorentz invariance becomes very exciting

Lorentz and CPT violation has been shown to occur in Planck scale theories, including:
- string theory
- noncommutative field theory
- quantum loop gravity
- extra dimensions
- etc

However, it is very difficult to build a self-consistent theory with Lorentz violation...

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Spontaneous Symmetry Breaking (SSB)!

Y. Nambu
(Nobel prize winner 2008),
picture taken from CPT04 at
Bloomington, IN

1. Spontaneous Lorentz symmetry breaking (SLSB)

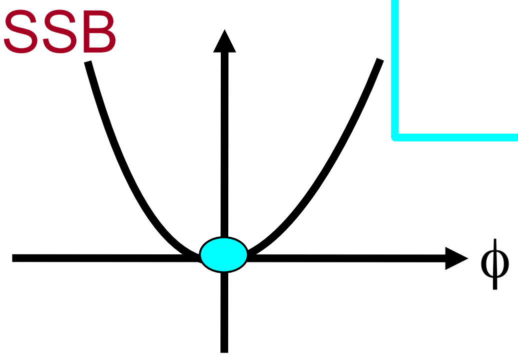
vacuum Lagrangian for fermion $L = i\overline{\Psi}\gamma_{\mu}\partial^{\mu}\Psi$

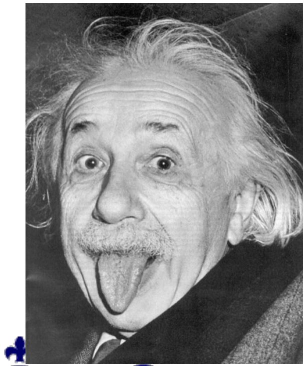
e.g.) SSB of scalar field in Standard Model (SM)

- If the scalar field has Mexican hat potential

$$L = \frac{1}{2}(\partial_{\mu}\varphi)^{2} - \frac{1}{2}\mu^{2}(\varphi^{*}\varphi) - \frac{1}{4}\lambda(\varphi^{*}\varphi)^{2}$$

$$M(\varphi) = \mu^{2} < 0$$





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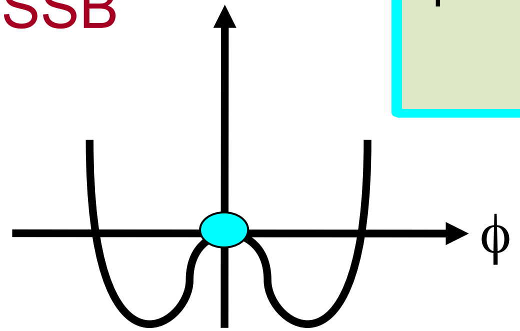
SSB



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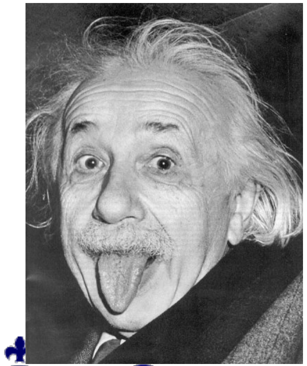

Particle acquires mass term!

Kostelecký and Samuel
PRD39(1989)683

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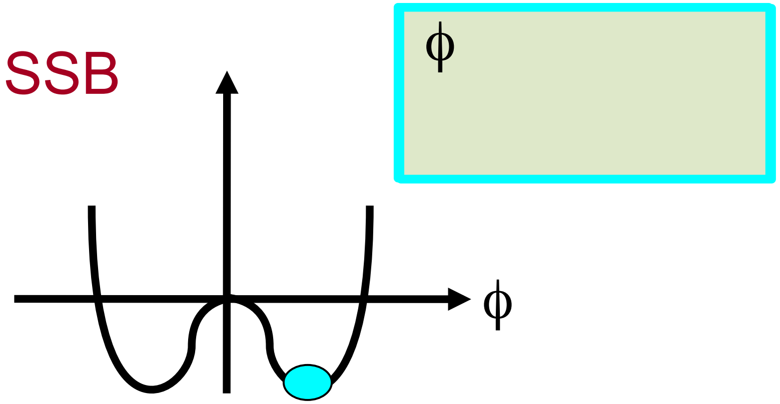
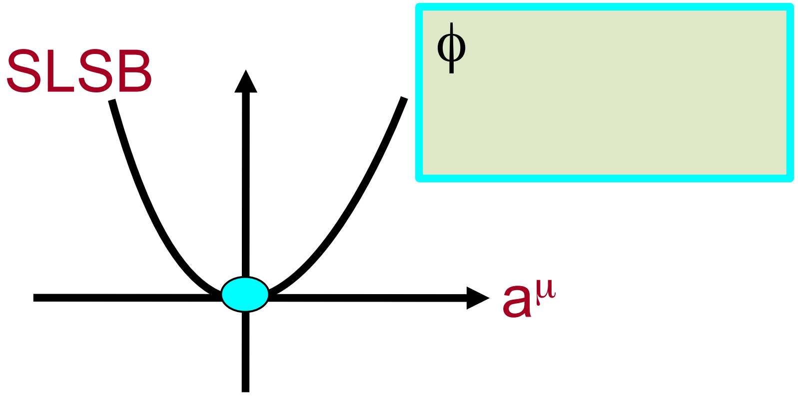
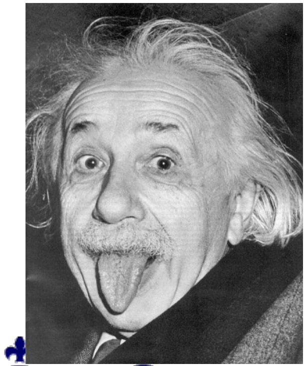


e.g.) SLSB in string field theory

- There are many Lorentz vector fields
- If any of vector field has Mexican hat potential

$$M(a^\mu) = \mu^2 < 0$$





Kostelecký and Samuel
PRD39(1989)683

1. Spontaneous Lorentz symmetry breaking (SLSB)

vacuum Lagrangian for fermion $L = i\bar{\Psi}\gamma_\mu\partial^\mu\Psi - m\bar{\Psi}\Psi + \bar{\Psi}\gamma_\mu a^\mu\Psi$

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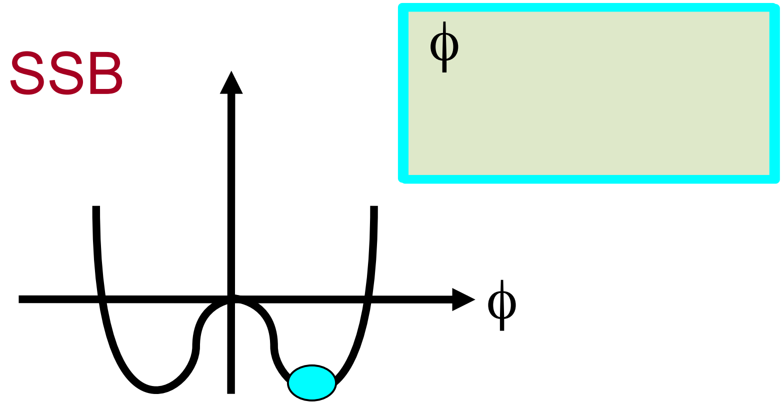

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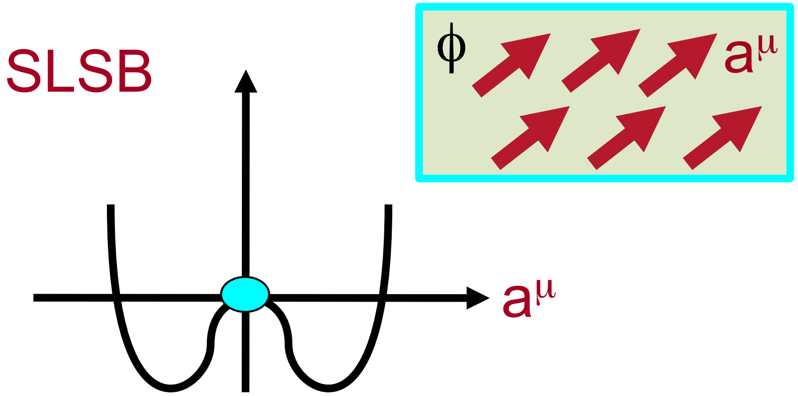
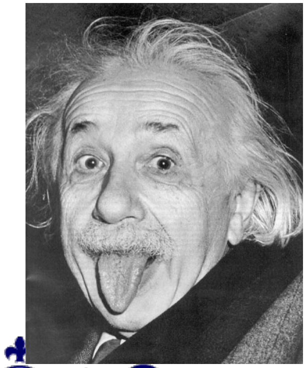




Lorentz symmetry is spontaneously broken!

1. Spontaneous Lorentz symmetry breaking

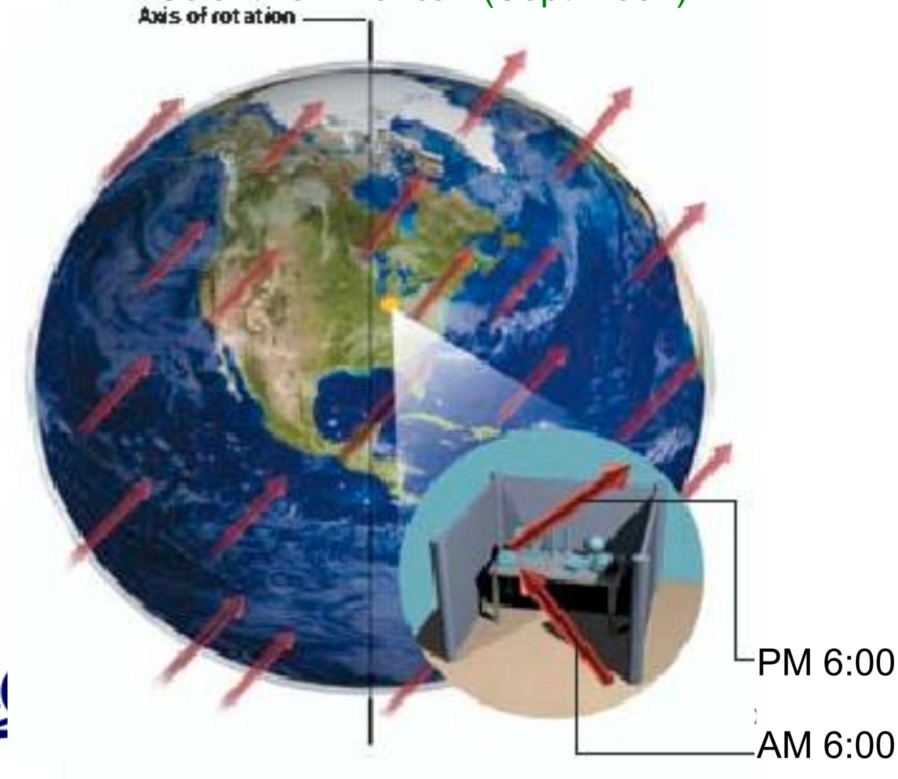
Test of Lorentz violation is to find the coupling of these background fields and ordinary fields (electrons, muons, neutrinos, etc); then the physical quantities may depend on the rotation of the earth (sidereal time dependence).

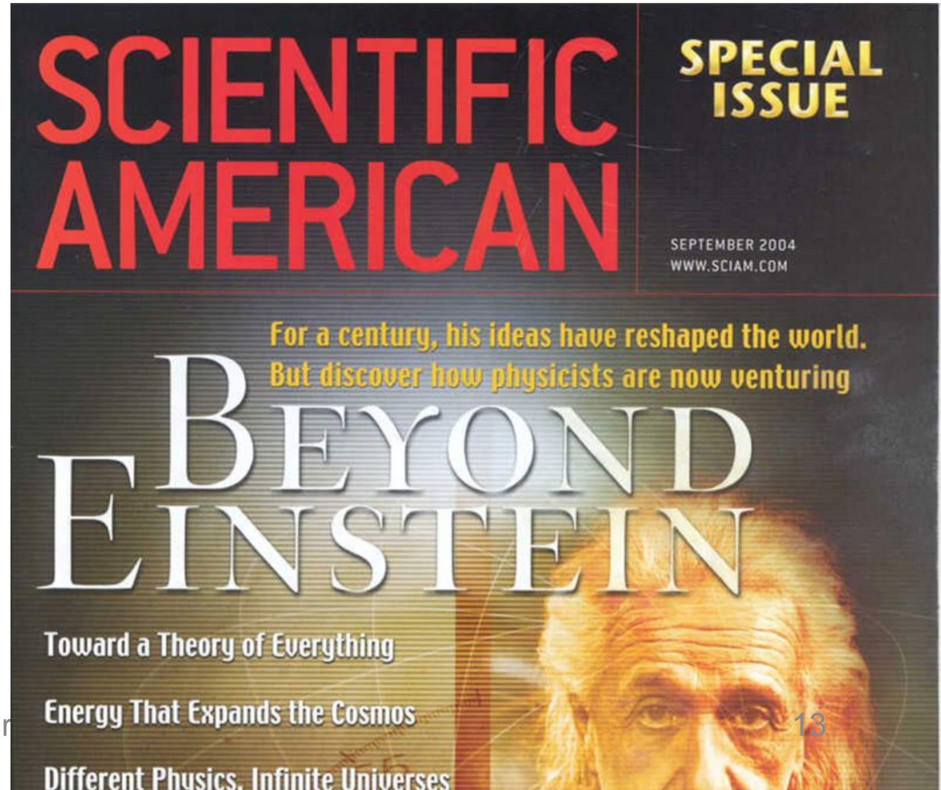
background fields of the universe

vacuum Lagrangian for fermion

$$L = i\bar{\Psi}\gamma_\mu\partial^\mu\Psi - m\bar{\Psi}\Psi + \bar{\Psi}\gamma_\mu\boxed{a^\mu}\Psi + \bar{\Psi}\gamma_\mu\boxed{c^{\mu\nu}}\partial_\nu\Psi\ldots$$

Scientific American (Sept. 2004)





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Sidereal time dependence

The smoking gun of Lorentz violation is the sidereal time dependence of the observables.

Solar time: 24h 00m 00.0s
sidereal time: 23h 56m 04.1s

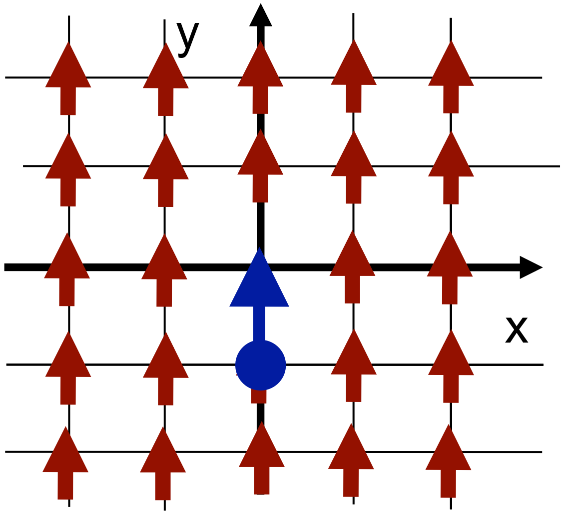
Sidereal time dependent physics is often smeared out in solar time distribution
→ Maybe we have some evidence of Lorentz violation but we just didn't notice?!

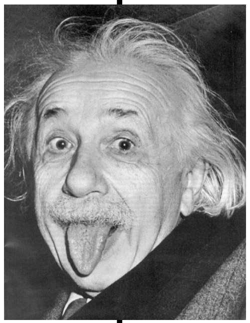
Target scale

Since it is Planck scale physics, either $>10^{19}$GeV or $<10^{-19}$GeV is the interesting region.
$>10^{19}$GeV is not possible (LHC is 10^4GeV), but $<10^{-19}$GeV is possible.

2. What is Lorentz violation?

$\overline{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)$





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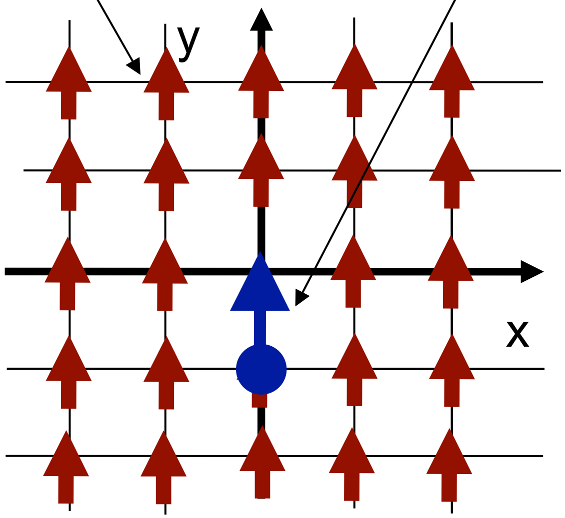
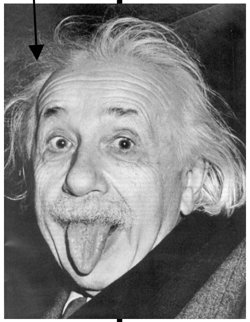


hypothetical background vector field

moving particle

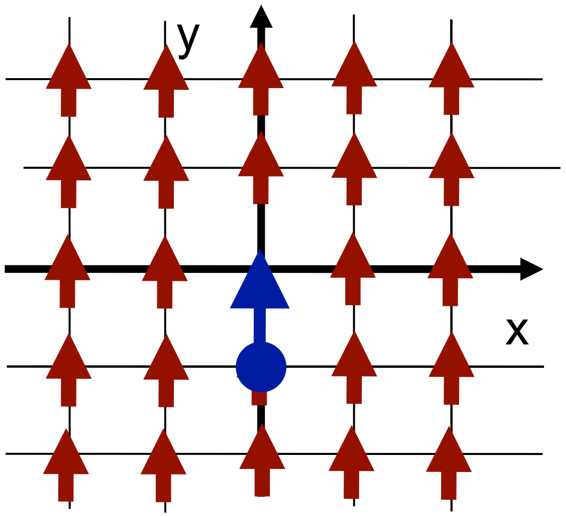
Einstein (observer)

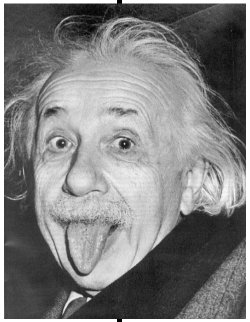


2. What is Lorentz violation?

Under the particle Lorentz transformation:

$$U\bar{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)U^{-1}$$





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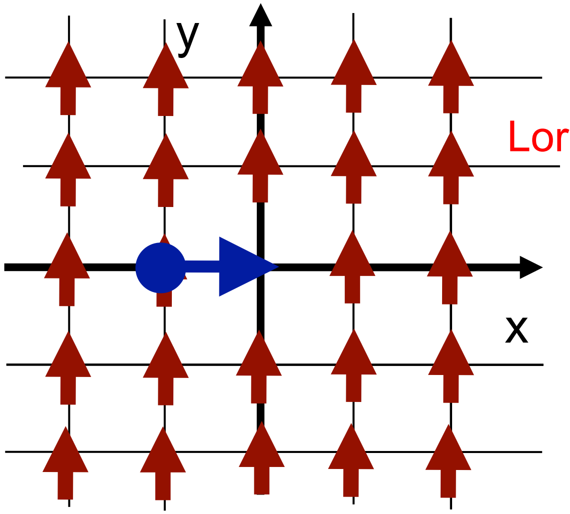
Under the particle Lorentz transformation:

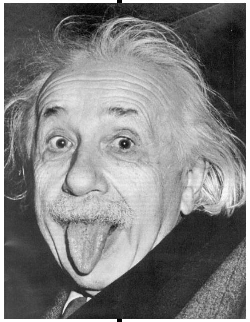
$$\overline{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x) \rightarrow U[\overline{\Psi}(x)\gamma_{\mu}a^{\mu}\Psi(x)]U^{-1}$$

$$\neq \overline{\Psi}(\Lambda x)\gamma_{\mu}a^{\mu}\Psi(\Lambda x)$$

Lorentz violation is observable
when a particle is moving in the
fixed coordinate space



Lorentz violation!



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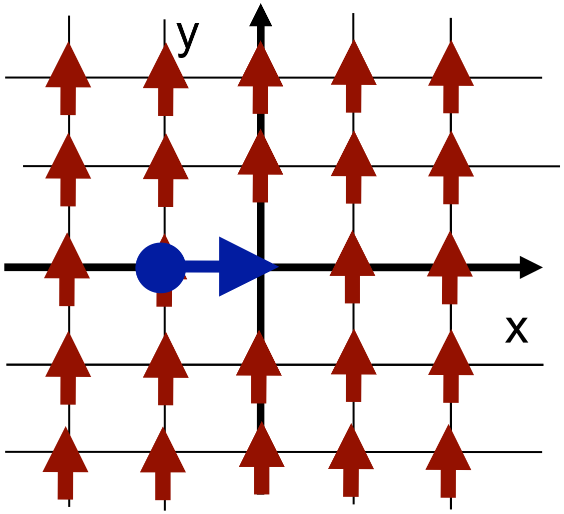
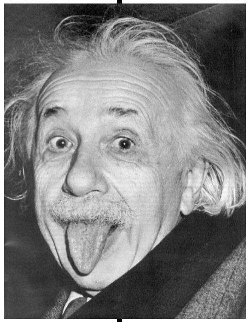
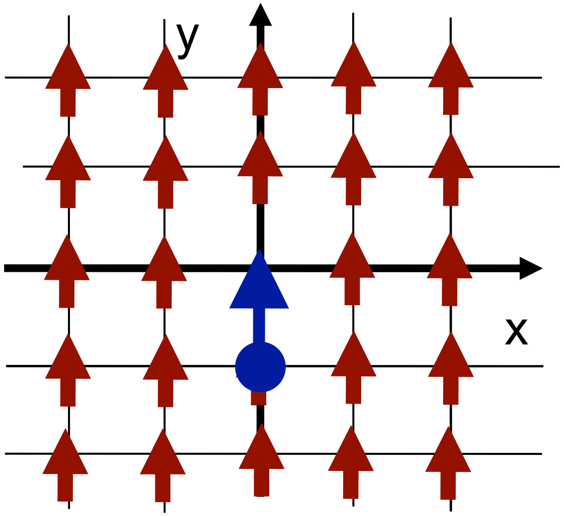




Under the observer Lorentz transformation:

$$\overline{\Psi}(x)\gamma_\mu a^\mu \Psi(x)$$



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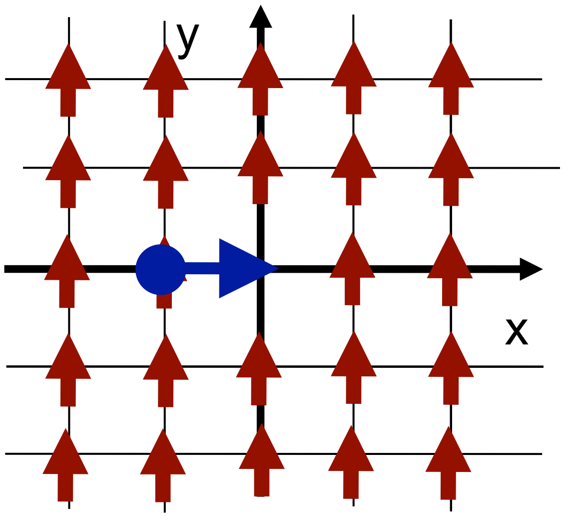
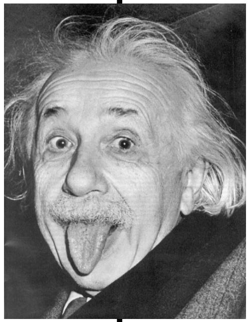
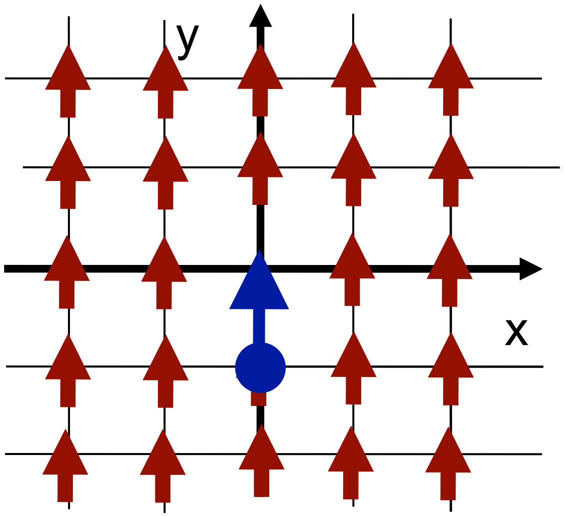




Under the observer Lorentz transformation:

$$\overline{\Psi}(x)\gamma_\mu a^\mu \Psi(x)$$

$$x \rightarrow \Lambda^{-1}x$$



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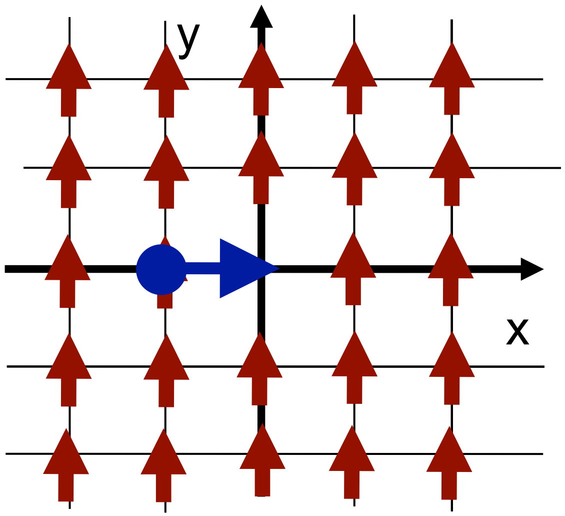
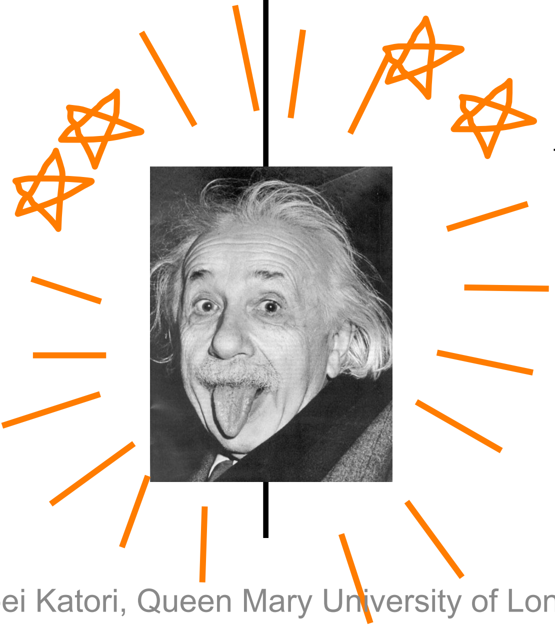


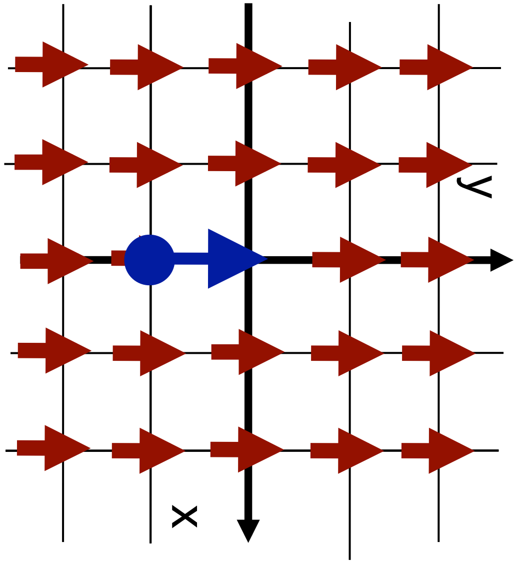


Under the observer Lorentz transformation:

$$\overline{\Psi}(x)\gamma_\mu a^\mu \Psi(x) \xrightarrow{\Lambda^{-1}} \overline{\Psi}(\Lambda^{-1}x)\gamma_\mu a^\mu \Psi(\Lambda^{-1}x)$$

Lorentz violation cannot be generated by observers motion (coordinate transformation is unbroken)

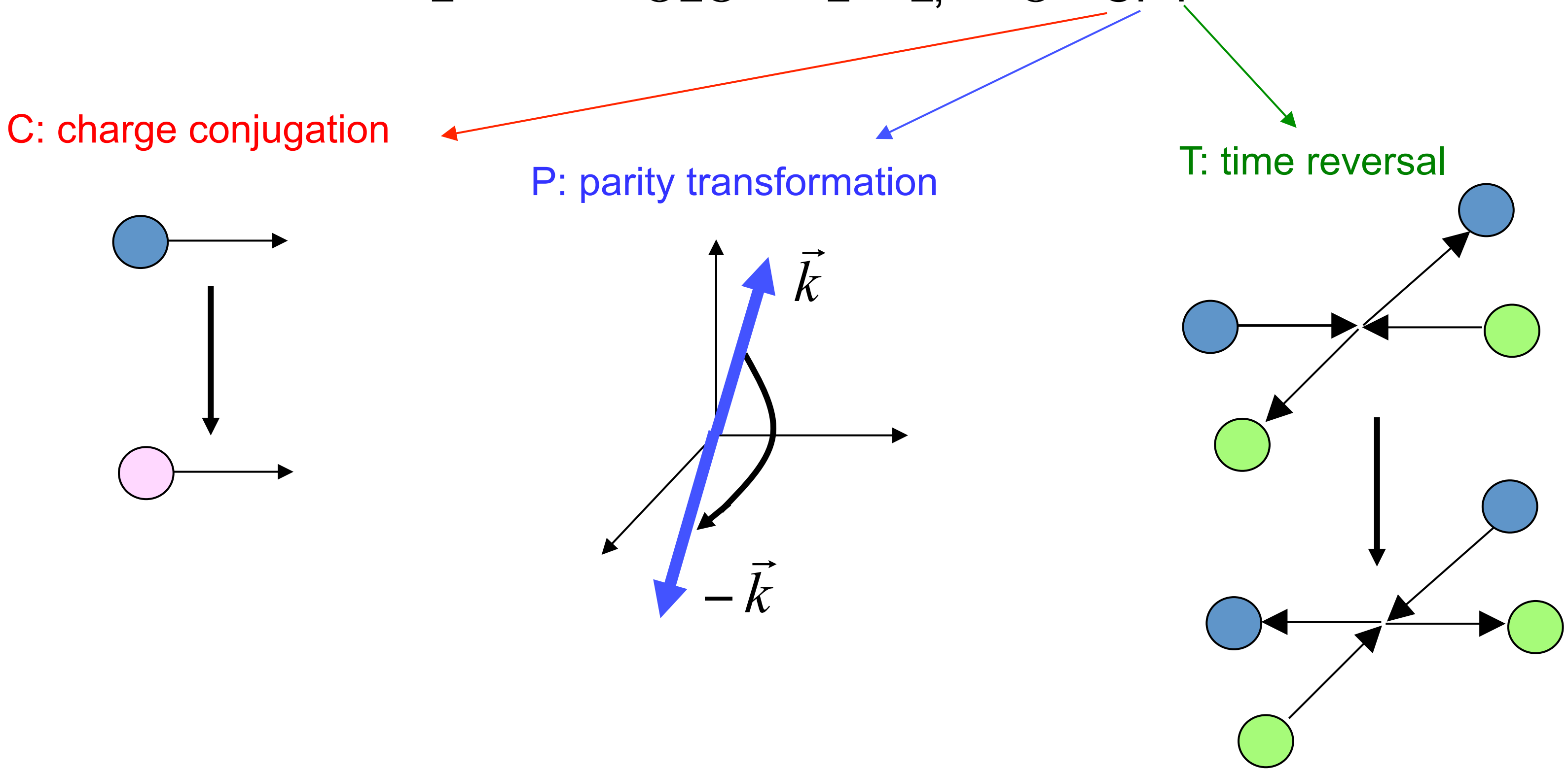
all observers agree for all observations



2. What is CPT violation?

CPT symmetry is the invariance under the CPT transformation

$$\mathrm{L} \xrightarrow{\mathrm{CPT}} \Theta \mathrm{L} \Theta^{-1} = \mathrm{L}' = \mathrm{L}, \qquad \Theta = \mathrm{CPT}$$



C: charge conjugation

P: parity transformation

T: time reversal

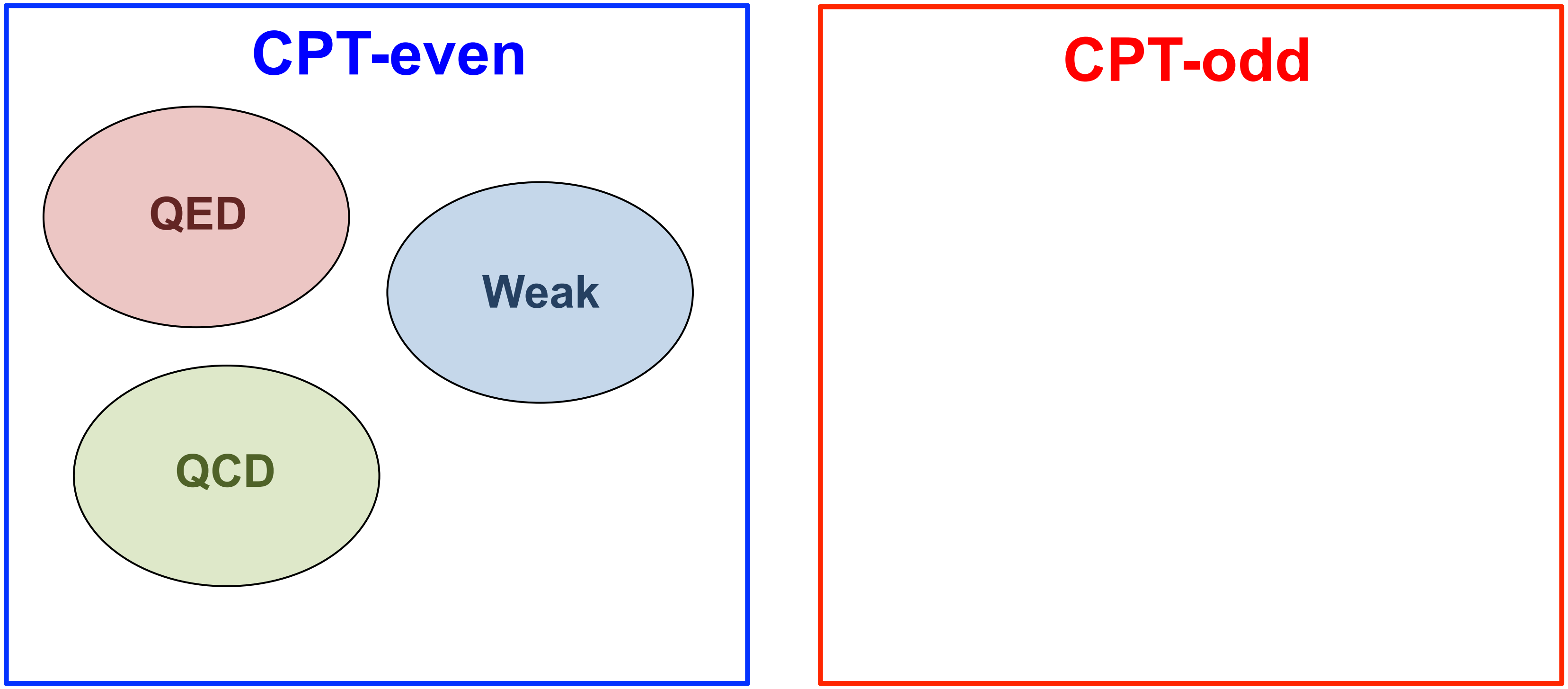
2. What is CPT violation?

CPT phase = $(-1)^n$
n = # Lorentz indices

CPT symmetry is the invariance under the CPT transformation

$$L \xrightarrow{\text{CPT}} \Theta L \Theta^{-1} = L' = L, \qquad \Theta = \text{CPT}$$

CPT is the perfect symmetry of the Standard Model, due to CPT theorem



CPT-even

QED

Weak

QCD

CPT-odd

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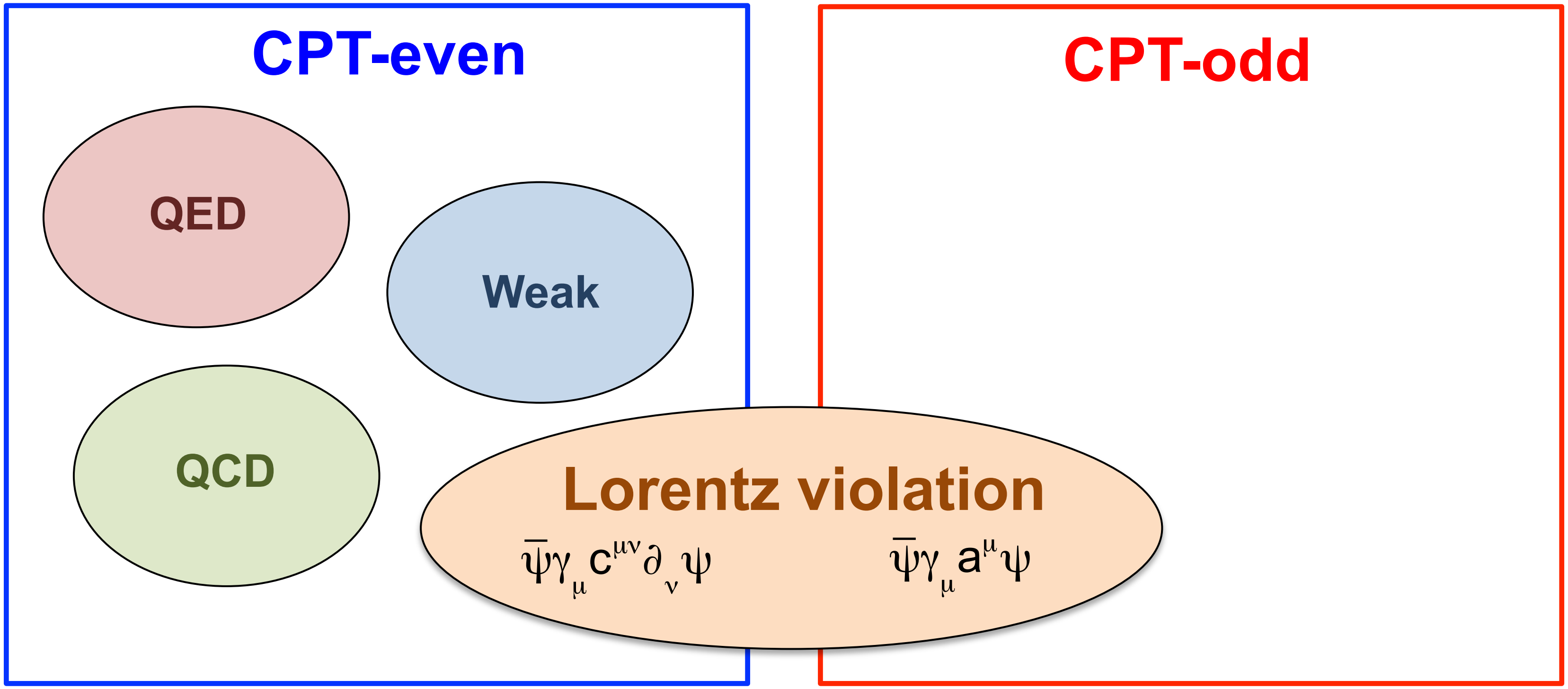


CPT-even

QED

Weak

QCD

Lorentz violation

$\bar{\psi}\gamma_\mu c^{\mu\nu}\partial_\nu\psi$ $\bar{\psi}\gamma_\mu a^\mu\psi$

CPT-odd

CPT-odd Lorentz violating coefficients (odd number Lorentz indices, e.g., a^μ , $g^{\lambda\mu\nu}$)

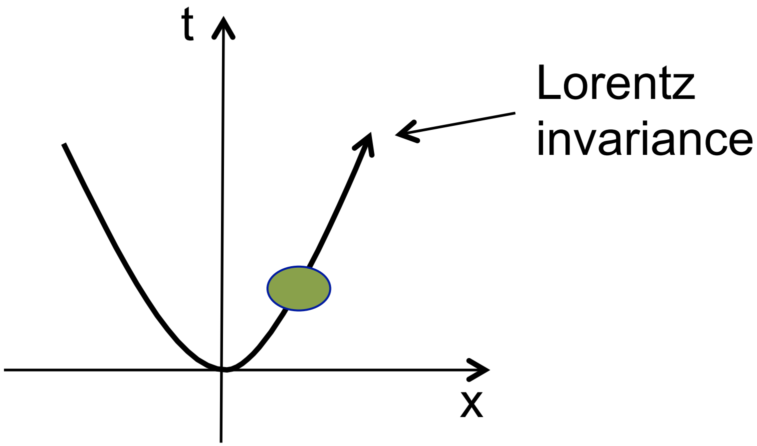
CPT-even Lorentz violating coefficients (even number Lorentz indices, e.g., $c^{\mu\nu}$, $\kappa^{\alpha\beta\mu\nu}$)

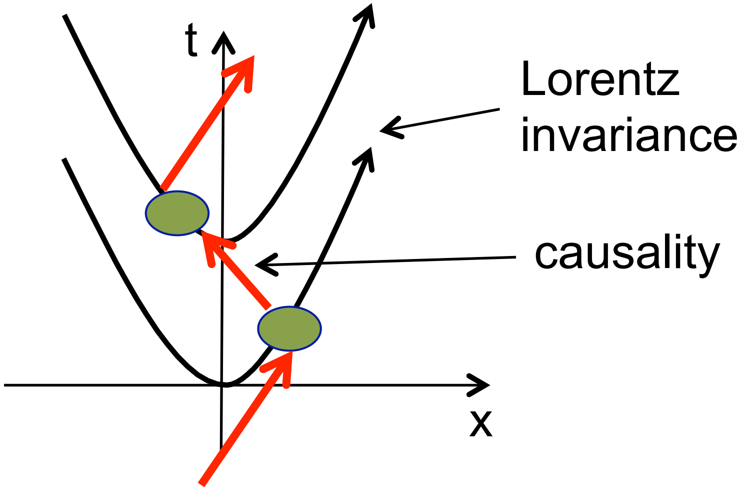
Greenberg, PRL(2002)231602

2. CPT violation implies Lorentz violation

Lorentz invariance → CPT → Lorentz invariance of quantum field theory

CPT violation implies Lorentz violation in interactive quantum field theory.





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Lorentz violation is realized as a coupling of particle fields and background fields, so the basic strategy to find Lorentz violation is:

(1) choose the coordinate system
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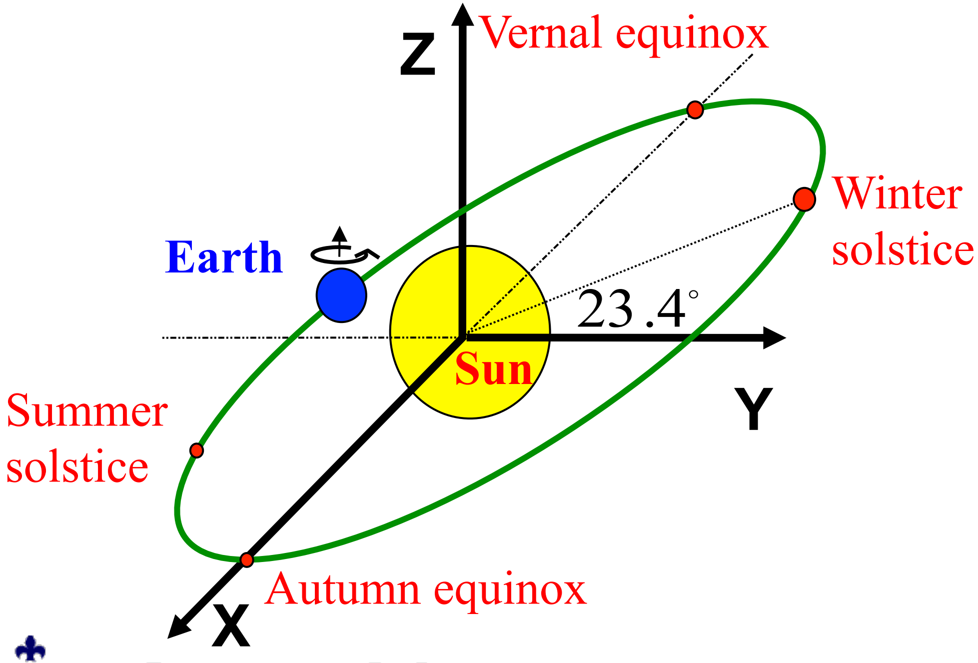
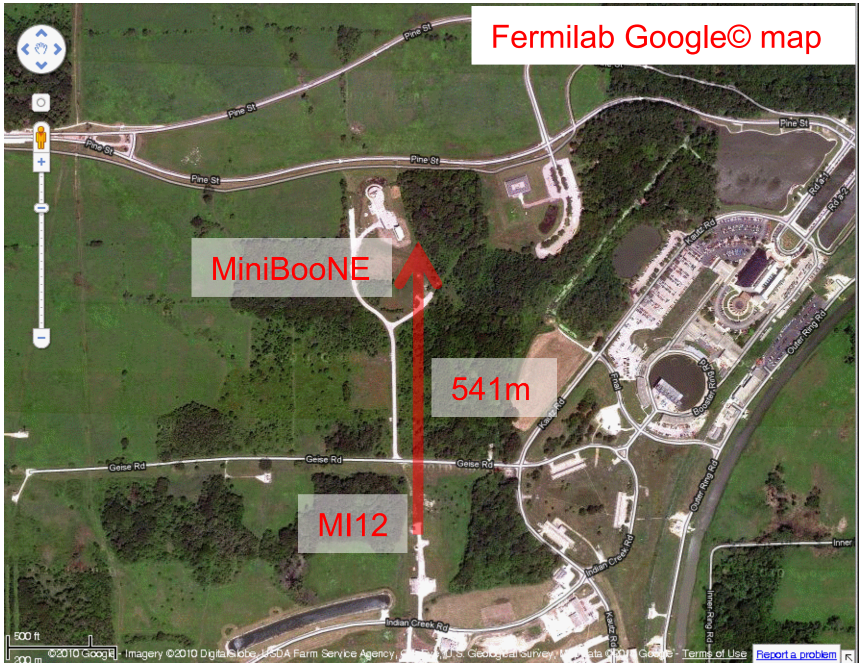
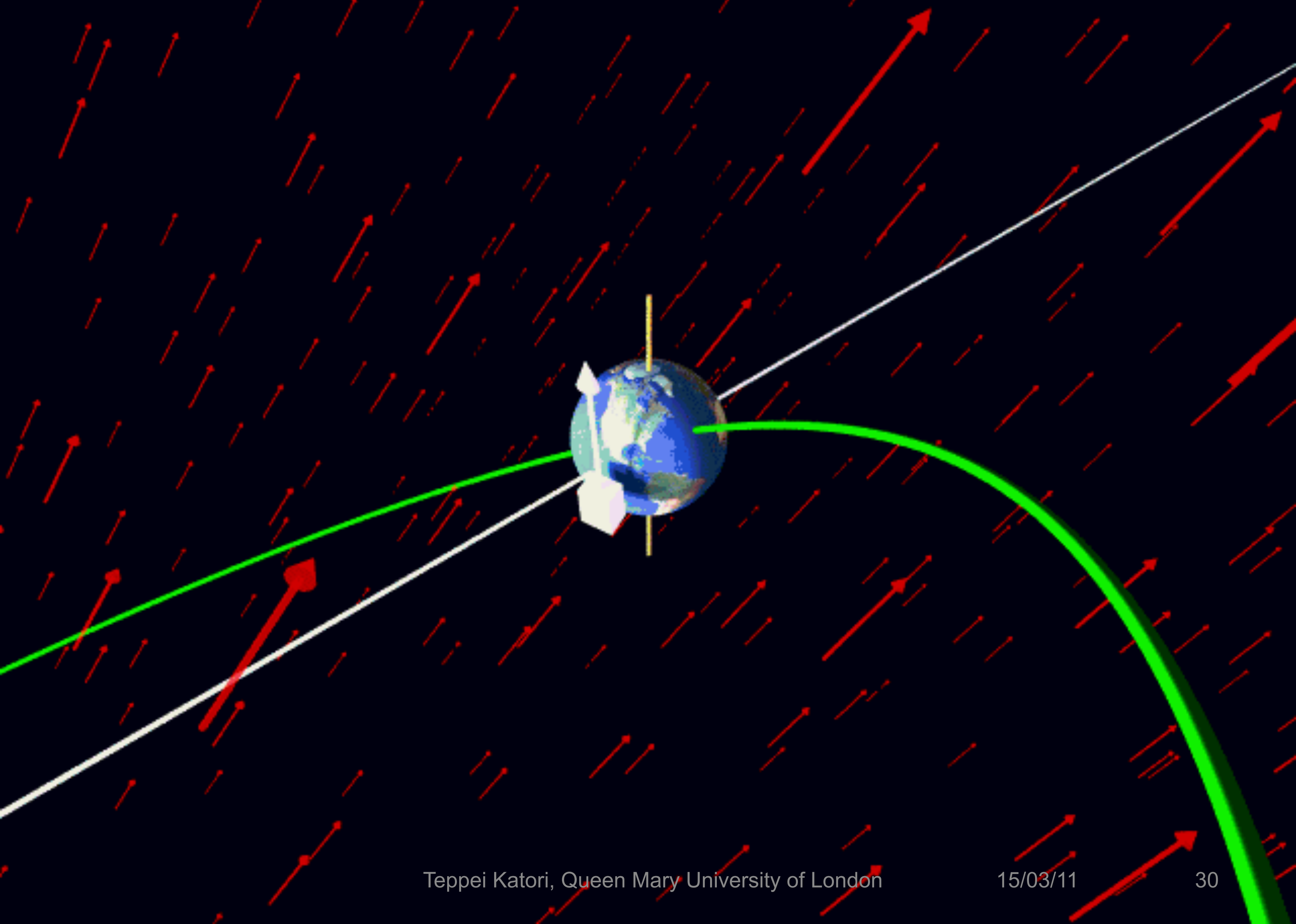
- Neutrino beamline is described in Sun-centred coordinates





MiniBooNE beamline

Bluhm, Kostelecky, Lane, Russell PRL 2002



Kostelecký and Mewes
PRD69(2004)016005

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Standard Model Extension (SME) is the standard formalism for the general search for Lorentz violation. SME is a minimum extension of QFT with Particle Lorentz violation

SME Lagrangian in neutrino sector

$$L = \frac{1}{2} i\bar{\psi}_A \Gamma^{\nu}_{AB} \partial_{\nu} \psi_B - M_{AB} \bar{\psi}_A \psi_B + h.c.$$

SME coefficients

$$\Gamma^{\nu}_{AB} = \gamma^{\nu}\delta_{AB} + c^{\mu\nu}_{AB}\gamma_{\mu} + d^{\mu\nu}_{AB}\gamma_{\mu}\gamma_5 + e^{\nu}_{AB} + if^{\nu}_{AB}\gamma_5 + \frac{1}{2} g^{\lambda\mu\nu}_{AB}\sigma_{\lambda\mu} \cdots$$

$$M_{AB} = m_{AB} + im_{5AB}\gamma_5 + a^{\mu}_{AB}\gamma_{\mu} + b^{\mu}_{AB}\gamma_5\gamma_{\mu} + \frac{1}{2} H^{\mu\nu}_{AB}\sigma_{\mu\nu} \cdots$$

Kostelecký and Mewes
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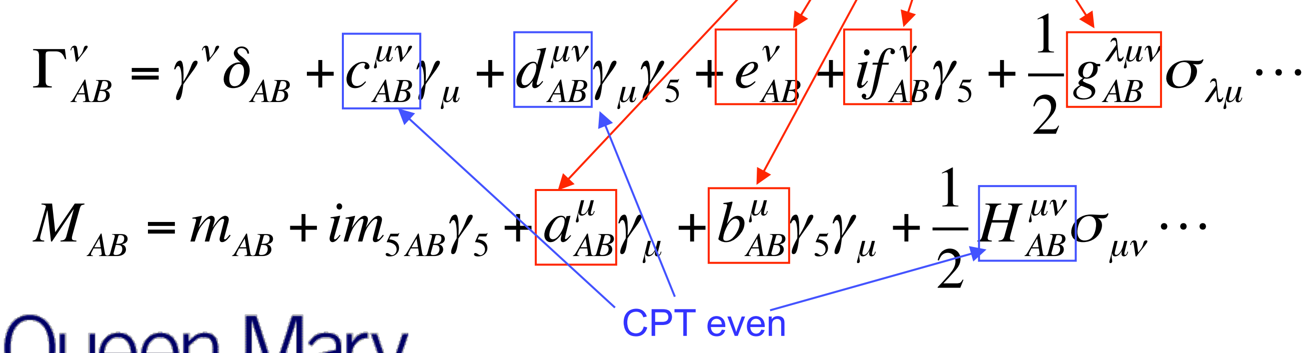
CPT odd

SME coefficients



$$\Gamma^{\nu}_{AB} = \gamma^{\nu} \delta_{AB} + \boxed{c^{\mu\nu}_{AB}} \gamma_{\mu} + \boxed{d^{\mu\nu}_{AB}} \gamma_{\mu} \gamma_5 + \boxed{e^{\nu}_{AB}} + \boxed{i f^{\nu}_{AB}} \gamma_5 + \frac{1}{2} \boxed{g^{\lambda\mu\nu}_{AB}} \sigma_{\lambda\mu} \cdots$$

$$M_{AB} = m_{AB} + i m_{5AB} \gamma_5 + \boxed{a^{\mu}_{AB}} \gamma_{\mu} + \boxed{b^{\mu}_{AB}} \gamma_5 \gamma_{\mu} + \frac{1}{2} \boxed{H^{\mu\nu}_{AB}} \sigma_{\mu\nu} \cdots$$

CPT even

Kostelecký and Mewes
PRD70(2004)076002

3. Test of Lorentz violation

Lorentz violation is realized as a coupling of particle fields and background fields, so the basic strategy to find Lorentz violation is:

(1) choose the coordinate system
(2) write down the Lagrangian, including Lorentz-violating terms under the formalism
(3) write down the observables using this Lagrangian

Various physics are predicted under SME, but among them, the smoking gun of Lorentz violation is the sidereal time dependence of the observables

solar time: 24h 00m 00.0s
sidereal time: 23h 56m 04.1s

sidereal frequency $\omega_\oplus = \dfrac{2\pi}{23h56m4.1s}$

sidereal time $T_\oplus$

Lorentz-violating neutrino oscillation probability for short-baseline experiments

$$P_{\nu_\mu \to \nu_e} = \left(\frac{L}{\hbar c}\right)^2 \left|(C)_{e\mu} + (A_s)_{e\mu}\sin\omega_\oplus T_\oplus + (A_c)_{e\mu}\cos\omega_\oplus T_\oplus + (B_s)_{e\mu}\sin 2\omega_\oplus T_\oplus + (B_c)_{e\mu}\cos 2\omega_\oplus T_\oplus\right|^2$$

Kostelecký and Mewes
PRD70(2004)076002

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Lorentz-violating neutrino oscillation probability for short-baseline experiments

time independent amplitude

sidereal time dependent amplitude

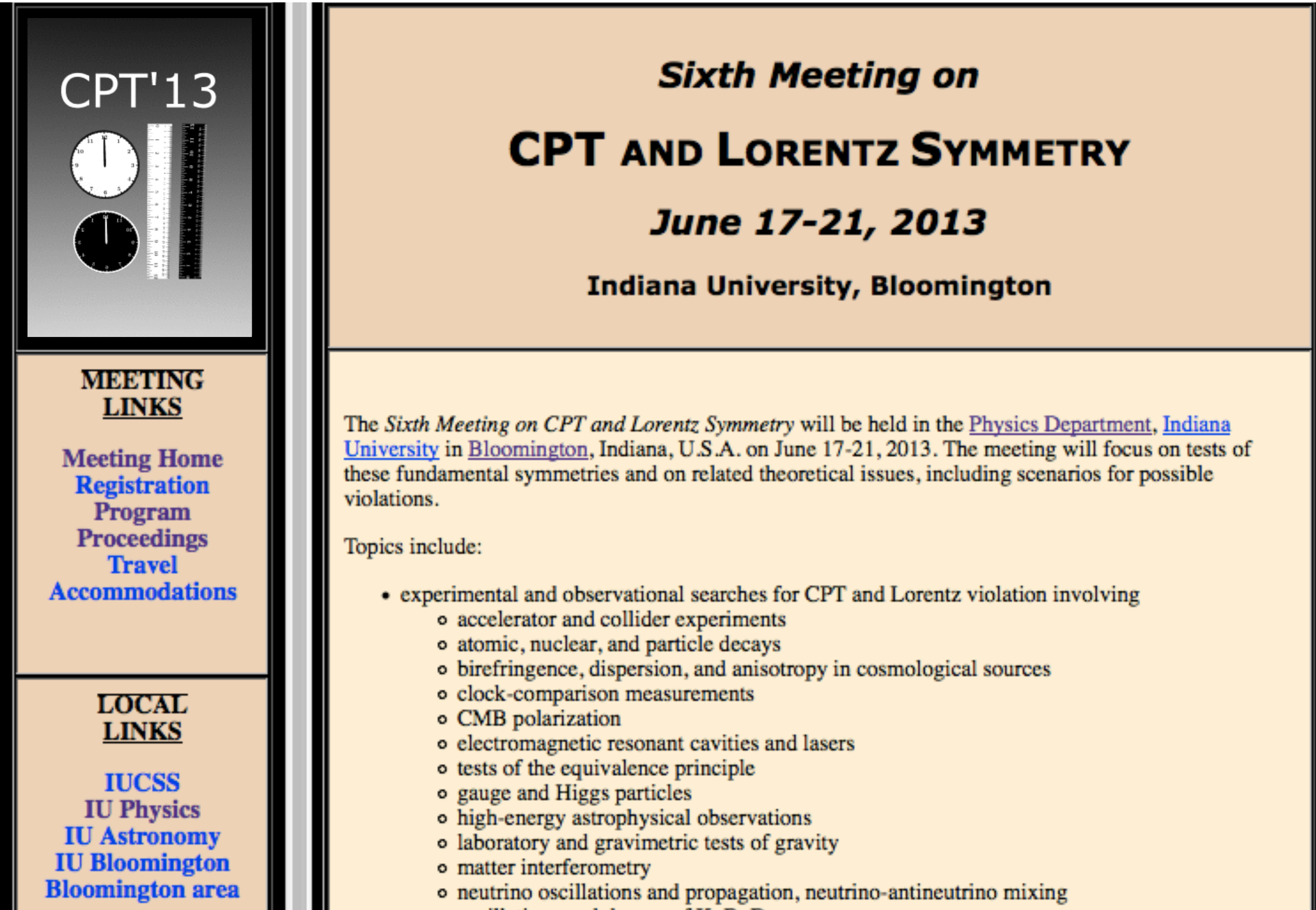
$$P_{\nu_\mu \to \nu_e} = \left(\frac{L}{\hbar c}\right)^2 \left|(C)_{e\mu} + (A_s)_{e\mu} \sin \omega_\oplus T_\oplus + (A_c)_{e\mu} \cos \omega_\oplus T_\oplus + (B_s)_{e\mu} \sin 2\omega_\oplus T_\oplus + (B_c)_{e\mu} \cos 2\omega_\oplus T_\oplus \right|^2$$

Sidereal variation analysis for short baseline neutrino oscillation is 5-parameter fitting problem

3. Modern tests of Lorentz violation

The latest meeting was in June 2013
(The next meeting is June 2016)

http://www.physics.indiana.edu/~kostelec/faq.html



MEETING LINKS

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Proceedings
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LOCAL LINKS

IUCSS
IU Physics
IU Astronomy
IU Bloomington
Bloomington area

Sixth Meeting on

CPT AND LORENTZ SYMMETRY

June 17-21, 2013

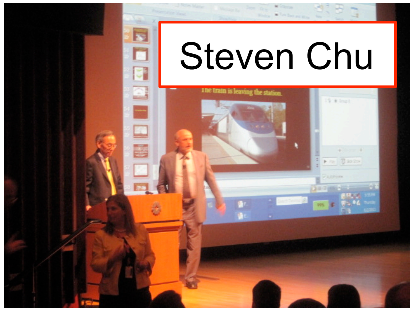
Indiana University, Bloomington

The *Sixth Meeting on CPT and Lorentz Symmetry* will be held in the Physics Department, Indiana University in Bloomington, Indiana, U.S.A. on June 17-21, 2013. The meeting will focus on tests of these fundamental symmetries and on related theoretical issues, including scenarios for possible violations.

Topics include:

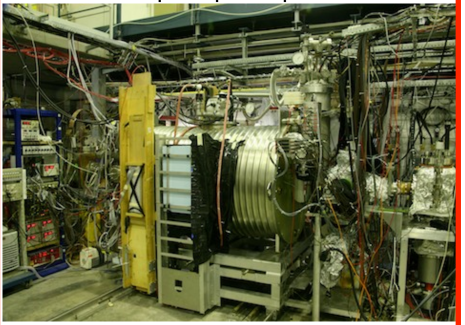
- experimental and observational searches for CPT and Lorentz violation involving
  - accelerator and collider experiments
  - atomic, nuclear, and particle decays
  - birefringence, dispersion, and anisotropy in cosmological sources
  - clock-comparison measurements
  - CMB polarization
  - electromagnetic resonant cavities and lasers
  - tests of the equivalence principle
  - gauge and Higgs particles
  - high-energy astrophysical observations
  - laboratory and gravimetric tests of gravity
  - matter interferometry
  - neutrino oscillations and propagation, neutrino-antineutrino mixing

Atomic Interferometer
$(a,c)^{n,p,e} < 10^{-6}$



PRL106(2011)151102

CERN Antiproton Decelerat
$(M_p-\overline{M}_p)/M_p<10^{-8}$



Nature419(2002)456

Spin torsion pendulum
$b_e<10^{-30}$ GeV

PRL9

Tevatron and LEP
$-5.8\times10^{-12}<\kappa_{tr}-4/3c_e^{00}<1.2\times10^{-11}$

PRL102(2009)170402

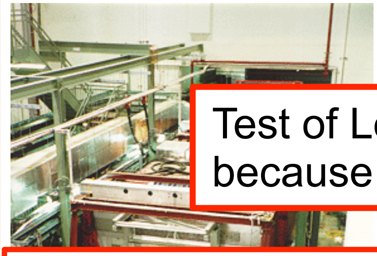
Neutrino TOF
$(v-c)/c<10^{-5}$

PRD76(2007)072005
JHEP11(2012)049

GRB vacuum birefringence
$\kappa_{e+}, \kappa_{o-}<10^{-37}$

PRL97(2006)140401

KTeV/KLOE (strange)
$\Delta a_K<10^{-22}$ GeV
FOCUS (charm)
$\Delta a_D<10^{-16}$ GeV
BaBar/Belle (bottom)
$\Delta m_B/m_B<10^{-14}$



PLB556(2003)7
PRL100(2008)131802

Limits from all these
experiments >50 page tables!
Rev.Mod.Phys.83(2011)11
ArXiv:0801.0287v6

laboratory and gravimetric tests of gra
matter interferometry
- neutrino oscillations and propagation, neutrino-antineutrino mixing
- oscillations and decays of K, B, D mesons

space-based missions

classical and quantum field the
mathematical foundations, Fins

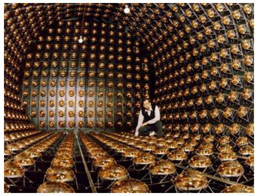
uble gas maser
tation)$<10^{-33}$GeV
oost)$<10^{-27}$GeV

PRL105(2010)151604
PRL107(2010)171604

PRL99(2007)050401

Test of Lorentz invariance with neutrino oscillation is very interesting, because neutrinos are the least known standard model particles!

LSND

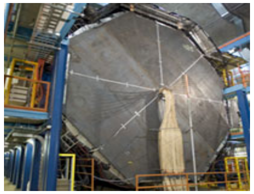


PRD72(2005)076004

MINOS ND

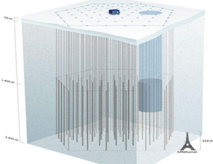
PRL101(2008)151601

MINOS FD



PRL105(2010)151601

IceCube

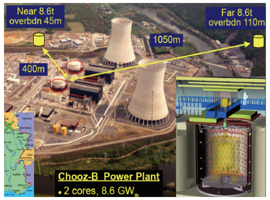


PRD82(2010)112003

MiniBooNE

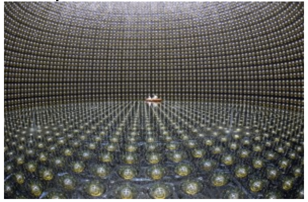
PLB718(2013)1303

Double Chooz



PRD86(2013)112009

Super-Kamiokande

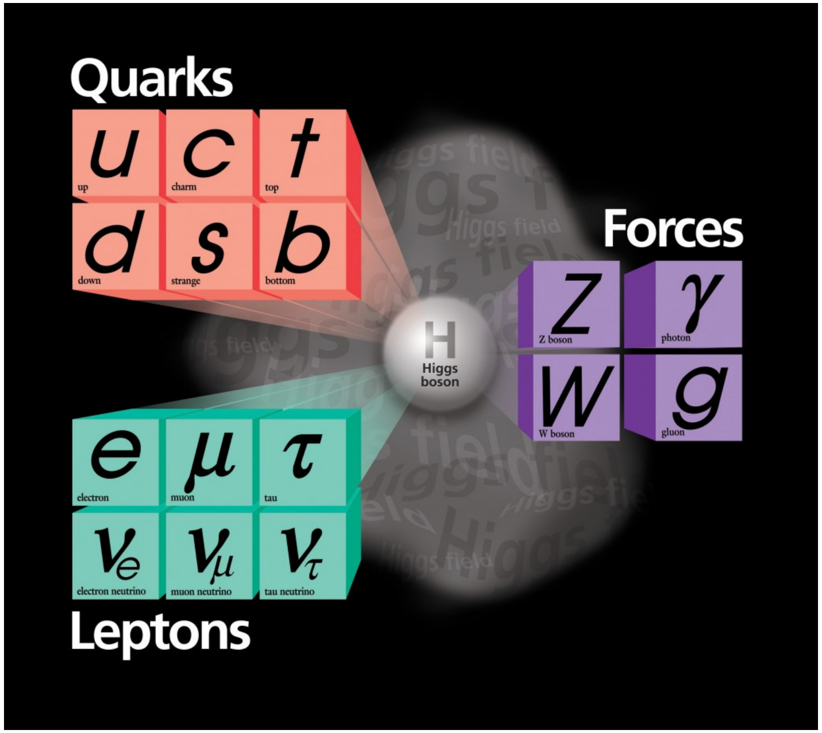


PRD91(2015)052003

4. Neutrinos

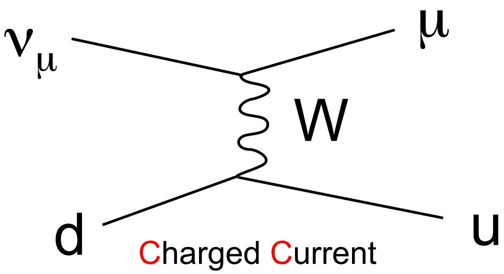
Neutrinos in the standard model

The standard model describes 6 quarks and 6 leptons and 3 types of force carriers.

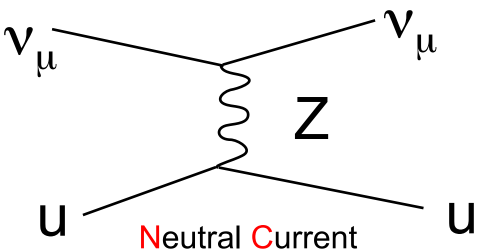


Neutrinos are special because,

1. they only interact with weak nuclear force.



Charged Current
(CC) interaction
"W-boson exchange"

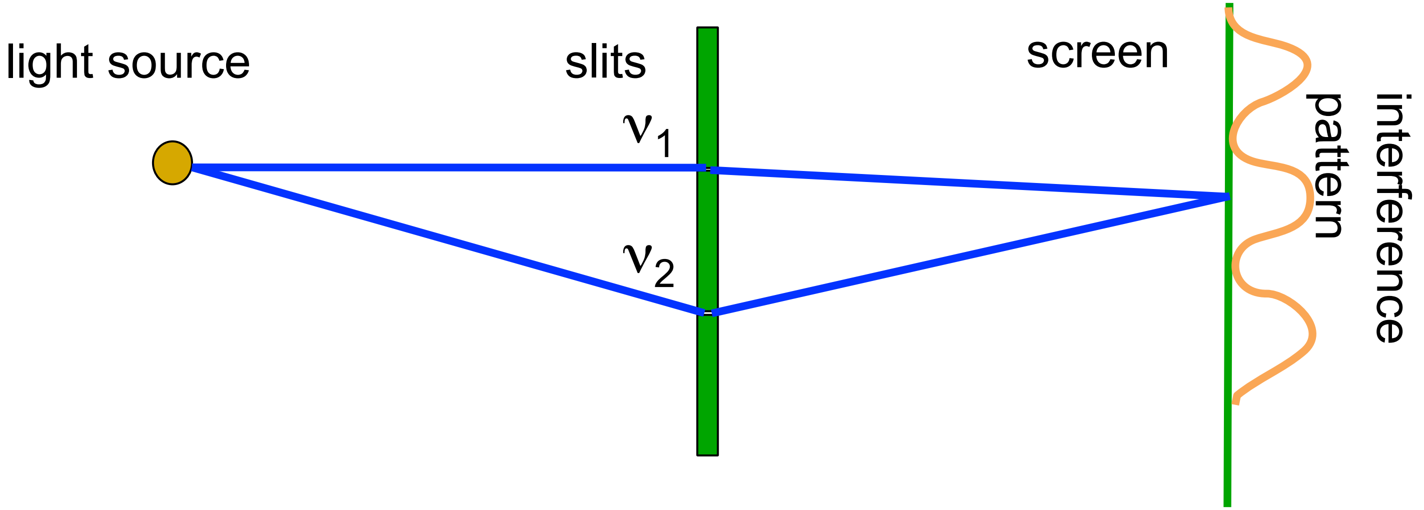


Neutral Current
(NC) interaction
"Z-boson exchange"

2. interaction eigenstate is not Hamiltonian eigenstate (propagation eigenstate). Thus propagation of neutrinos changes their species, called neutrino oscillation.

4. Neutrino oscillations, natural interferometers

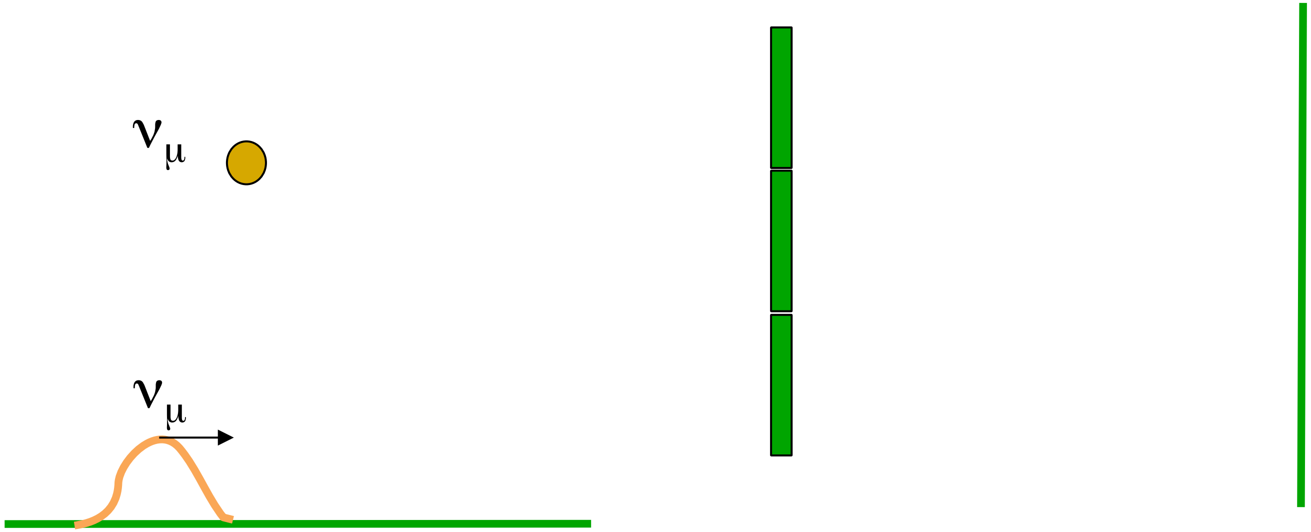
Neutrino oscillation is an interference experiment (cf. double slit experiment)



For double slit experiment, if path ν_1 and path ν_2 have different length, they have different phase rotations and it causes interference.

4. Neutrino oscillations, natural interferometers

Neutrino oscillation is an interference experiment (cf. double slit experiment)



If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2, have different phase rotation, they cause quantum interference.

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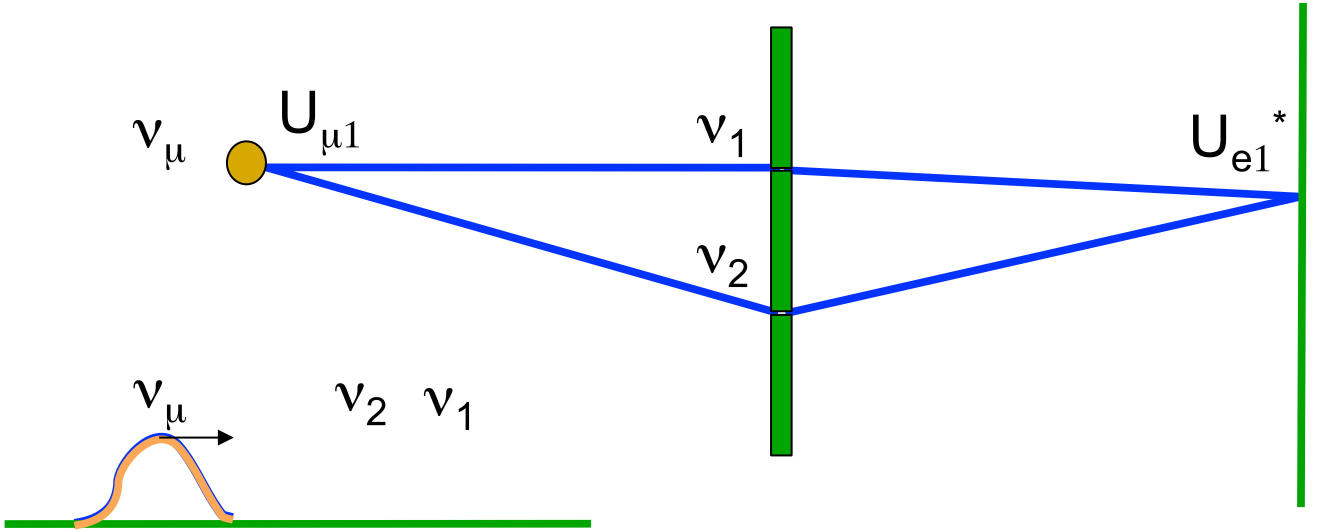

If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2, have different phase rotation, they cause quantum interference.

If ν_1 and ν_2, have different mass, they have different velocity, so thus different phase rotation.

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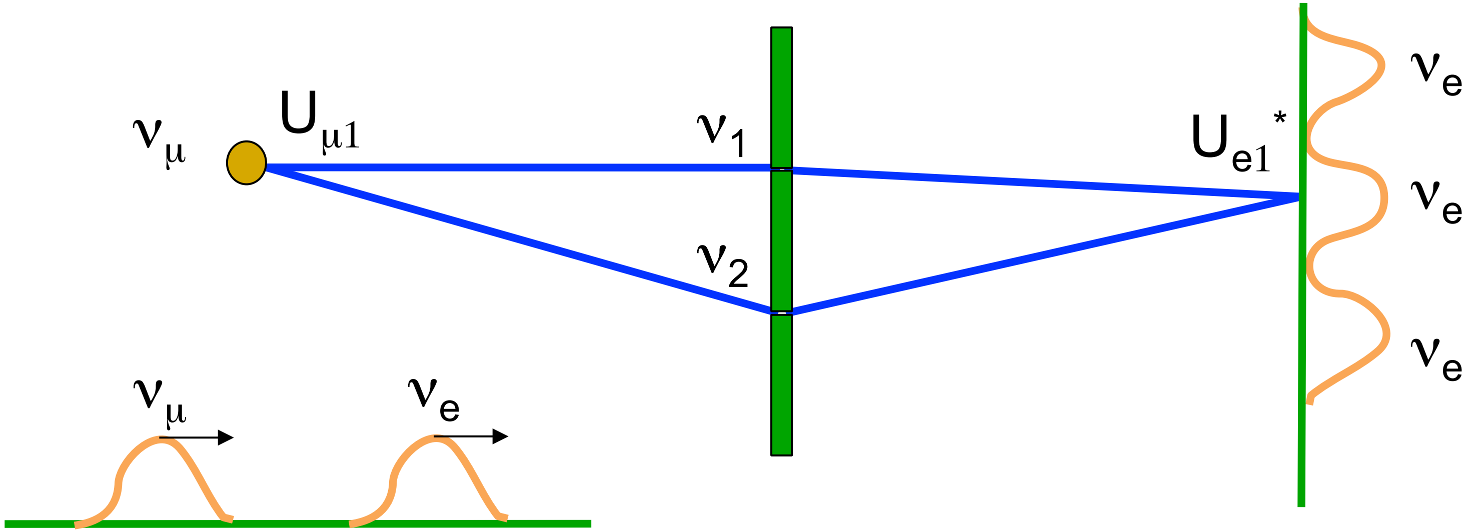


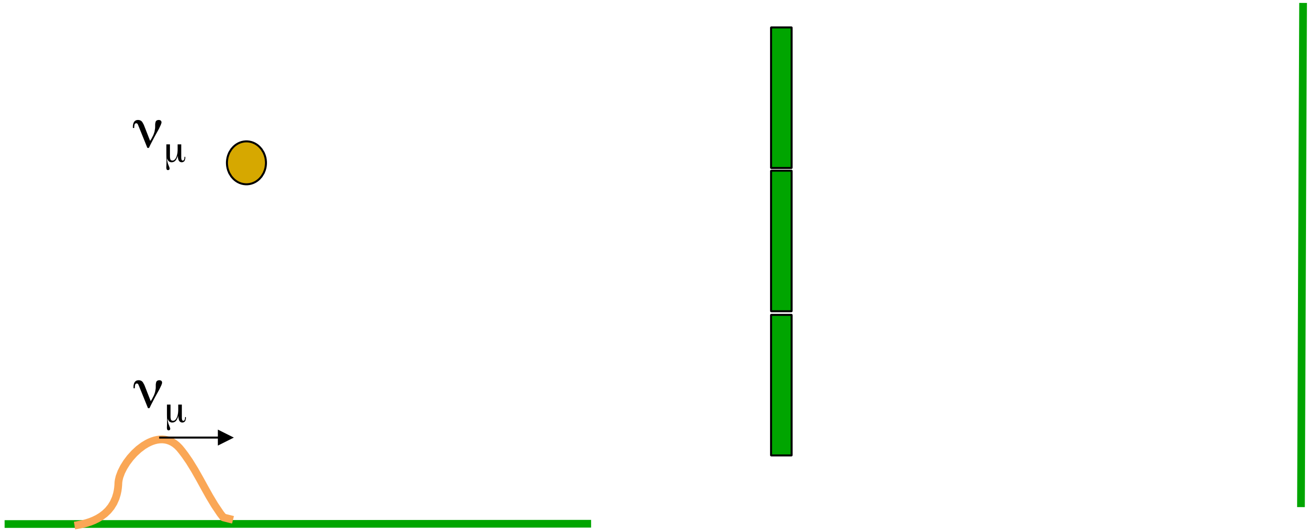
If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2, have different phase rotation, they cause quantum interference.

If ν_1 and ν_2, have different mass, they have different velocity, so thus different phase rotation.

The detection may be different flavor (neutrino oscillations).

4. Lorentz violation with neutrino oscillation

Neutrino oscillation is an interference experiment (cf. double slit experiment)



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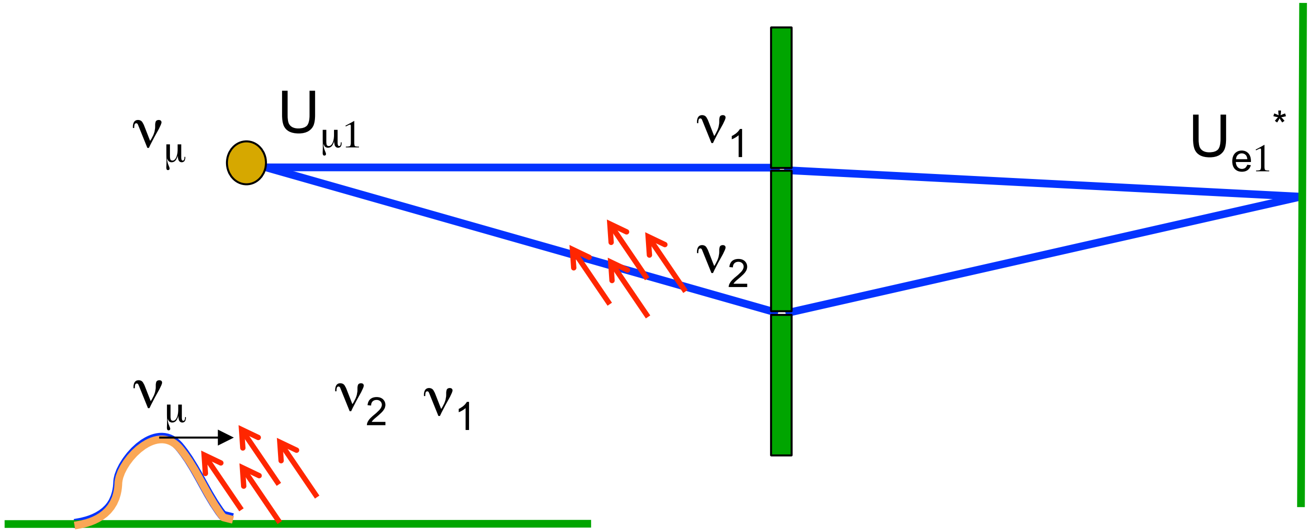

If 2 neutrino Hamiltonian eigenstates, ν_1 and ν_2, have different phase rotation, they cause quantum interference.

If ν_1 and ν_2, have different coupling with Lorentz violating field, neutrinos also oscillate. The sensitivity of neutrino oscillation is comparable the target scale of Lorentz violation ($<10^{-19}$GeV).

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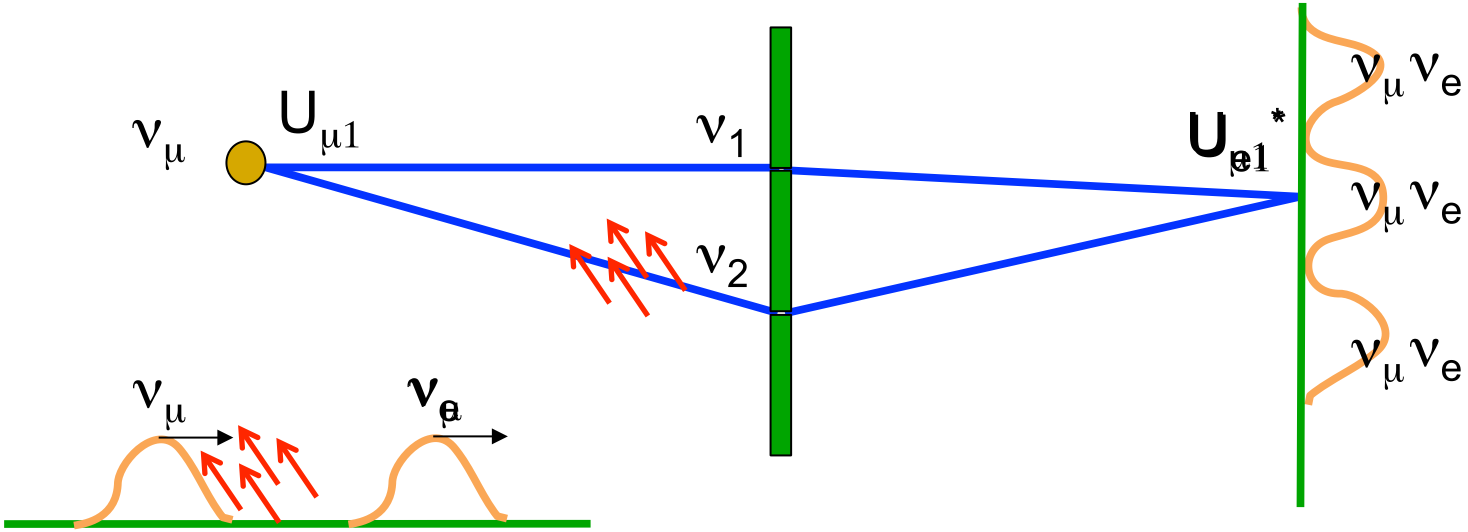

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If ν_1 and ν_2, have different coupling with Lorentz violating field, neutrinos also oscillate. The sensitivity of neutrino oscillation is comparable the target scale of Lorentz violation ($<10^{-19}$GeV).

If neutrino oscillation is caused by Lorentz violation, interference pattern (oscillation probability) may have sidereal time dependence.

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern test of Lorentz violation
4. Lorentz violating neutrino oscillation
5. Test for Lorentz violation with MiniBooNE data
6. Test for Lorentz violation with Double Chooz data
7. Double Chooz spectrum fit
8. Extra-terrestrial neutrinos
9. Conclusion

MiniBooNE collaboration,
PRD79(2009)072002
NIM.A599(2009)28

5. MiniBooNE experiment

MiniBooNE is a short-baseline neutrino oscillation experiment at Fermilab.

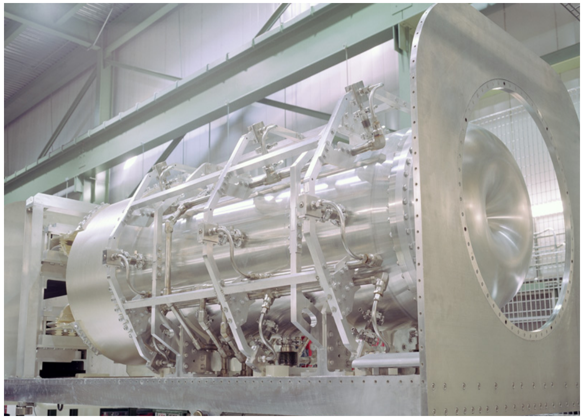
$$\nu_\mu \xrightarrow{oscillation} \nu_e + n \rightarrow e^- + p$$

$$\bar{\nu}_\mu \xrightarrow{oscillation} \bar{\nu}_e + p \rightarrow e^+ + n$$

Booster Neutrino Beamline (BNB) creates ~800(600)MeV neutrino(anti-neutrino) by pion decay-in-flight. Cherenkov radiation from the charged leptons are observed by MiniBooNE Cherenkov detector to reconstruct neutrino energy.

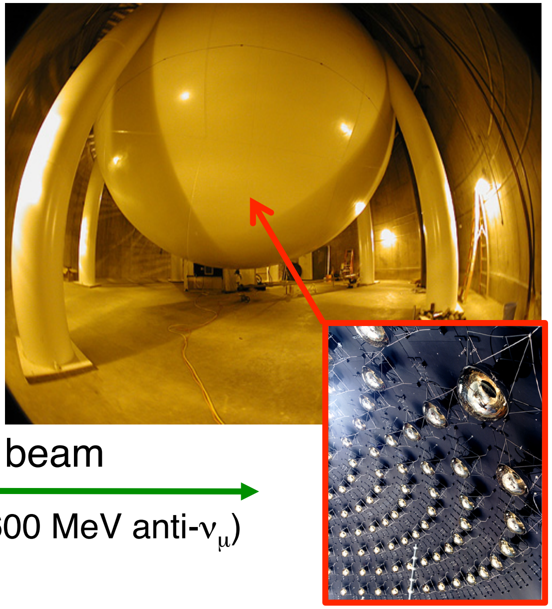
FNAL Booster

Magnetic focusing horn



~520m →

MiniBooNE detector



1280 of 8” PMT

primary beam → secondary beam → tertiary beam →

(8 GeV protons)

(1-2 GeV pions)

(800 MeV ν_μ , 600 MeV anti-ν_μ)

MiniBooNE collaboration,
PRL102(2009)101802,
PRL105(2010)181801

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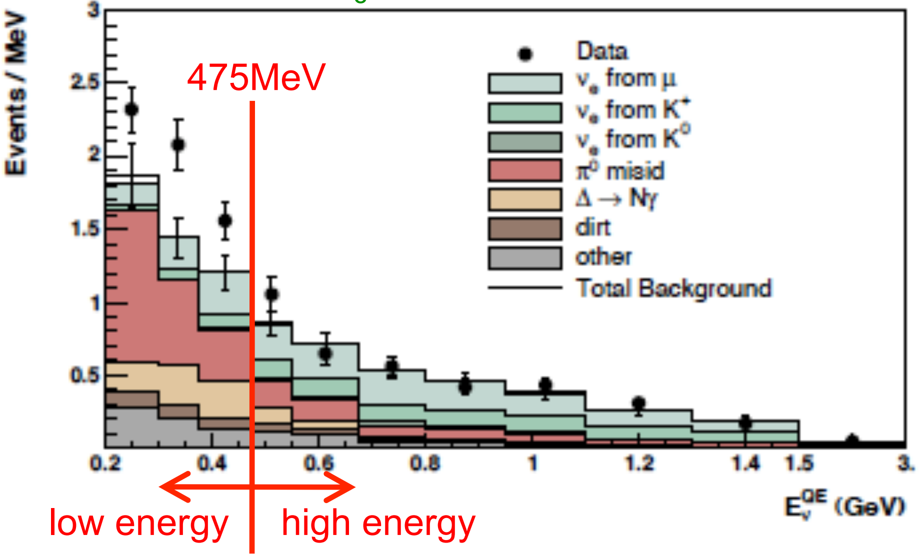
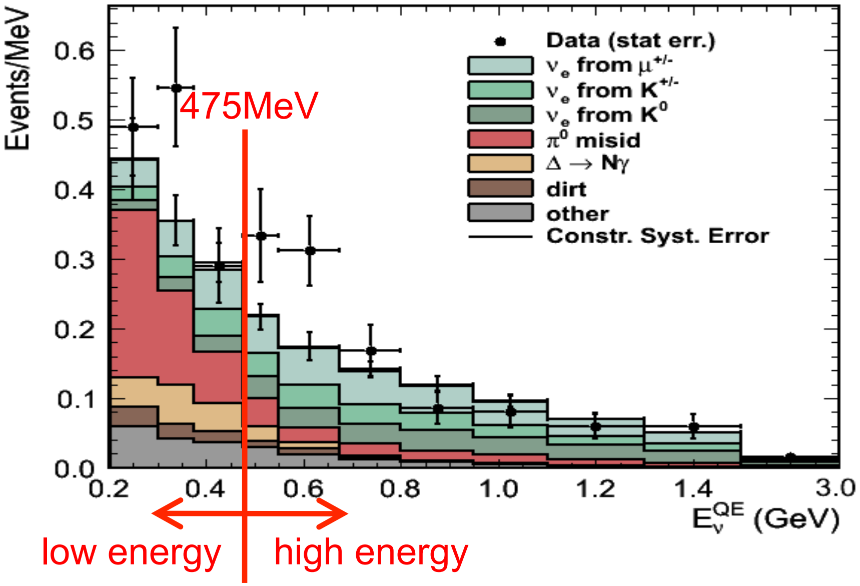
Neutrino mode analysis: MiniBooNE saw the 3.0σ excess at low energy region
Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at low and high energy region

MiniBooNE low E ν_e excess



MiniBooNE anti-ν_e excess



These excesses are not predicted by neutrino Standard Model (νSM), therefor it might sterile neutrino or other new physics, such as Lorentz violation
→ Oscillation candidate events may have sidereal time dependence!

MiniBooNE collaboration,
PLB718(2013)1303

5. Lorentz violation with MiniBooNE neutrino data

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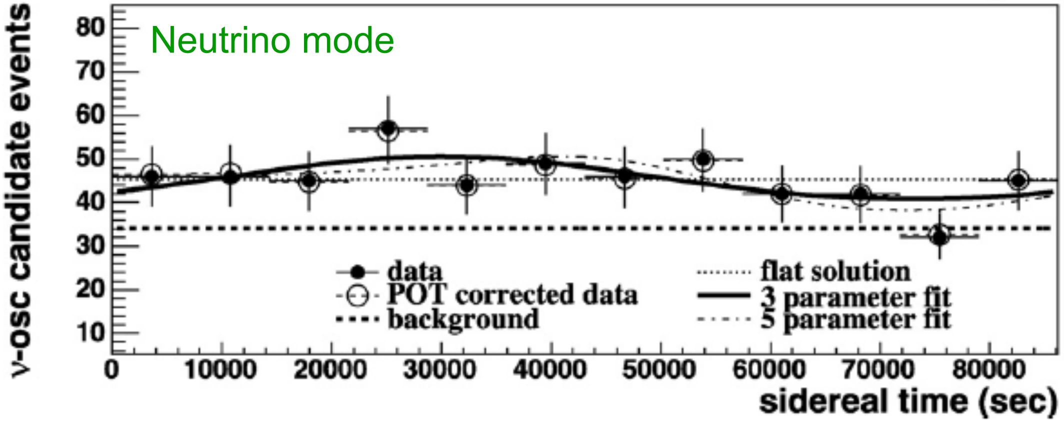
Electron neutrino candidate data prefer sidereal time independent solution (flat)



MiniBooNE collaboration,
PLB718(2013)1303

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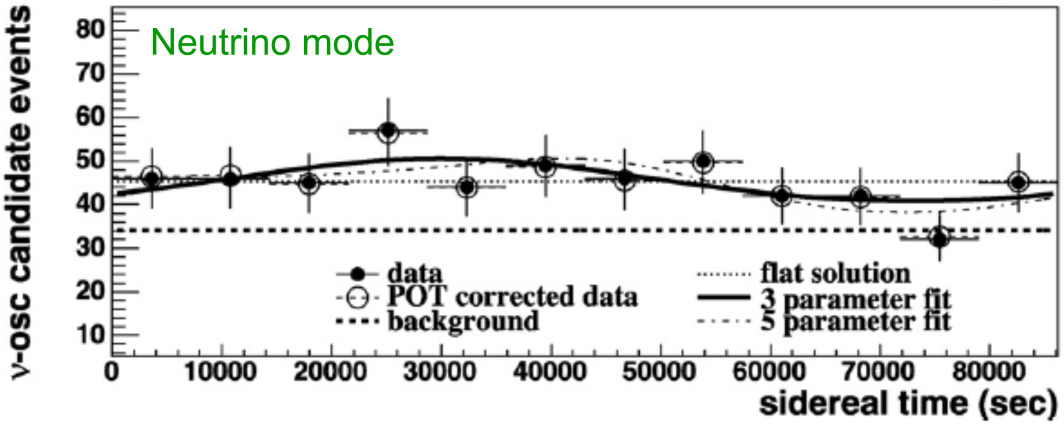
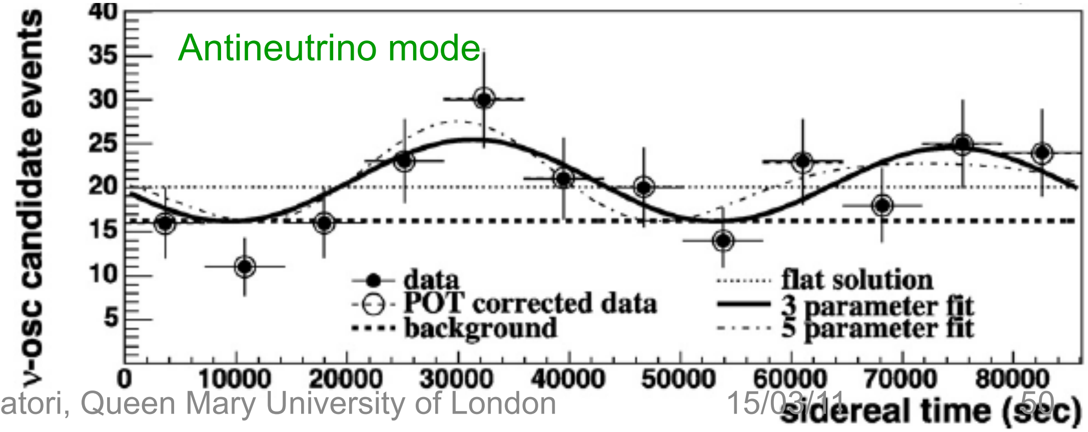


Electron antineutrino candidate data prefer sidereal time dependent solution, however statistical significance is marginal

We find no evidence of Lorentz violation



MiniBooNE collaboration,
PLB718(2013)1303

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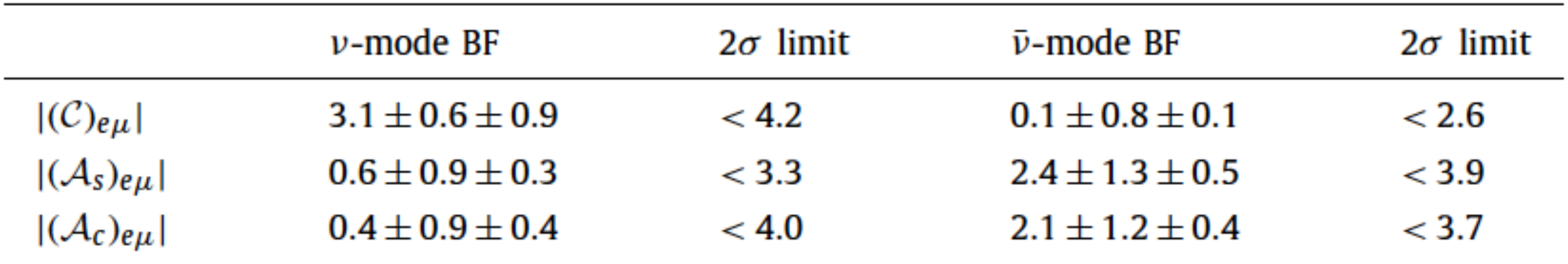
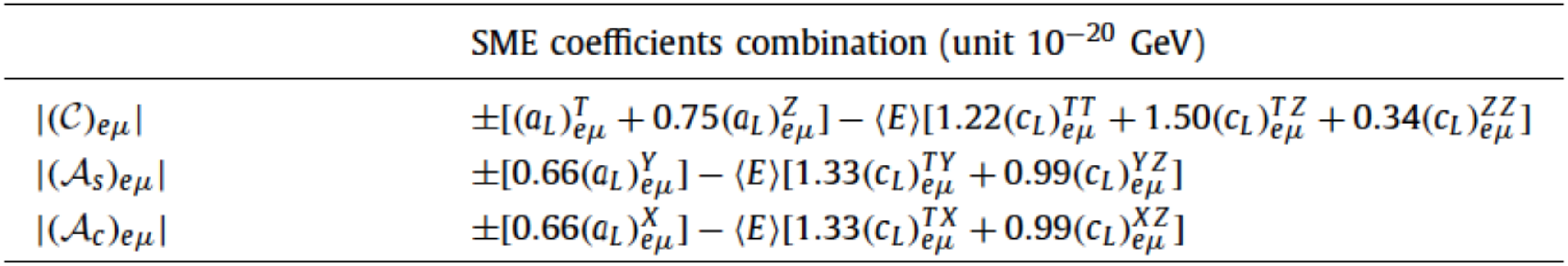
Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at low and high energy region

Since we find no evidence of Lorentz violation, we set limits on the combination SME coefficients.



	ν-mode BF	2σ limit	$\bar{\nu}$-mode BF	2σ limit
$\lvert(\mathcal{C})_{e\mu}\rvert$	$3.1 \pm 0.6 \pm 0.9$	< 4.2	$0.1 \pm 0.8 \pm 0.1$	< 2.6
$\lvert(\mathcal{A}_s)_{e\mu}\rvert$	$0.6 \pm 0.9 \pm 0.3$	< 3.3	$2.4 \pm 1.3 \pm 0.5$	< 3.9
$\lvert(\mathcal{A}_c)_{e\mu}\rvert$	$0.4 \pm 0.9 \pm 0.4$	< 4.0	$2.1 \pm 1.2 \pm 0.4$	< 3.7



	SME coefficients combination (unit 10^{-20} GeV)
$\lvert(\mathcal{C})_{e\mu}\rvert$	$\pm[(a_L)^T_{e\mu} + 0.75(a_L)^Z_{e\mu}] - \langle E\rangle[1.22(c_L)^{TT}_{e\mu} + 1.50(c_L)^{TZ}_{e\mu} + 0.34(c_L)^{ZZ}_{e\mu}]$
$\lvert(\mathcal{A}_s)_{e\mu}\rvert$	$\pm[0.66(a_L)^Y_{e\mu}] - \langle E\rangle[1.33(c_L)^{TY}_{e\mu} + 0.99(c_L)^{YZ}_{e\mu}]$
$\lvert(\mathcal{A}_c)_{e\mu}\rvert$	$\pm[0.66(a_L)^X_{e\mu}] - \langle E\rangle[1.33(c_L)^{TX}_{e\mu} + 0.99(c_L)^{XZ}_{e\mu}]$

LSND collaboration,
PRD72(2005)076004

5. Summary of results

LSND experiment

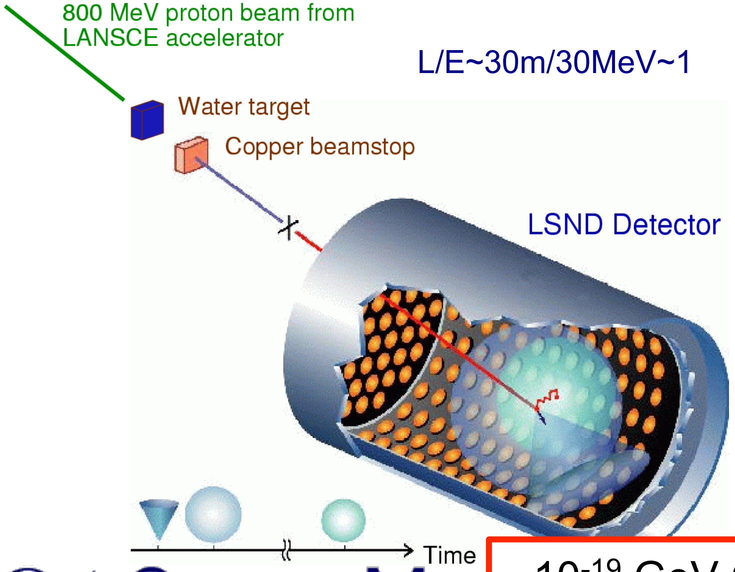
LSND is a short-baseline neutrino oscillation experiment at Los Alamos.

$$\bar{\nu}_\mu \xrightarrow{oscillation} \bar{\nu}_e + p \to e^+ + n$$

$$n + p \to d + \gamma$$

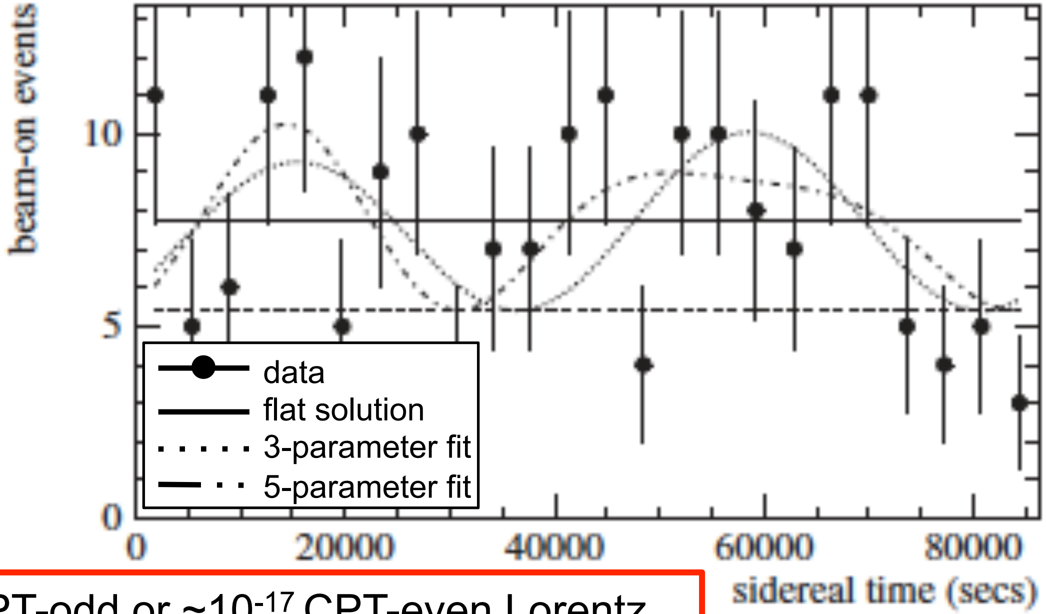
LSND saw the 3.8σ excess of electron antineutrinos from muon antineutrino beam; since this excess is not understood by neutrino Standard Model, it might be new physics

Data is consistent with flat solution, but sidereal time solution is not excluded.



L/E~30m/30MeV~1

LSND oscillation candidate sidereal time distribution



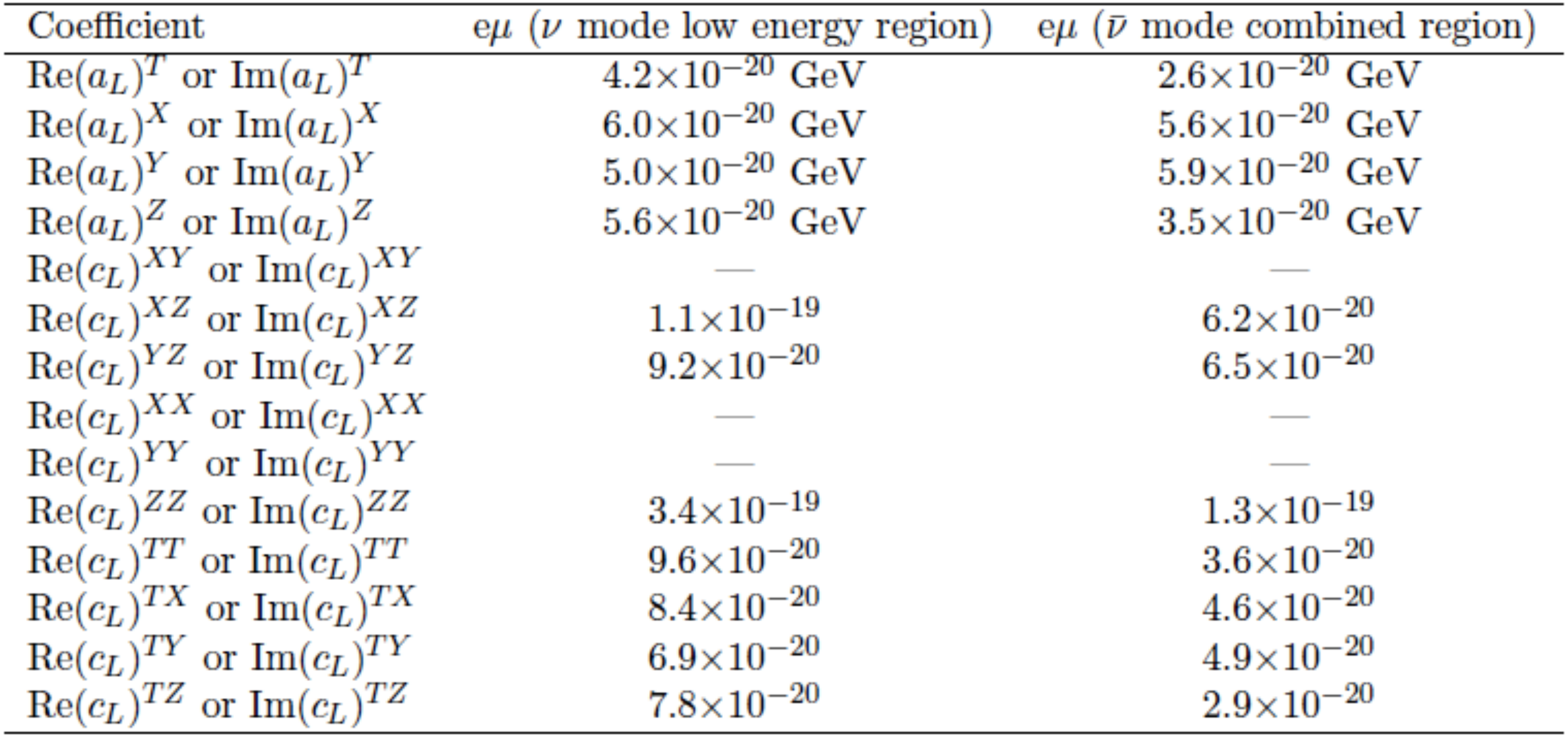
~10^{-19} GeV CPT-odd or ~10^{-17} CPT-even Lorentz violation could be the solution of LSND excess

TK,
MPLA27(2012)1230024

5. Summary of results

Since we find no evidence of Lorentz violation from MiniBooNE analysis, we set limits on the SME coefficients.

These limits exclude SME values to explain LSND data, therefore there is no simple Lorentz violation motivated scenario to accommodate LSND and MiniBooNE results simultaneously



Coefficient	$e\mu$ (ν mode low energy region)	$e\mu$ ($\bar{\nu}$ mode combined region)
$\mathrm{Re}(a_L)^T$ or $\mathrm{Im}(a_L)^T$	4.2×10^{-20} GeV	2.6×10^{-20} GeV
$\mathrm{Re}(a_L)^X$ or $\mathrm{Im}(a_L)^X$	6.0×10^{-20} GeV	5.6×10^{-20} GeV
$\mathrm{Re}(a_L)^Y$ or $\mathrm{Im}(a_L)^Y$	5.0×10^{-20} GeV	5.9×10^{-20} GeV
$\mathrm{Re}(a_L)^Z$ or $\mathrm{Im}(a_L)^Z$	5.6×10^{-20} GeV	3.5×10^{-20} GeV
$\mathrm{Re}(c_L)^{XY}$ or $\mathrm{Im}(c_L)^{XY}$	—	—
$\mathrm{Re}(c_L)^{XZ}$ or $\mathrm{Im}(c_L)^{XZ}$	1.1×10^{-19}	6.2×10^{-20}
$\mathrm{Re}(c_L)^{YZ}$ or $\mathrm{Im}(c_L)^{YZ}$	9.2×10^{-20}	6.5×10^{-20}
$\mathrm{Re}(c_L)^{XX}$ or $\mathrm{Im}(c_L)^{XX}$	—	—
$\mathrm{Re}(c_L)^{YY}$ or $\mathrm{Im}(c_L)^{YY}$	—	—
$\mathrm{Re}(c_L)^{ZZ}$ or $\mathrm{Im}(c_L)^{ZZ}$	3.4×10^{-19}	1.3×10^{-19}
$\mathrm{Re}(c_L)^{TT}$ or $\mathrm{Im}(c_L)^{TT}$	9.6×10^{-20}	3.6×10^{-20}
$\mathrm{Re}(c_L)^{TX}$ or $\mathrm{Im}(c_L)^{TX}$	8.4×10^{-20}	4.6×10^{-20}
$\mathrm{Re}(c_L)^{TY}$ or $\mathrm{Im}(c_L)^{TY}$	6.9×10^{-20}	4.9×10^{-20}
$\mathrm{Re}(c_L)^{TZ}$ or $\mathrm{Im}(c_L)^{TZ}$	7.8×10^{-20}	2.9×10^{-20}

1. Spontaneous Lorentz symmetry breaking
2. What is Lorentz and CPT violation?
3. Modern test of Lorentz violation
4. Lorentz violating neutrino oscillation
5. Test for Lorentz violation with MiniBooNE data
6. **Test for Lorentz violation with Double Chooz data**
7. Double Chooz spectrum fit
8. Extra-terrestrial neutrinos
9. Conclusion

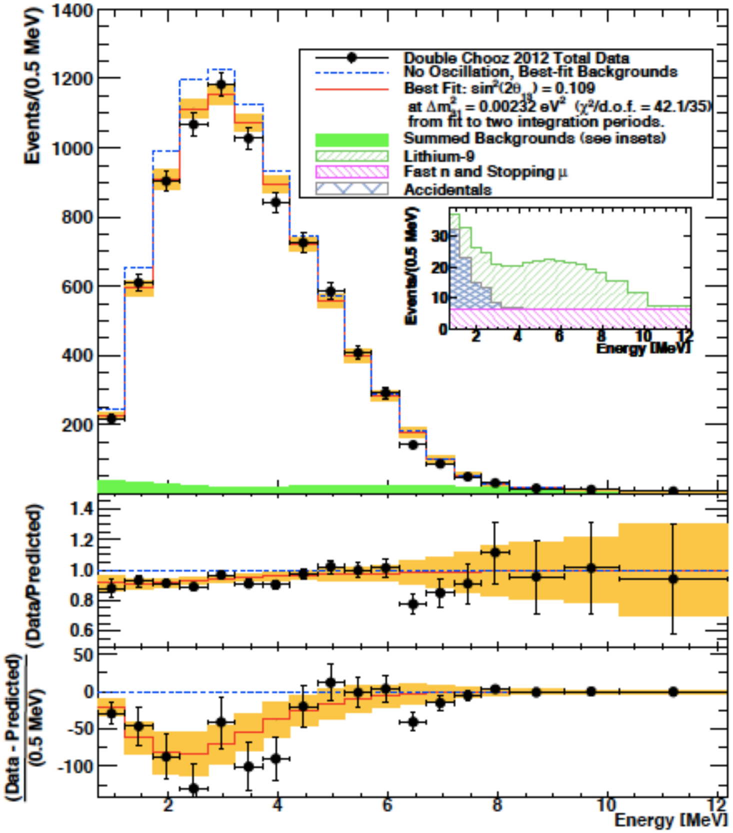
Double Chooz collaboration, PRL108(2012)131801
DayaBay collaboration, PRL108(2012)171803
RENO collaboration, PRL108(2012)191802

6. Double Chooz experiment

Reactor electron antineutrino disappearance

- Double Chooz, DayaBay and RENO experiments observed disappearance signals

Double Chooz reactor neutrino candidate



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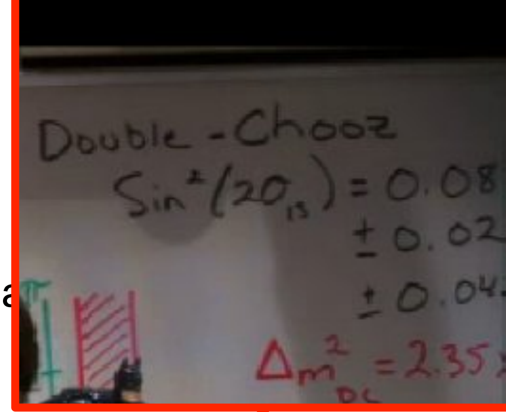
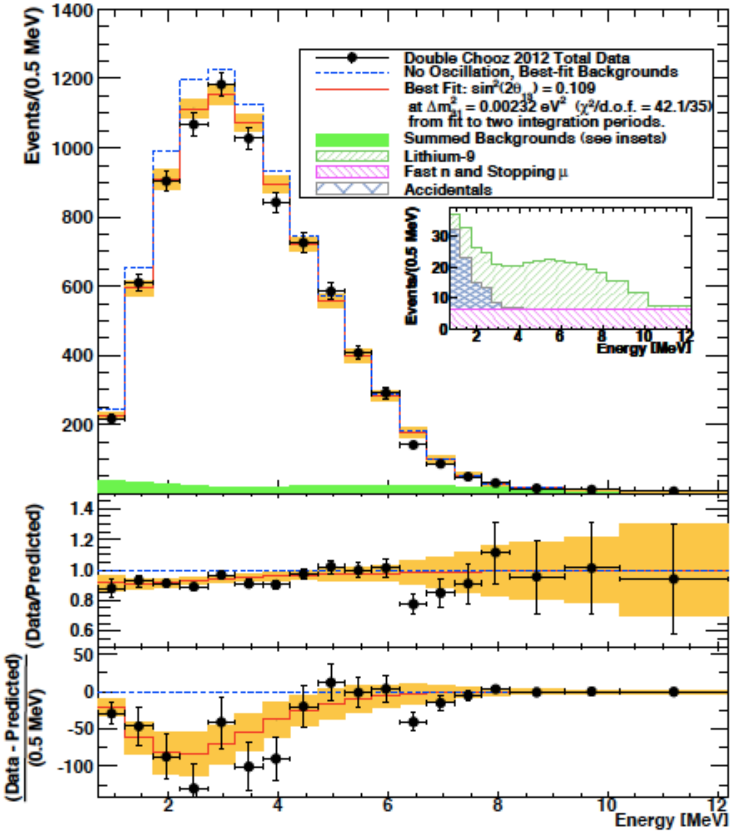
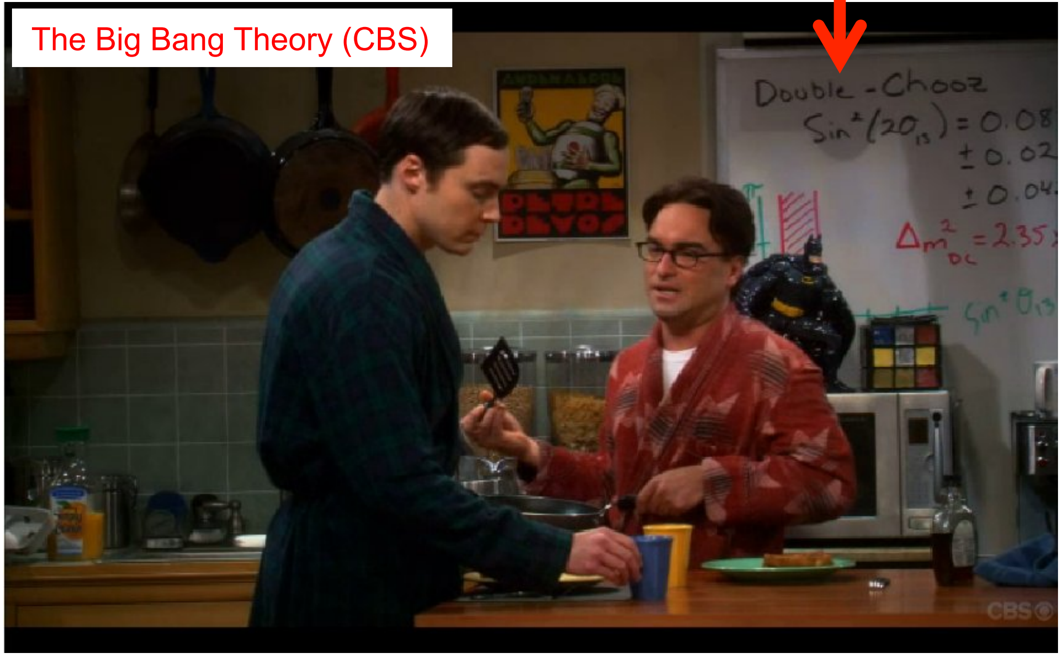


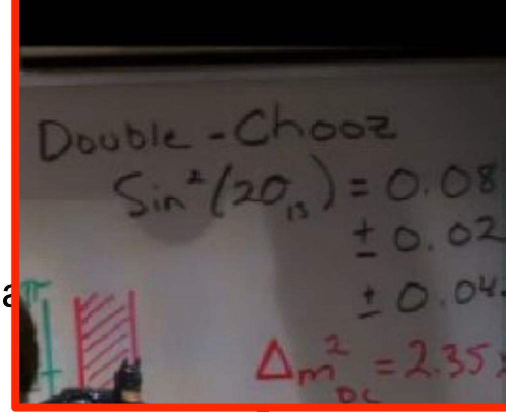
Double Chooz reactor neutrino candidate





The Big Bang Theory (CBS)

6. Double Chooz experiment

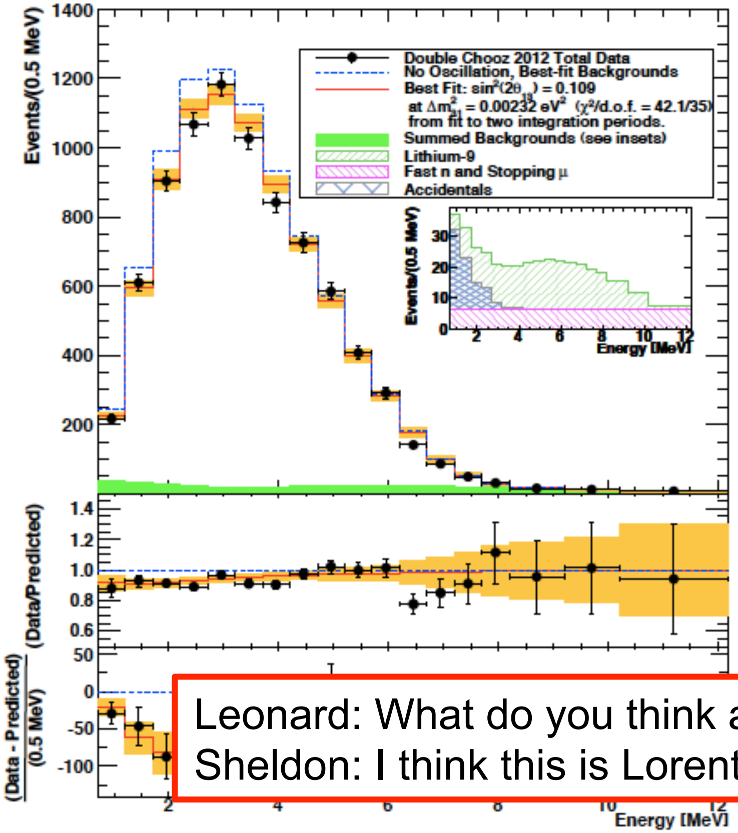


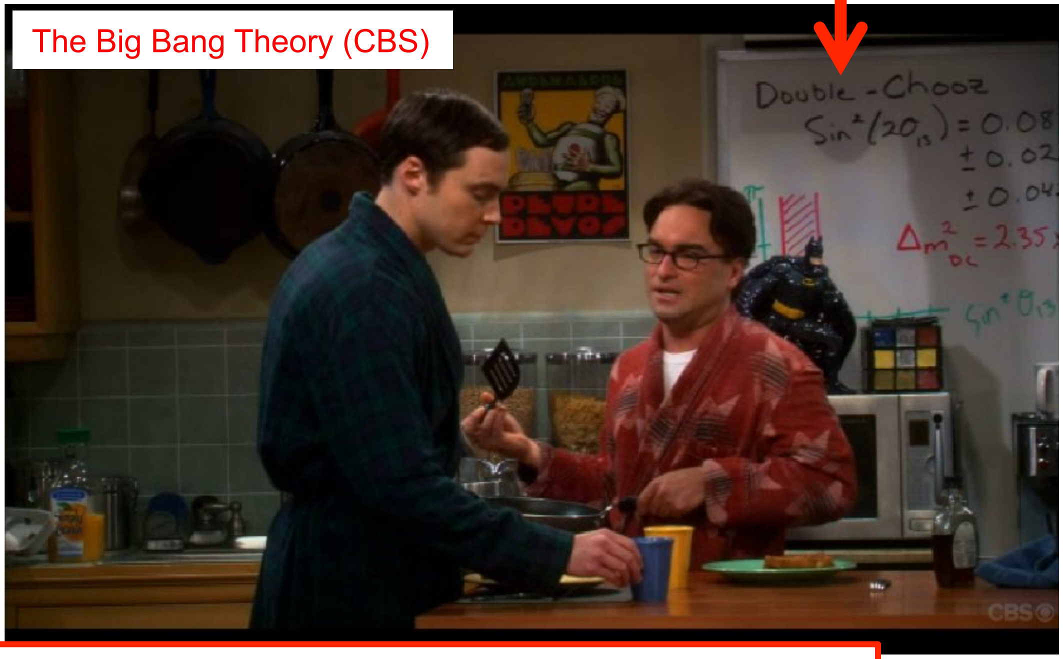
Reactor electron antineutrino disappearance

- Double Chooz, DayaBay and RENO experiments observed disappea

This small disappearance may have sidereal time dependence?

Double Chooz reactor neutrino candidate





The Big Bang Theory (CBS)

Leonard: What do you think about the latest Double Chooz result?
Sheldon: I think this is Lorentz violation..., check sidereal time dependence

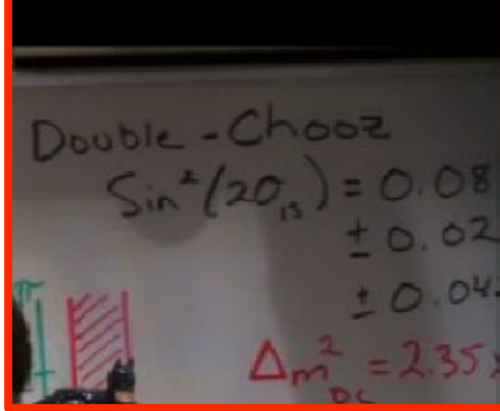
6. Double Chooz experiment

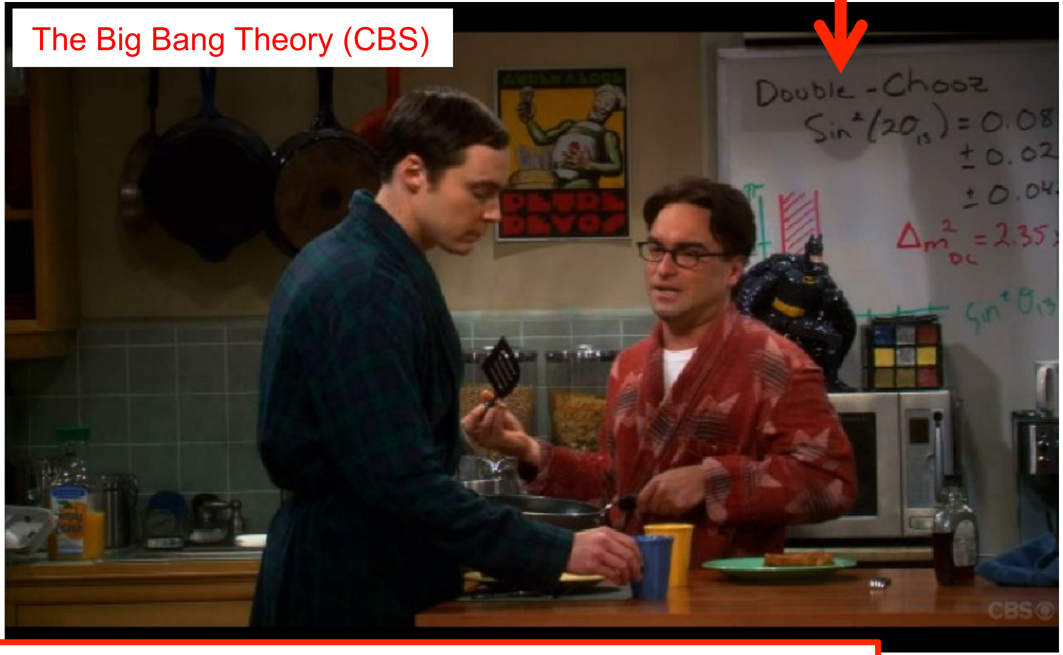
So far, we have set limits on
1. $\nu_e \leftrightarrow \nu_\mu$ channel: LSND, MiniBooNE, MINOS ($<10^{-20}$ GeV)
2. $\nu_\mu \leftrightarrow \nu_\tau$ channel: MINOS, IceCube ($<10^{-23}$ GeV)

The last untested channel is $\nu_e \leftrightarrow \nu_\tau$

It is possible to limit $\nu_e \leftrightarrow \nu_\tau$ channel from reactor ν_e disappearance experiment

$$P(\nu_e \leftrightarrow \nu_e) = 1 - P(\nu_e \leftrightarrow \nu_\mu) - P(\nu_e \leftrightarrow \nu_\tau) \sim 1 - P(\nu_e \leftrightarrow \nu_\tau)$$




The Big Bang Theory (CBS)

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Double Chooz collaboration,
PRD86(2012)112009

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So far, we have set limits on

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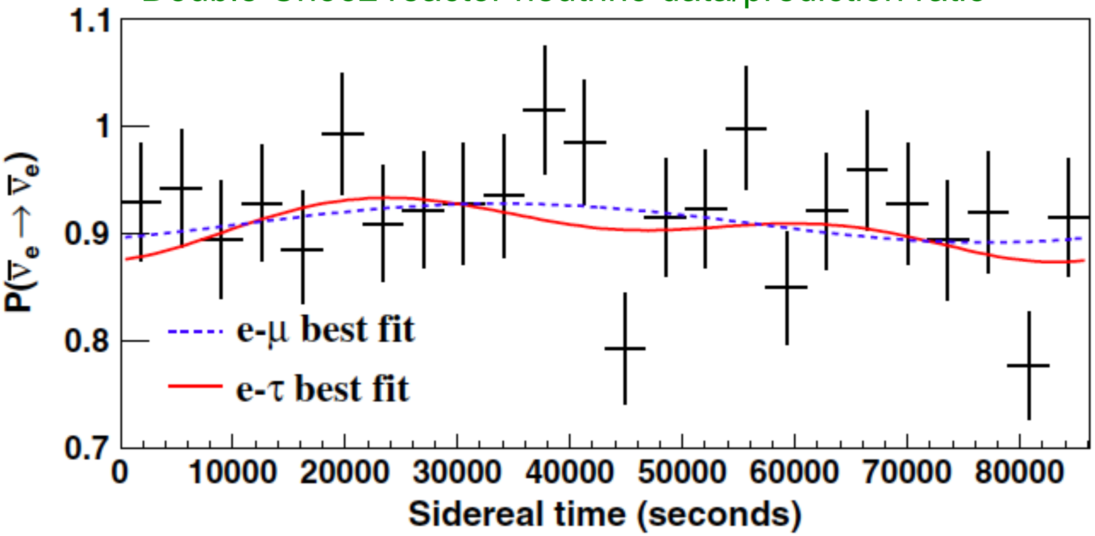
Small disappearance signal prefers sidereal time independent solution (flat)

We set limits in the e-τ sector for the first time; $\nu_e \leftrightarrow \nu_\tau$ ($<10^{-20}$ GeV)

Double Chooz reactor neutrino data/prediction ratio



6. Double Chooz experiment

Kostelecký and Russel
Rev.Mod.Phys.83(2011)11
ArXiv:0801.0287v6

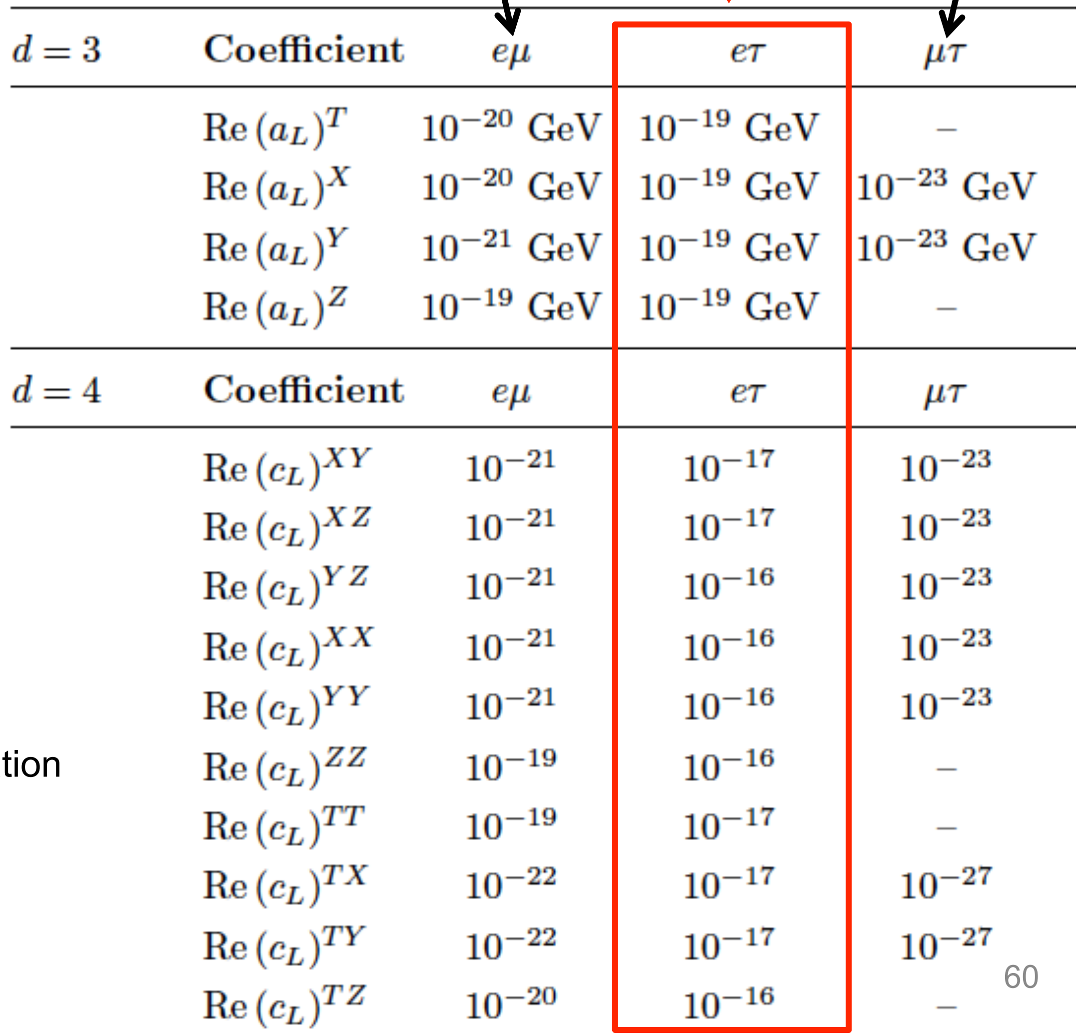
By this work, Lorentz violation is tested with all neutrino channels

Chance to see the Lorentz violation in terrestrial neutrino experiments will be very small

MiniBooNE
MINOS ND

Double Chooz

IceCube
MINOS FD



$d=3$	Coefficient	$e\mu$	$e\tau$	$\mu\tau$
	$\mathrm{Re}\,(a_L)^T$	10^{-20} GeV	10^{-19} GeV	–
	$\mathrm{Re}\,(a_L)^X$	10^{-20} GeV	10^{-19} GeV	10^{-23} GeV
	$\mathrm{Re}\,(a_L)^Y$	10^{-21} GeV	10^{-19} GeV	10^{-23} GeV
	$\mathrm{Re}\,(a_L)^Z$	10^{-19} GeV	10^{-19} GeV	–

$d=4$	Coefficient	$e\mu$	$e\tau$	$\mu\tau$
	$\mathrm{Re}\,(c_L)^{XY}$	10^{-21}	10^{-17}	10^{-23}
	$\mathrm{Re}\,(c_L)^{XZ}$	10^{-21}	10^{-17}	10^{-23}
	$\mathrm{Re}\,(c_L)^{YZ}$	10^{-21}	10^{-16}	10^{-23}
	$\mathrm{Re}\,(c_L)^{XX}$	10^{-21}	10^{-16}	10^{-23}
	$\mathrm{Re}\,(c_L)^{YY}$	10^{-21}	10^{-16}	10^{-23}
	$\mathrm{Re}\,(c_L)^{ZZ}$	10^{-19}	10^{-16}	–
	$\mathrm{Re}\,(c_L)^{TT}$	10^{-19}	10^{-17}	–
	$\mathrm{Re}\,(c_L)^{TX}$	10^{-22}	10^{-17}	10^{-27}
	$\mathrm{Re}\,(c_L)^{TY}$	10^{-22}	10^{-17}	10^{-27}
	$\mathrm{Re}\,(c_L)^{TZ}$	10^{-20}	10^{-16}	–

Recently, Super-Kamiokande collaboration published significantly better limits arXiv:1410.4267

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8. Extra-terrestrial neutrinos
9. Conclusion

Díaz, Kostelecký, Mewes
PRD80(2009)076007

7. Massive Lorentz-violating model

Double Chooz oscillation signal has no sidereal time dependence.

By assuming main source of neutrino oscillation is neutrino mass, we can study perturbation terms to find secondary effect to cause oscillations.

massive neutrino oscillation

Lorentz violating neutrino oscillation

$$P(\bar{\nu}_e \to \bar{\nu}_e) = P^0(\bar{\nu}_e \to \bar{\nu}_e) + P^1(\bar{\nu}_e \to \bar{\nu}_e) + P^2(\bar{\nu}_e \to \bar{\nu}_e) + \cdots$$

In this way, we can access to different types of Lorentz violation

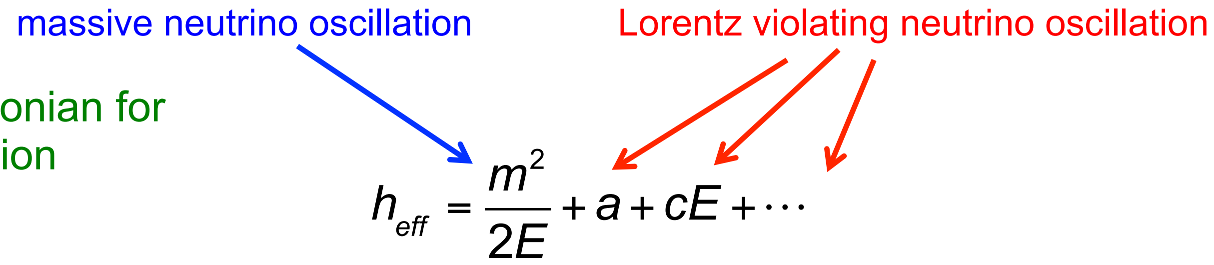
Díaz, Kostelecký, Mewes
PRD80(2009)076007

7. Anomalous energy spectrum

Sidereal variation is one of many predicted phenomena of Lorentz violating neutrino oscillations.

Lorentz violation predicts unexpected energy dependence of neutrino oscillations from standard neutrino mass oscillations.

Effective Hamiltonian for neutrino oscillation



massive neutrino oscillation

Lorentz violating neutrino oscillation

$$h_{eff} = \frac{m^2}{2E} + a + cE + \cdots$$

This is very useful to differentiate 2 effects:
- massive neutrino oscillation
- sidereal time independent Lorentz violating neutrino oscillation

Double Chooz released its energy spectrum (with full error matrix). We use this to test time independent Lorentz violating neutrino oscillation.

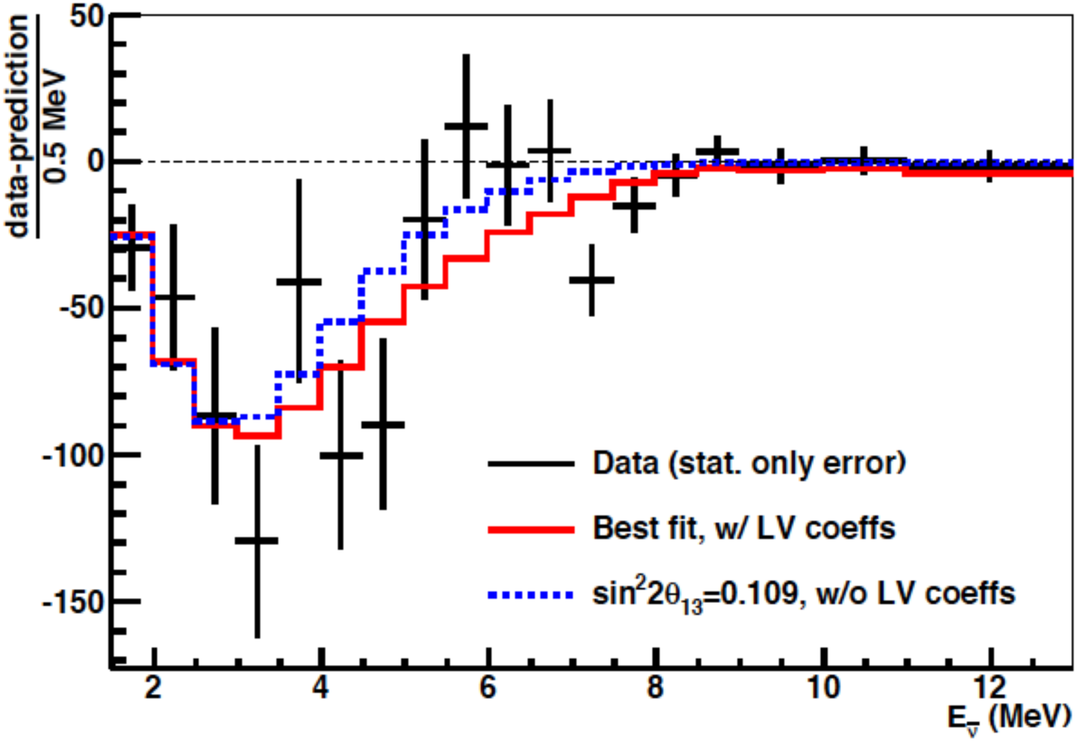
Díaz, TK, Spitz, Conrad
PLB727(2013)412

7. Double Chooz spectrum fit

Neutrino-Antineutrino oscillation

- Most of neutrino-neutrino oscillation channels are constraint from past analyses
- Here, we focus to test neutrino-antineutrino oscillation

ex) anti-ν_e→ν_e oscillation fit with Double Chooz data



These fits provide first limits on neutrino-antineutrino time independent Lorentz violating coefficients

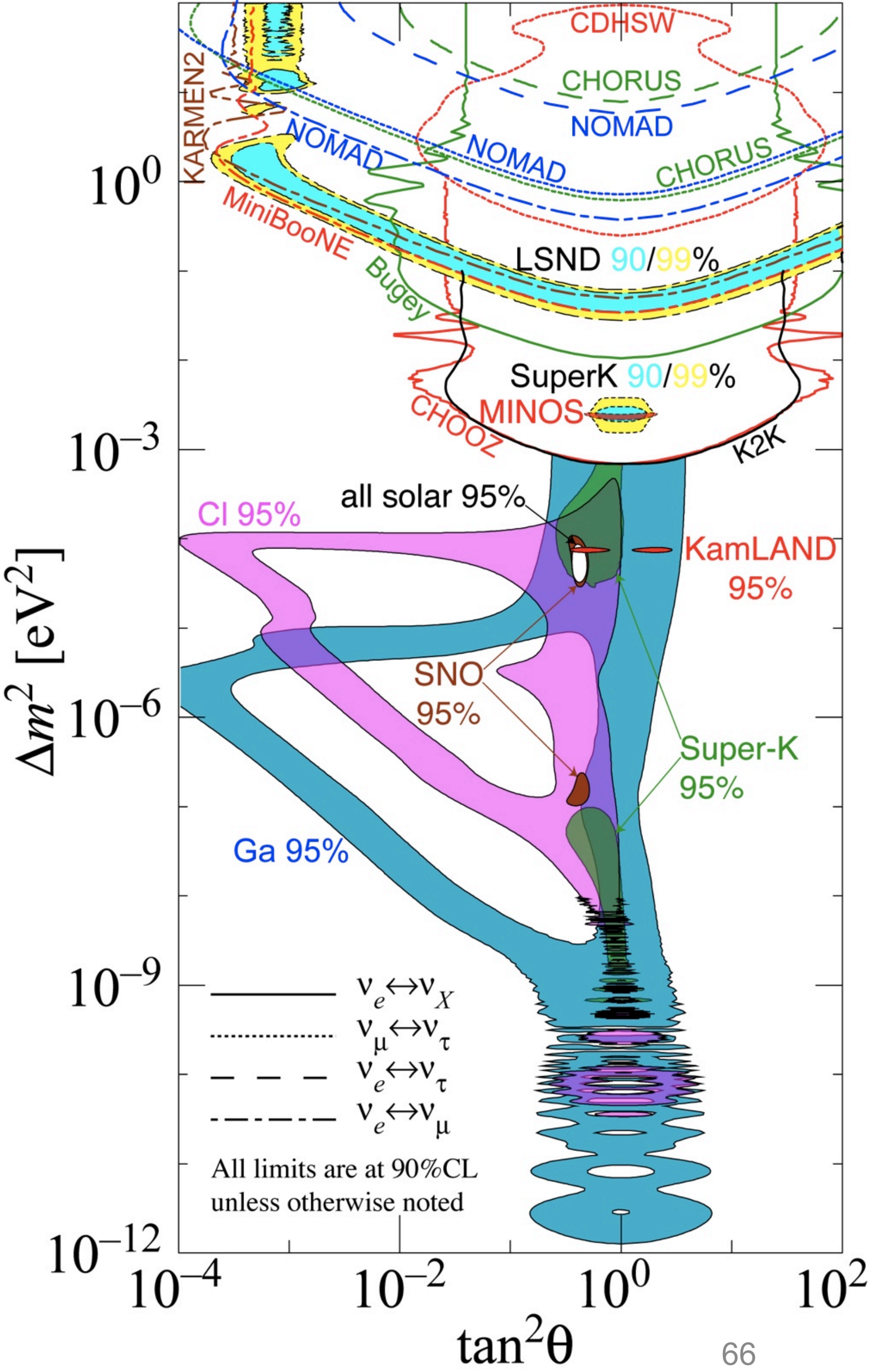
8. Neutrino standard Model (νSM)

This is the world data of neutrino oscillation

It looks majority of region is either accepted (positive signals) or excluded

But this is model dependent diagram, because it assumes neutrino mass as phase, and mass mixing matrix elements as amplitude of neutrino oscillations

What is model independent diagram look like?

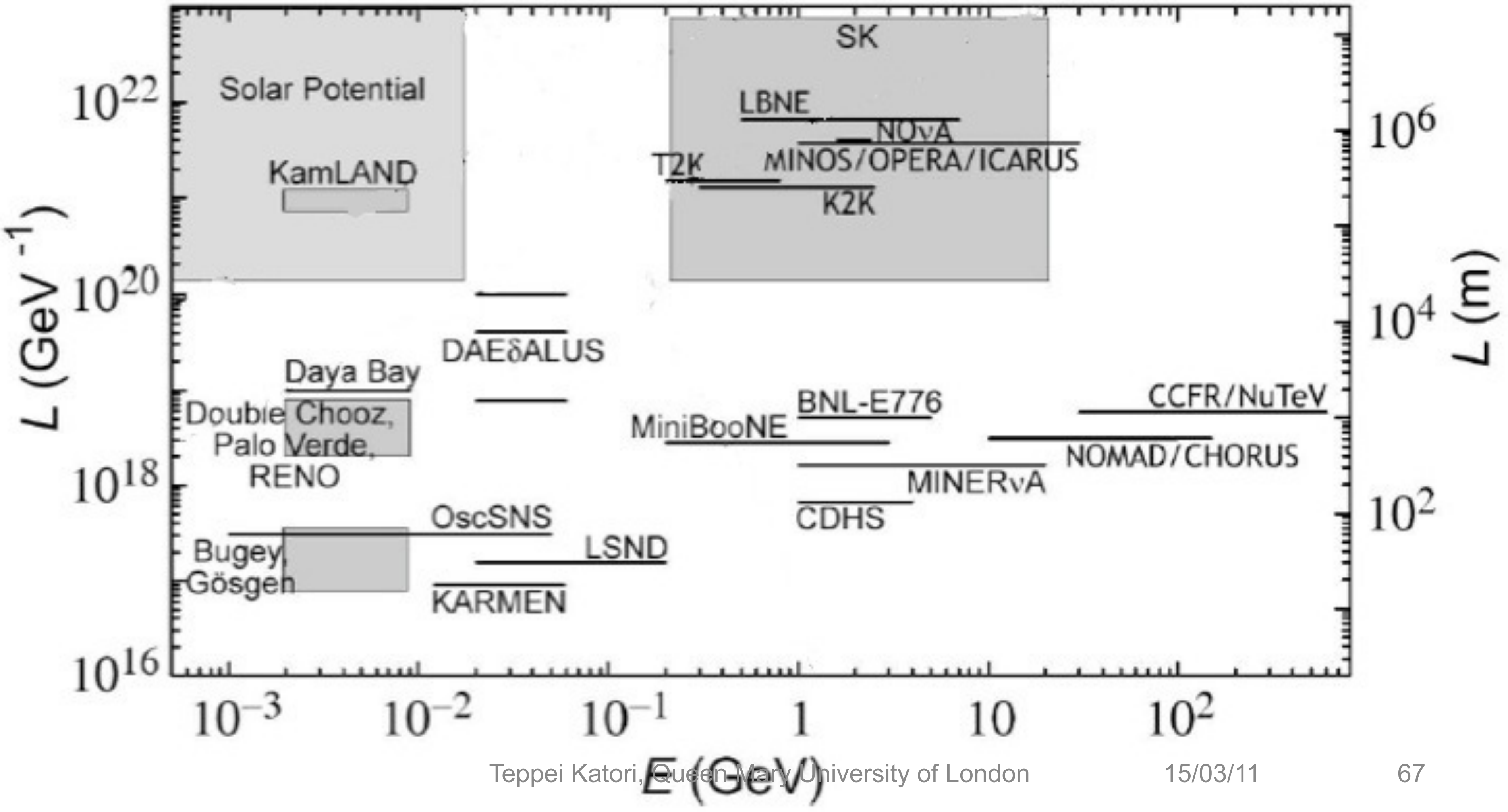


http://hitoshi.berkeley.edu/neutrino

Kostelecký and Mewes
PRD69(2004)016005

8. Lorentz violation with neutrino oscillation

Model independent neutrino oscillation data is the function of neutrino energy and baseline.



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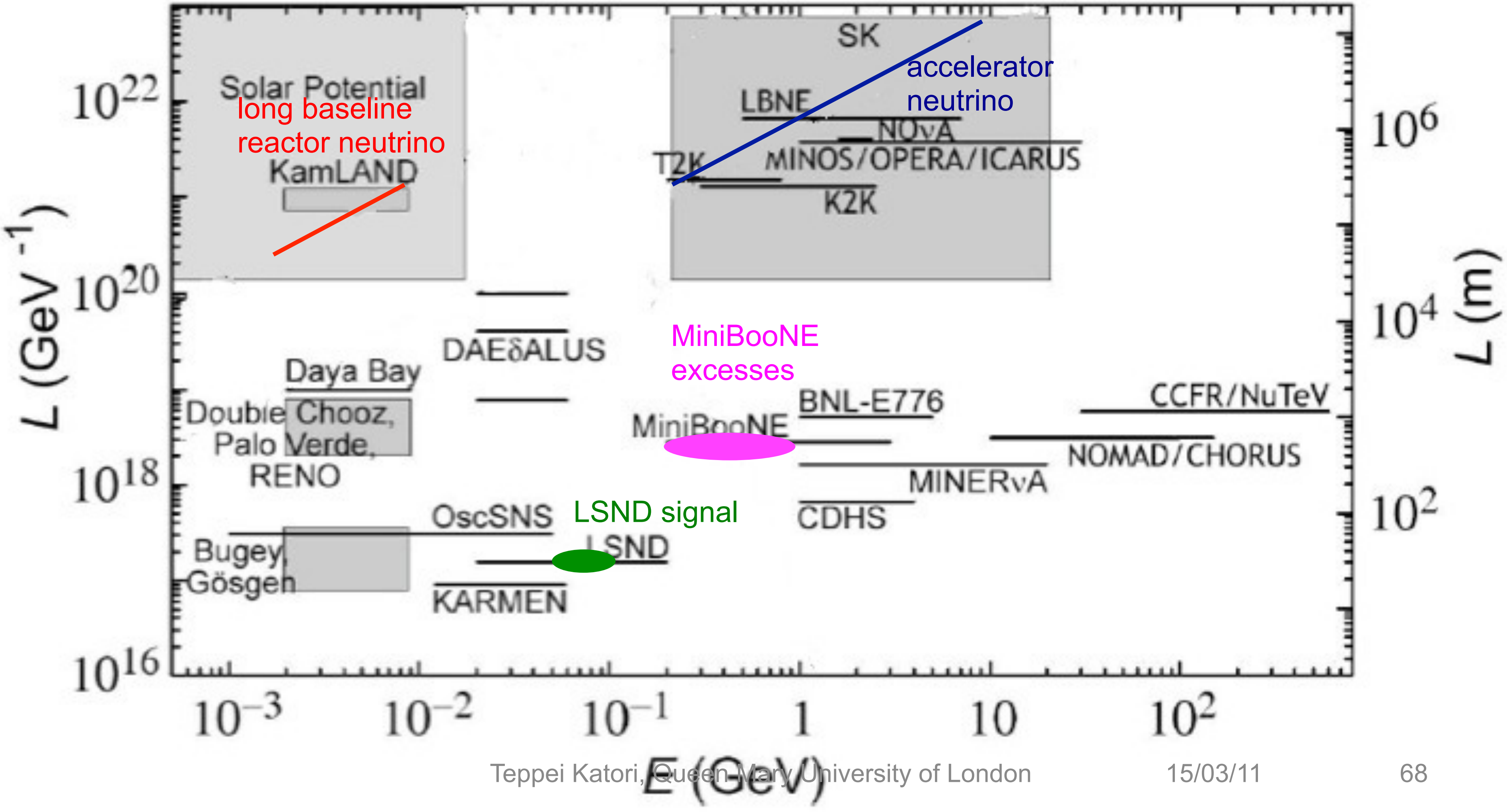

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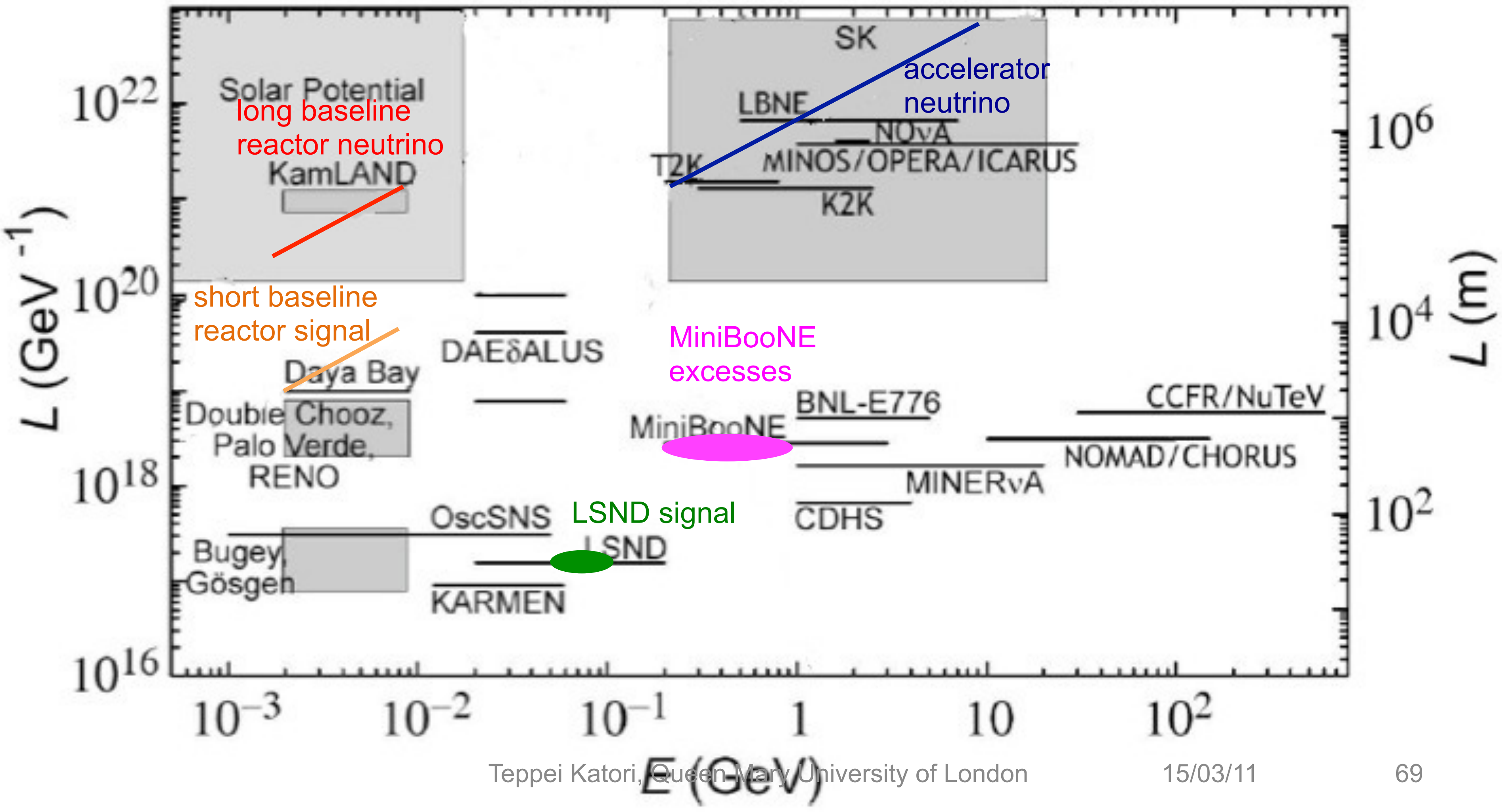

Kostelecký and Mewes
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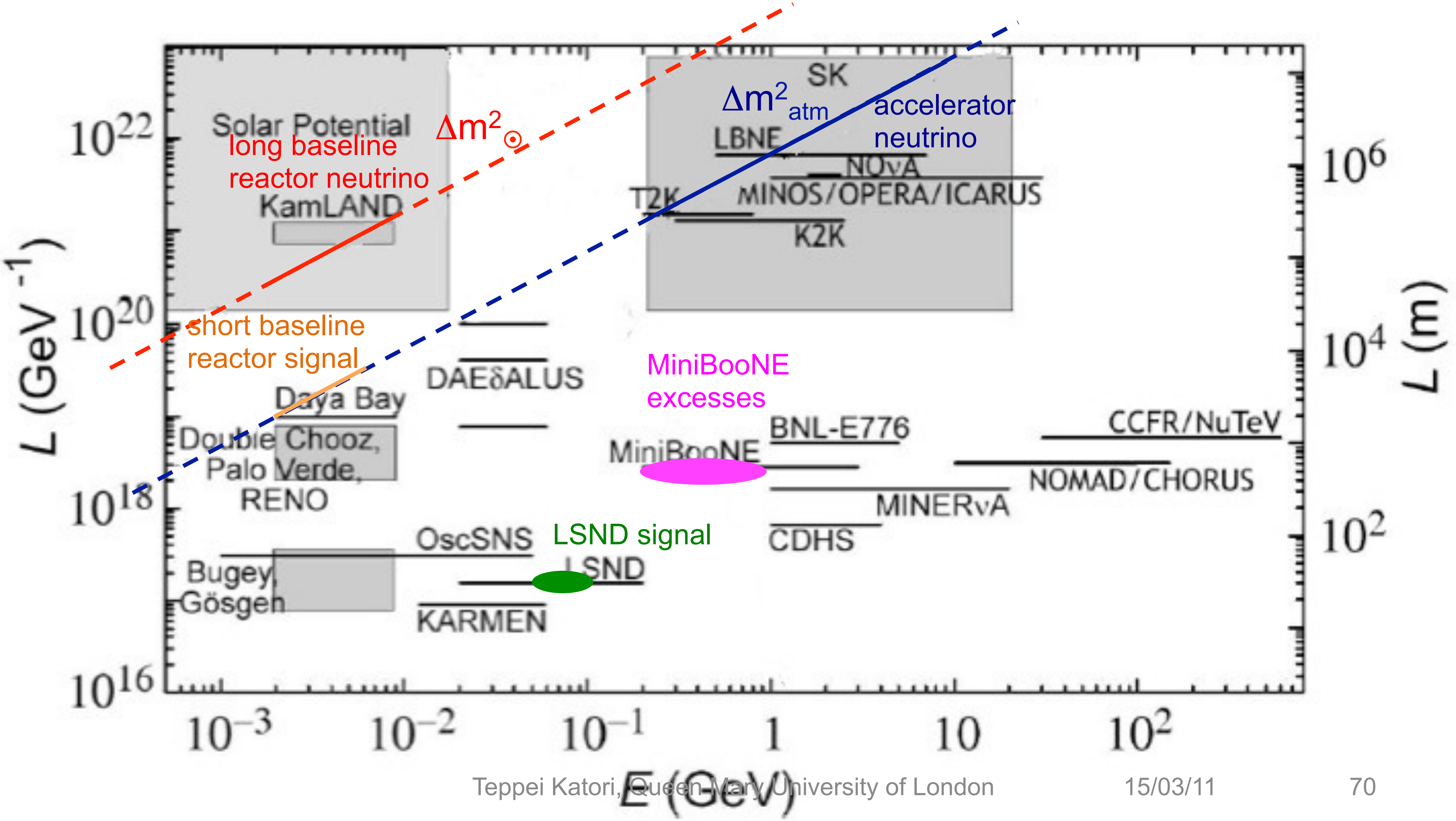

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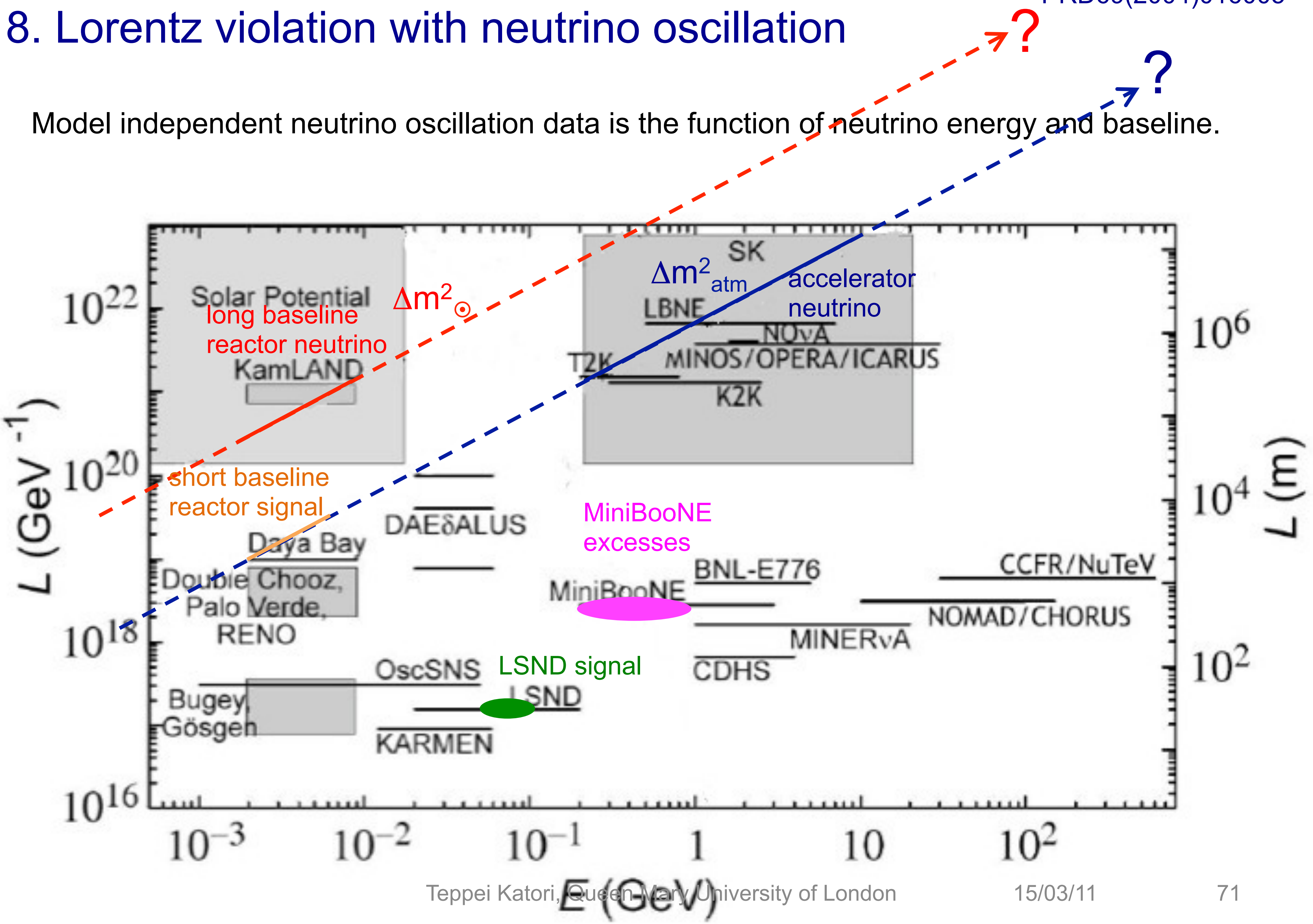
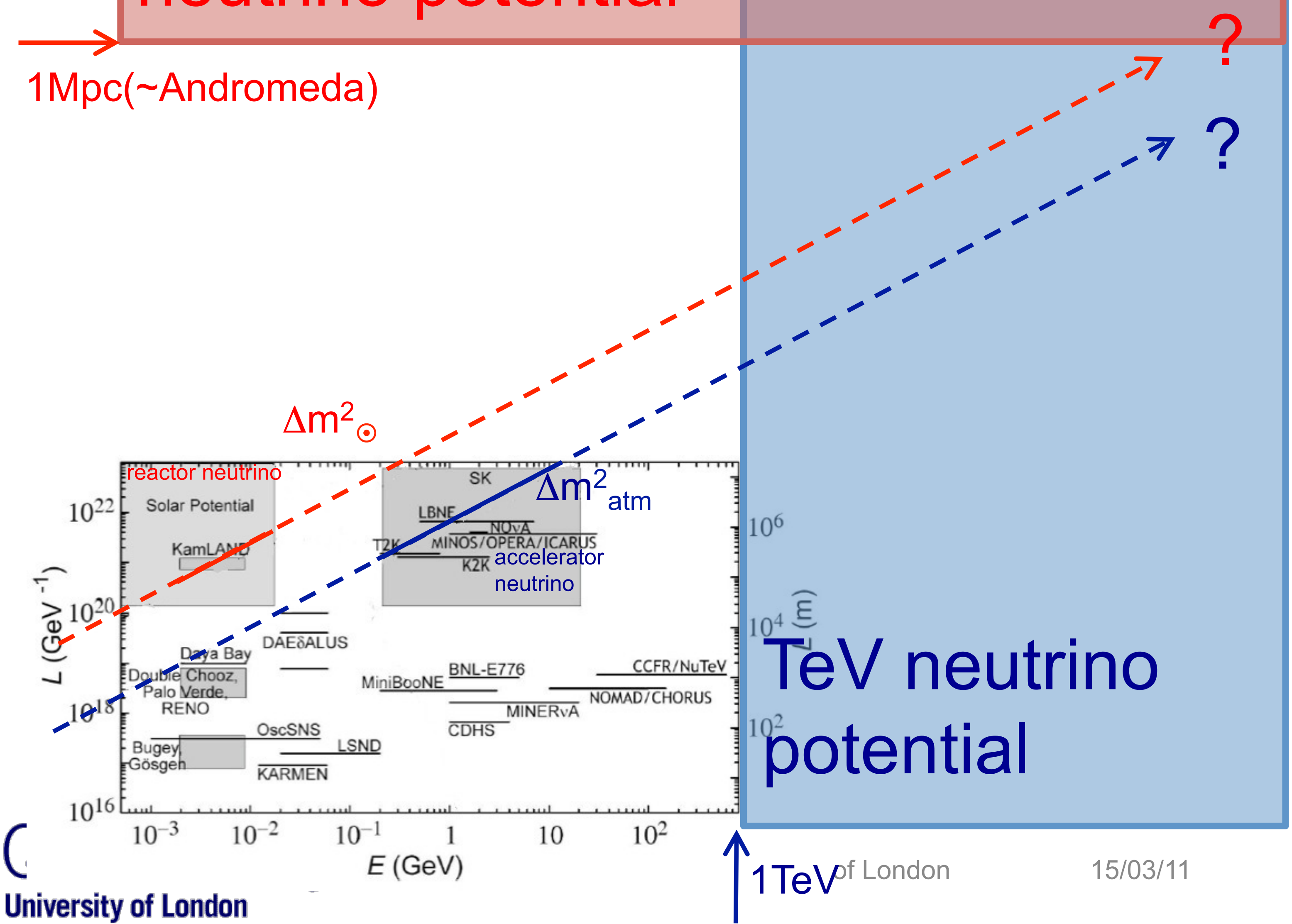


Kostelecký and Mewes
PRD69(2004)016005

8. Lorentz violation with neutrino oscillation

extra galactic
neutrino potential

1Mpc(~Andromeda)



TeV neutrino
potential

Kostelecký and Mewes
PRD69(2004)016005

8. Lorentz violation with neutrino oscillation

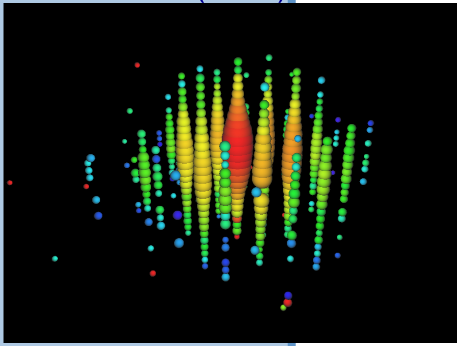
extra galactic
neutrino potential

1Mpc(~Andromeda)

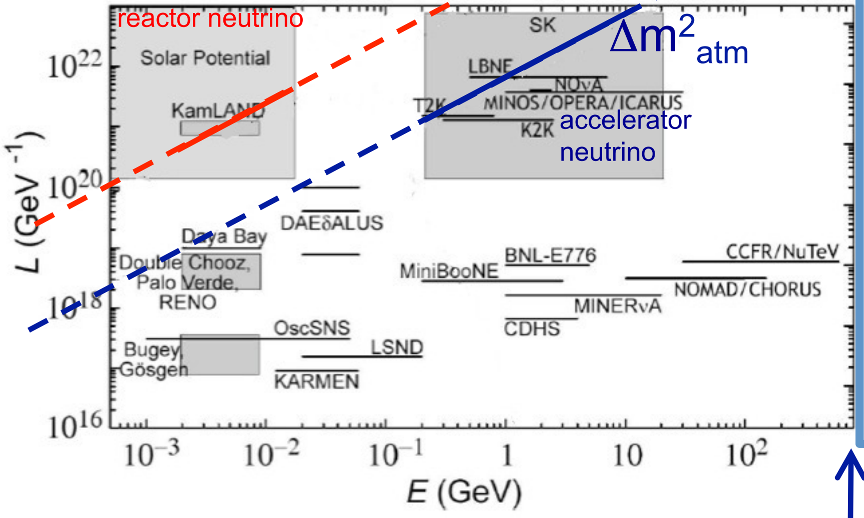
?

?

IceCube collaboration
PRL111(2013)021103



$\Delta m^2_{\odot}$



Δm^2_{atm}

TeV neutrino
potential

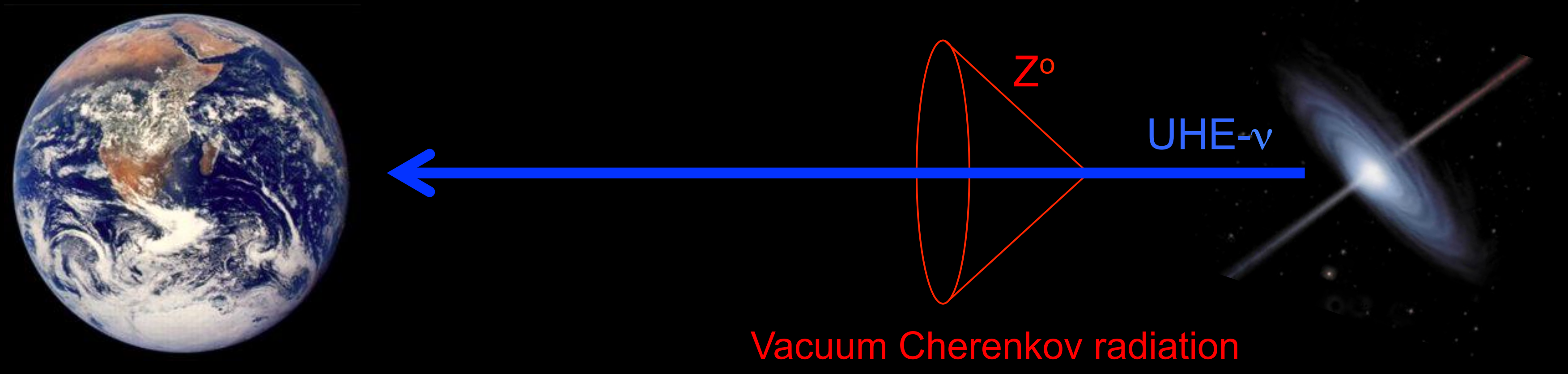
1TeV

Diaz, Kostelecký, Mewes
PRD85(2013)096005;89(2014)043005

8. Lorentz violation with extra-terrestrial neutrinos

Combination of longer baseline and higher energy makes extra-terrestrial neutrino to be the most sensitive source of fundamental physics.

Vacuum Cherenkov radiation can limit new physics of neutrino up to 10^{-20}



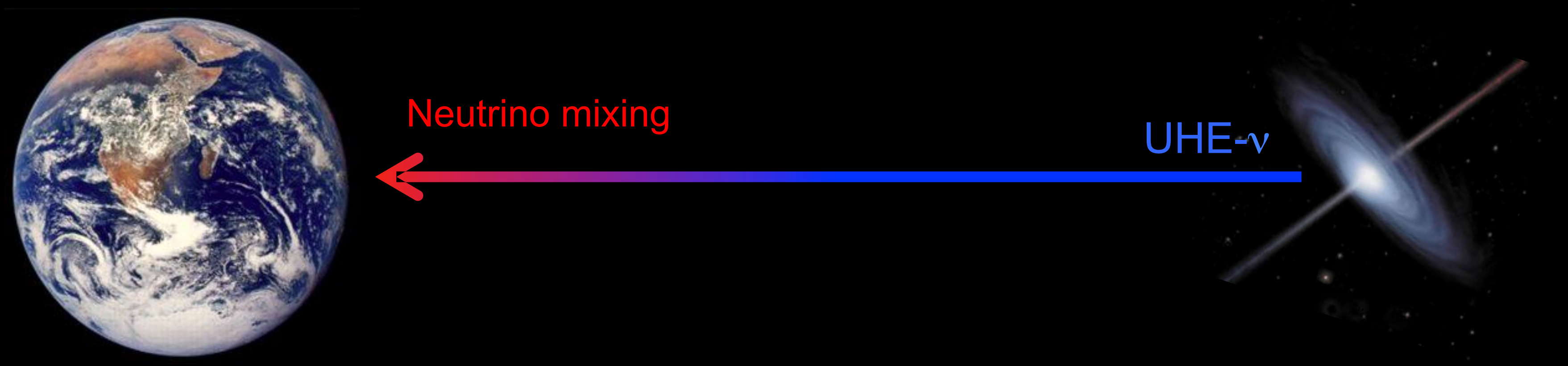
TK, Aruguelles, Halzen, Salvado
To be published

8. Lorentz violation with extra-terrestrial neutrinos

Combination of longer baseline and higher energy makes extra-terrestrial neutrino to be the most sensitive source of fundamental physics.

Vacuum Cherenkov radiation can limit new physics of neutrino up to 10^{-20}

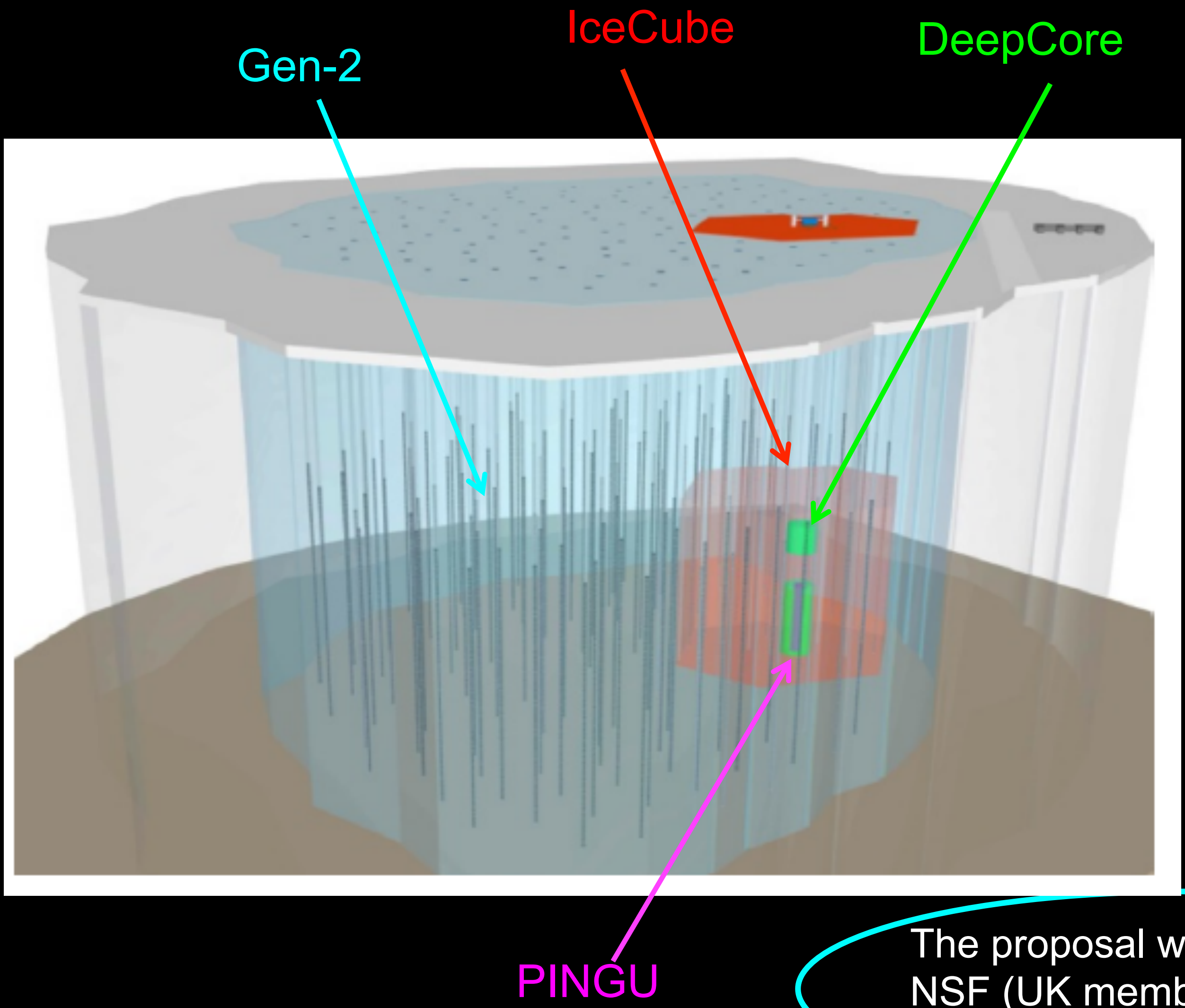
However, the neutrino mixing properties of UHE neutrinos can push this limit further ($\sim 10^{-34}$).
It is the most sensitive test of new physics (including Lorentz violation) with neutrinos.



More data at IceCube could reveal the new fundamental law of Nature...

IceCube-Gen2 collaboration
arXiv:1412.5106

8. IceCube-Gen2



Bigger IceCube and denser DeepCore can push their physics

Gen-2
Larger string separations to cover larger area

PINGU
Smaller string separation to achieve lower energy threshold for neutrino mass hierarchy measurement

The proposal will be submitted to NSF (UK members: Queen Mary, Oxford, Manchester)

Conclusion

Lorentz and CPT violation has been shown to occur in Planck-scale theories.

There is a world wide effort to test Lorentz violation with various state-of-the-art technologies.

LSND and MiniBooNE data suggest Lorentz violation is an interesting solution to neutrino oscillation.

MiniBooNE sets limits on Lorentz violation on $\nu_\mu \rightarrow \nu_e$ oscillation coefficients. These limits together with MINOS exclude simple Lorentz violation motivated scenario to explain LSND anomaly.

MiniBooNE, LSND, MINOS, IceCube, and Double Chooz, Super-Kamiokande set stringent limits on Lorentz violation in neutrino sector in terrestrial level.

Extra-terrestrial neutrinos from IceCube are one of the most sensitive tool to test fundamental physics, such as Lorentz violation.

Thank you for your attention!

backup

2. Comment: Is there preferred frame?

As we see, all observers are related with observer’s Lorentz transformation, so there is no special “preferred” frame (all observer’s are consistent)

But there is a frame where universe looks isotropic even with a Lorentz violating vector field. You may call that is the “preferred frame”, and people often speculate the frame where CMB looks isotropic is such a frame (called “CMB frame”).

However, we are not on CMB frame (e.g., dipole term of WMAP is nonzero), so we expect anisotropy by lab experiments even CMB frame is the preferred frame.

5. MiniBooNE experiment

MiniBooNE collaboration,
PRL102(2009)101802,
PRL105(2010)181801

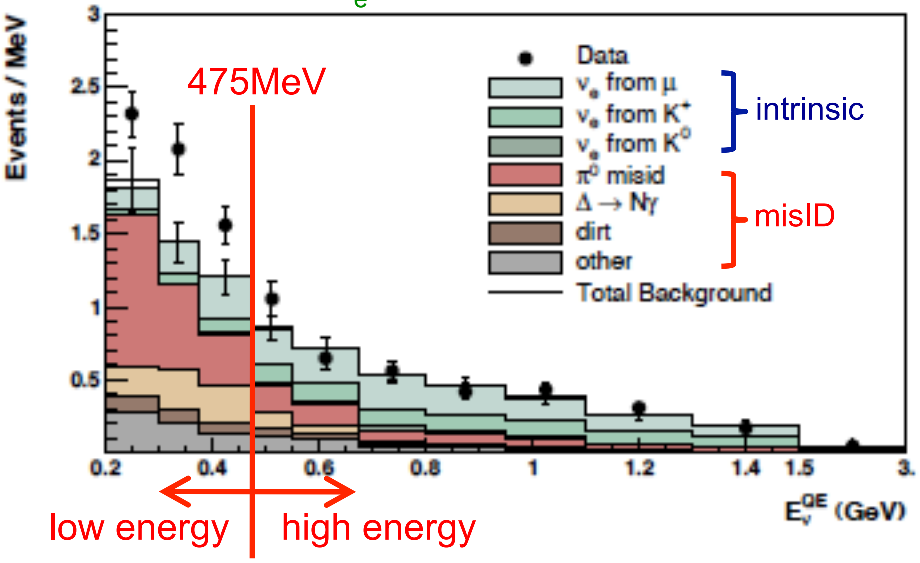
MiniBooNE is a short-baseline neutrino oscillation experiment at Fermilab.

$$\nu_\mu \xrightarrow{oscillation} \nu_e + n \rightarrow e^- + p$$

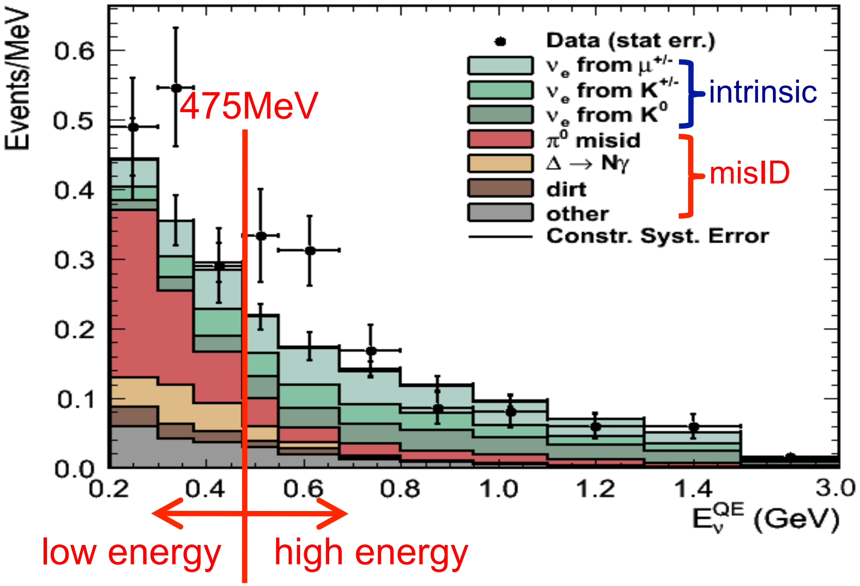
$$\bar{\nu}_\mu \xrightarrow{oscillation} \bar{\nu}_e + p \rightarrow e^+ + n$$

Neutrino mode analysis: MiniBooNE saw the 3.0σ excess at low energy region
Antineutrino mode analysis: MiniBooNE saw the 1.4σ excess at low and high energy region

MiniBooNE low E ν_e excess



MiniBooNE anti-ν_e excess



Intrinsic background errors are constraint from MiniBooNE data
Data driven corrections are applied to MisID backgrounds

MiniBooNE collaboration,
PRL102(2009)101802,
PRL105(2010)181801

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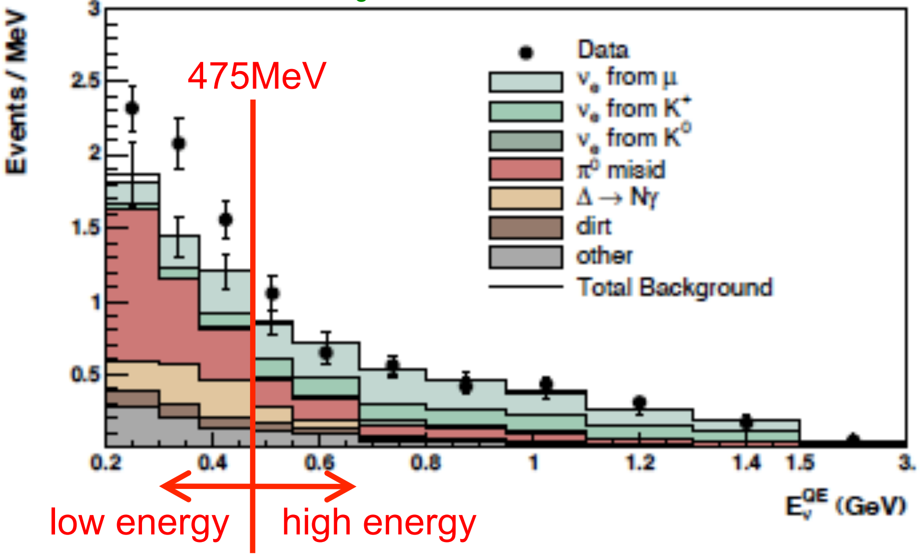
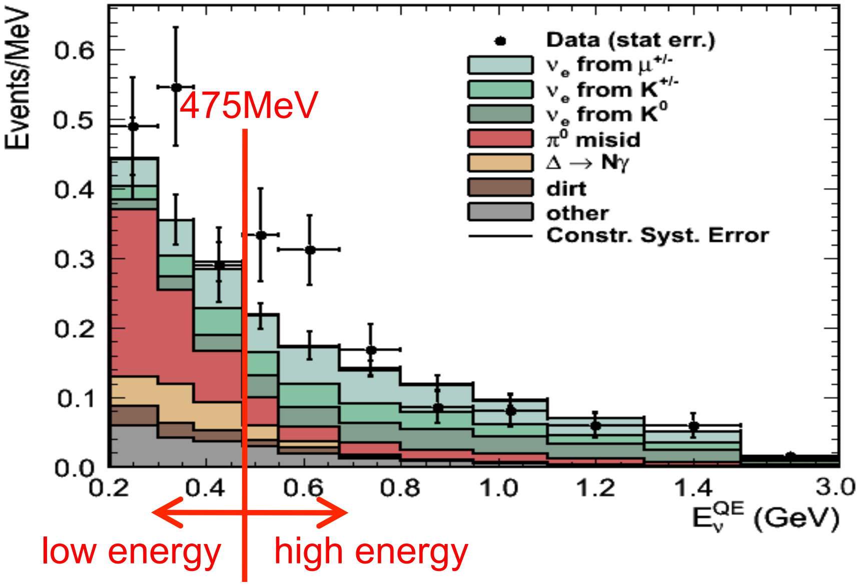


475MeV

low energy

high energy

MiniBooNE anti-ν_e excess



475MeV

low energy

high energy

These excesses are not predicted by neutrino Standard Model (νSM), therefor it might sterile neutrino or other new physics, such as Lorentz violation

→ Oscillation candidate events may have sidereal time dependence!

Kostelecký and Mewes
PRD70(2004)076002

6. Lorentz violation with MiniBooNE

Sidereal variation of neutrino oscillation probability for MiniBooNE (5 parameters)

$$P_{\nu_e\to\nu_\mu} = \left(\frac{L}{\hbar c}\right)^2 \left|(C)_{e\mu} + (A_s)_{e\mu}\sin w_\oplus T_\oplus + (A_c)_{e\mu}\cos w_\oplus T_\oplus + (B_s)_{e\mu}\sin 2w_\oplus T_\oplus + (B_c)_{e\mu}\cos 2w_\oplus T_\oplus\right|^2$$

Expression of 5 observables (14 SME parameters)

$$(C)_{e\mu} = (a_L)^T_{e\mu} - N^Z(a_L)^Z_{e\mu} + E\left[-\frac{1}{2}(3-N^ZN^Z)(c_L)^{TT}_{e\mu} + 2N^Z(c_L)^{TZ}_{e\mu} + \frac{1}{2}(1-3N^ZN^Z)(c_L)^{ZZ}_{e\mu}\right]$$

$$(A_s)_{e\mu} = N^Y(a_L)^X_{e\mu} - N^X(a_L)^Y_{e\mu} + E\left[-2N^Y(c_L)^{TX}_{e\mu} + 2N^X(c_L)^{TY}_{e\mu} + 2N^YN^Z(c_L)^{XZ}_{e\mu} - 2N^XN^Z(c_L)^{YZ}_{e\mu}\right]$$

$$(A_c)_{e\mu} = -N^X(a_L)^X_{e\mu} - N^Y(a_L)^Y_{e\mu} + E\left[2N^X(c_L)^{TX}_{e\mu} + 2N^Y(c_L)^{TY}_{e\mu} - 2N^XN^Z(c_L)^{XZ}_{e\mu} - 2N^YN^Z(c_L)^{YZ}_{e\mu}\right]$$

$$(B_s)_{e\mu} = E\left[N^XN^Y\left((c_L)^{XX}_{e\mu} - (c_L)^{YY}_{e\mu}\right) - (N^XN^X - N^YN^Y)(c_L)^{XY}_{e\mu}\right]$$

$$(B_c)_{e\mu} = E\left[-\frac{1}{2}(N^XN^X - N^YN^Y)\left((c_L)^{XX}_{e\mu} - (c_L)^{YY}_{e\mu}\right) - 2N^XN^Y(c_L)^{XY}_{e\mu}\right]$$

$$\begin{pmatrix} N^X \\ N^Y \\ N^Z \end{pmatrix} = \begin{pmatrix} \cos\chi\sin\theta\cos\phi - \sin\chi\cos\theta \\ \sin\theta\sin\phi \\ -\sin\chi\sin\theta\cos\phi - \cos\chi\cos\theta \end{pmatrix}$$

coordinate dependent direction vector
(depends on the latitude of FNAL, location of BNB and MiniBooNE detector)

OPERA collaboration,
ArXiv:1109.4897

8. Superluminal neutrinos

OPERA

$v(\text{neutrino}) = c + (2.37 \pm 0.32) \times 10^{-5}\, c$
$\quad = c + (16 \pm 2) \times 10^{3}$ mph

It is fascinating result, but...

- time of flight is kinematic test (less sensitive than neutrino oscillations)
- no indication of Lorentz violation from any neutrino oscillation experiments
- superluminal neutrino is unstable (vacuum Cherenkov radiation) ArXiv:1109.6562
- pion phase space is limited to create such neutrinos ArXiv:1109.6630
- SN1987A neutrinos provide severe limit to superluminal neutrinos PRL58(1987)1490
- etc...

It is very difficult to interpret superluminal neutrinos at OPERA by Lorentz violation within field theory approach.