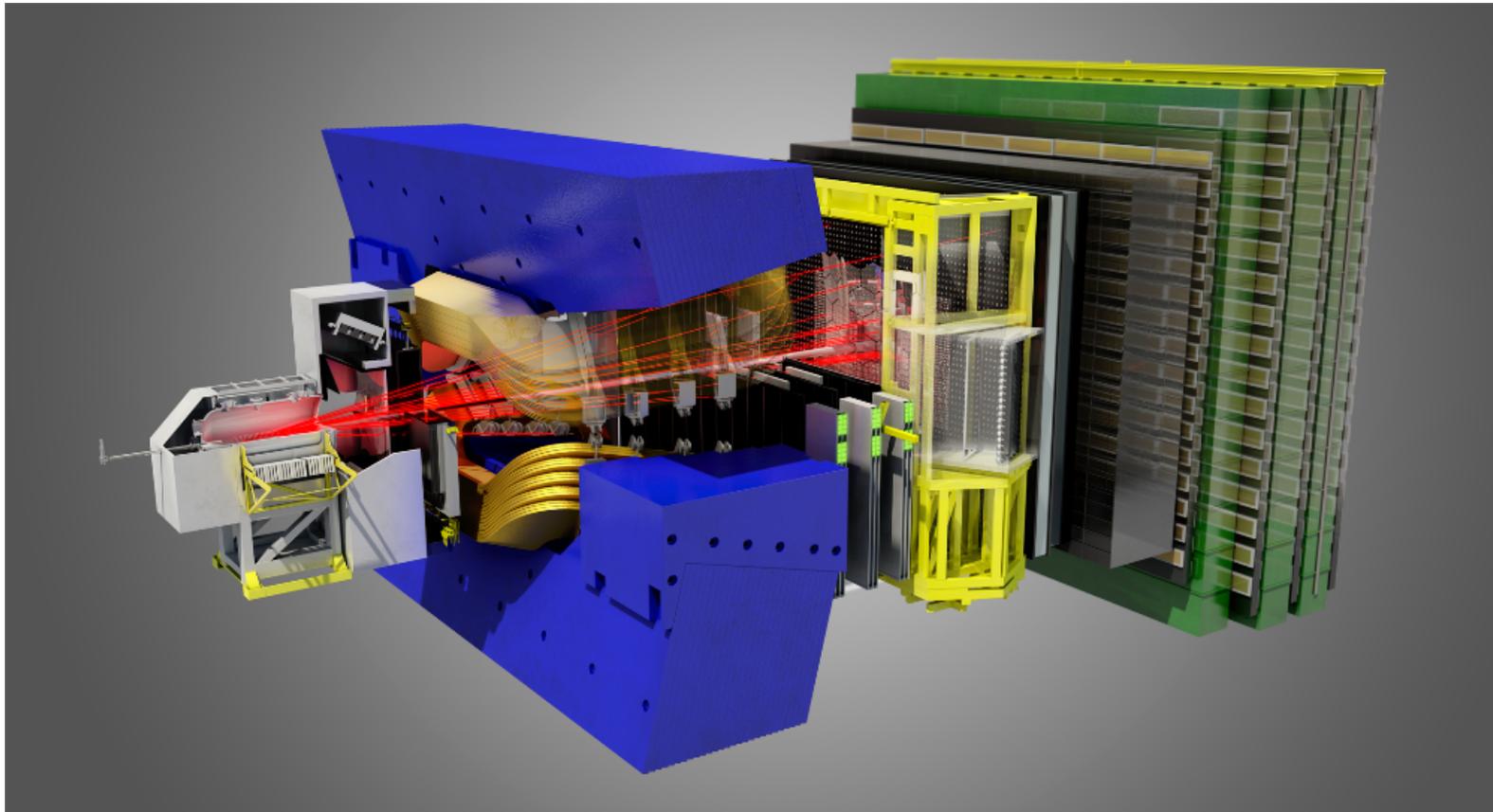


# Rare Decays at LHCb

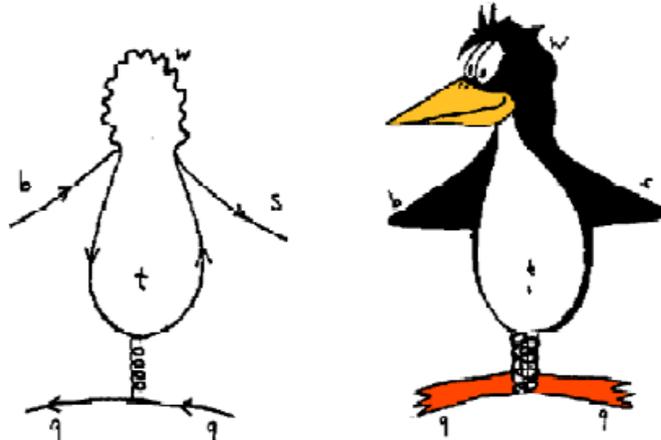


Mitesh Patel (Imperial College London)

The University of Birmingham, 2<sup>nd</sup> March 2016

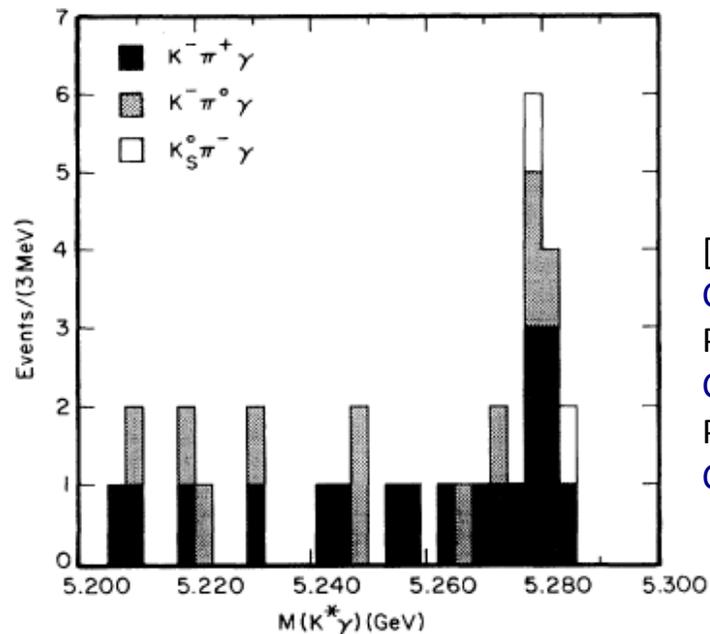
# The interest in Rare Decays

- Standard Model has no tree-level Flavour Changing Neutral Currents (FCNC)
- FCNC only occur as loop processes, proceed via penguin or box diagrams – sensitive to contributions from new (virtual) particles which can then be at same level as SM contributions
  - Probe masses  $> E_{\text{CM}}$  of the accelerator
- e.g.  $B_d^0 \rightarrow K^{*0} \gamma$  decay

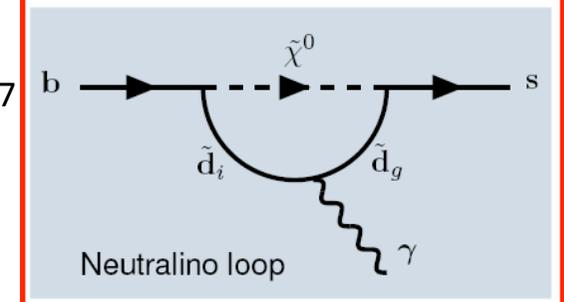
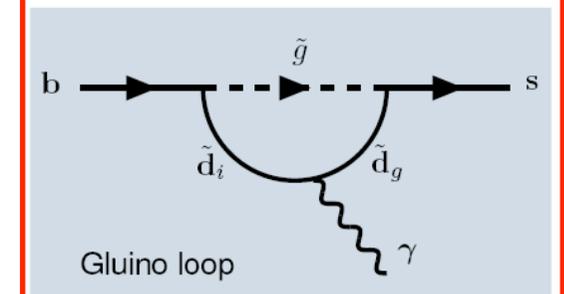
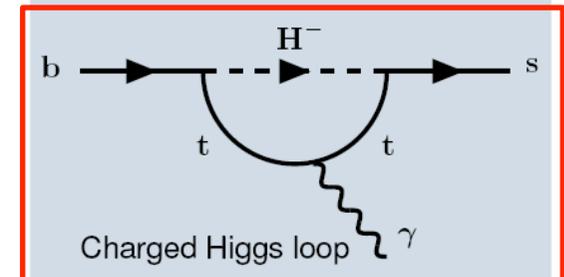
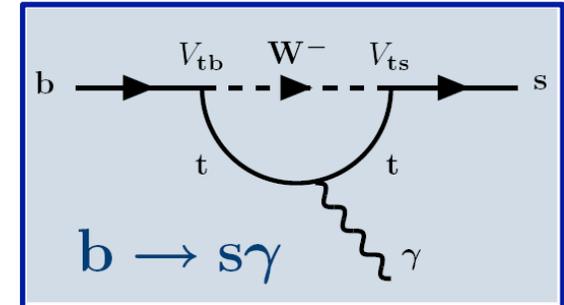


# A historical example – $B_d^0 \rightarrow K^{*0} \gamma$

- **In SM**: occurs through a dominating  $W$ - $t$  loop
- **Possible NP diagrams**:
- Observed by CLEO in 1993, two years before the direct observation of the top quark
  - BF was expected to be  $(2-4) \times 10^{-4}$
  - measured BF =  $(4.5 \pm 1.7) \times 10^{-4}$



[Phys.Rev.Lett. 71 (1993) 674 - Cited by 605 records  
 Phys.Rev.Lett. 74 (1995) 2885 - Cited by 836 records  
 Phys.Rev.Lett. 87 (2001) 251807 Cited by 565 records]



# Theoretical Foundation

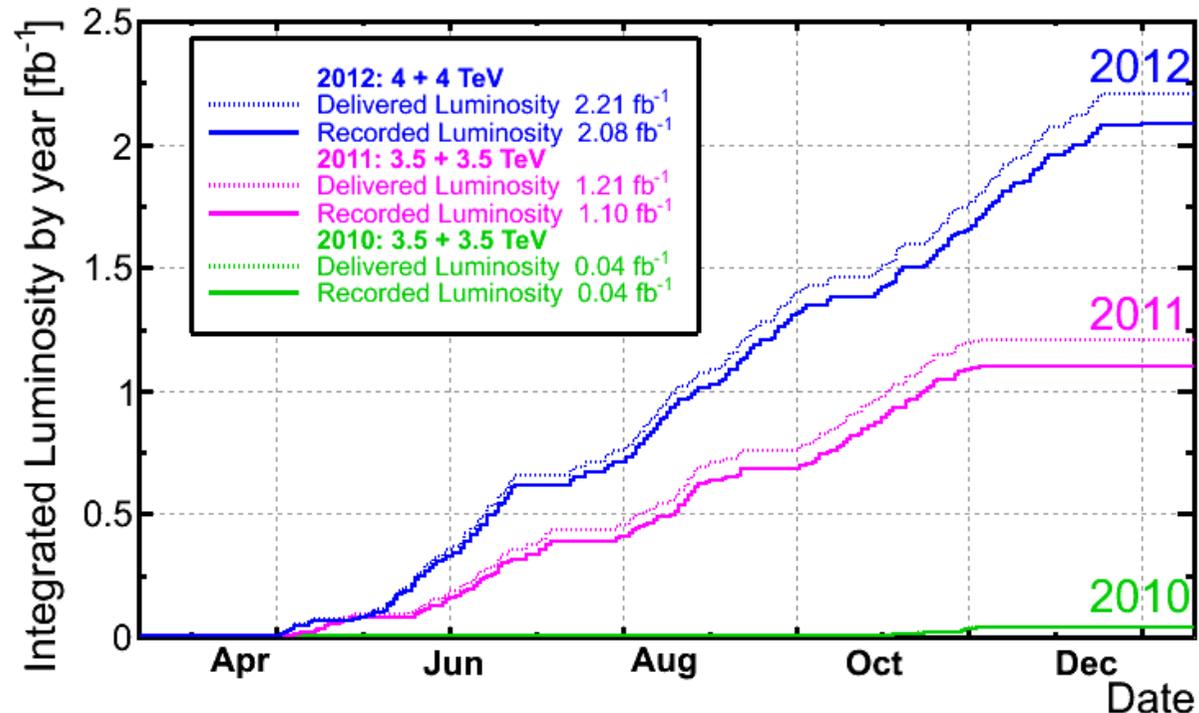
- The **Operator Product Expansion** is the theoretical tool that underpins rare decay measurements – rewrite SM Lagrangian as :

$$\mathcal{L} = \sum_i C_i O_i$$

- “Wilson Coefficients”  $C_i$ 
    - Describe the short distance part, can compute *perturbatively* in given theory
    - Integrate out the heavy degrees of freedom that can't resolve at some scale  $\mu$
  - “Operators”  $O_i$ 
    - Describe the long distance, *non-perturbative* part involving particles below scale  $\mu$
    - Account for effects of strong interactions and are difficult to calculate reliably
- **Form a complete basis – can put in all operators from NP/SM**

- Mixing between different operators :  $C_i \rightarrow C_i^{\text{effective}}$
- In *certain* observables the uncertainties on the operators cancel out – are then free from theoretical problems and measuring the  $C_i$  tells us about the heavy degrees of freedom – *independent of model*

# LHCb data-taking



- In total have recorded  $3\text{fb}^{-1}$  at instantaneous luminosities of up to  $4 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$  (twice the design value!)
- While Run-II data-taking will add substantial luminosity (so far  $0.3\text{fb}^{-1}$ ), will not be the step-change from higher  $\sqrt{s}$  anticipated at the central detectors – need 2019 upgrade for that step-change

# Outline

- A tour of existing LHCb rare decay measurements
  - $B^0 \rightarrow \mu\mu$  branching fraction measurements
  - $B_d^0 \rightarrow K^{*0} \mu\mu$  angular measurements
  - Other  $b \rightarrow s \mu\mu$  branching fraction measurements
  - Global fits to  $b \rightarrow s ll$  data
  - Mention a couple of other anomalous results
- (Very) latest  $B_d^0 \rightarrow K^{*0} \mu\mu$  angular results
  - Compatibility with SM
  - Updated global fits
- Some remarks about the future

# Outline

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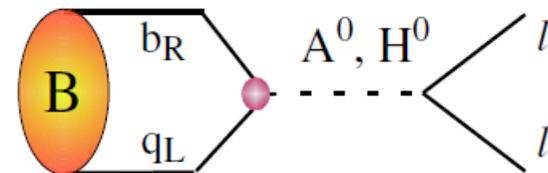
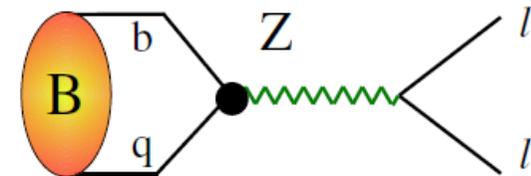
# $B^0 \rightarrow \mu^+ \mu^-$ – Physics Interest

- Both **helicity** suppressed and **GIM** suppressed

- In the **SM**,

- Dominant contribution from **Z-penguin** diagram
- Precise predictions for BFs :
- $B(B_s^0 \rightarrow \mu\mu) = (3.66 \pm 0.23) \times 10^{-9}$
- $B(B_d^0 \rightarrow \mu\mu) = (1.06 \pm 0.09) \times 10^{-10}$

[PRL 112 (2014) 101801]

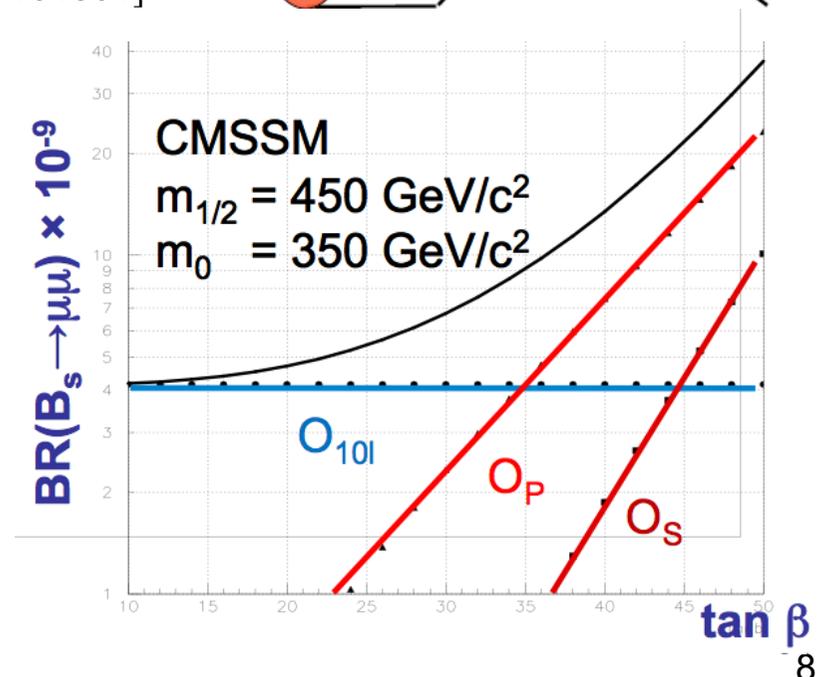


- In **NP** models,

- New scalar ( $O_S$ ) or pseudoscalar ( $O_P$ ) interactions can modify BF

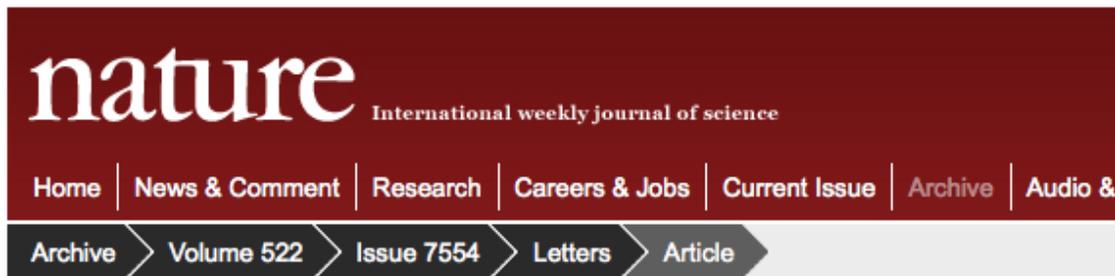
e.g. in **MSSM**, extended Higgs sector gives BF that scales with  $\tan^6 \beta / M_{A^0}^4$

→ **Extremely sensitive probe of NP!**



# $B^0 \rightarrow \mu^+ \mu^-$ analysis

LHCb's  $B^0 \rightarrow \mu^+ \mu^-$  analysis has now been combined with that from CMS :



NATURE | LETTER OPEN

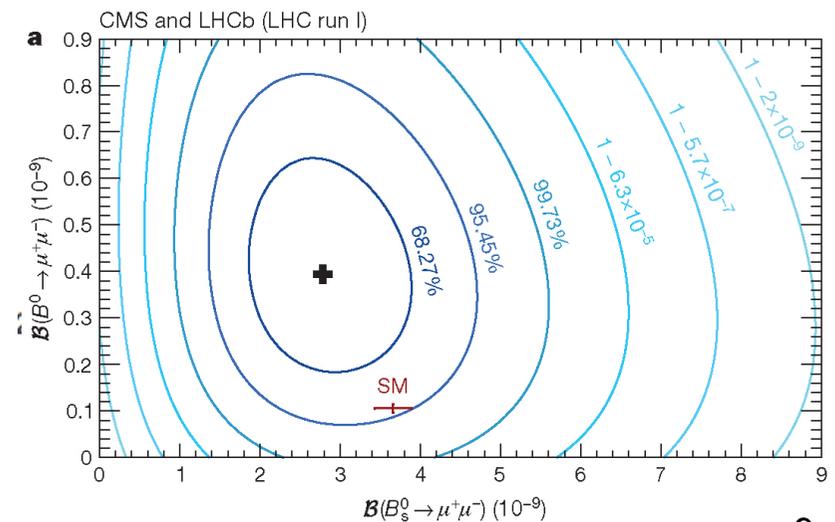
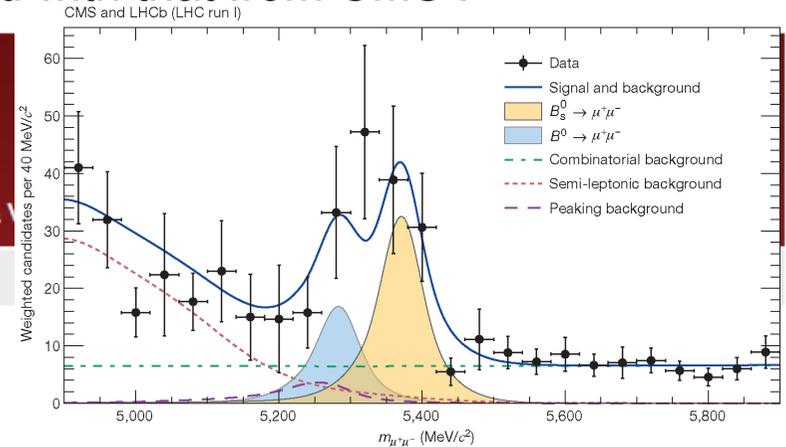
- Measure

- $B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8^{+0.7}_{-0.6}) \times 10^{-9}$

- $B(B_d^0 \rightarrow \mu^+ \mu^-) = (3.9^{+1.6}_{-1.4}) \times 10^{-9}$

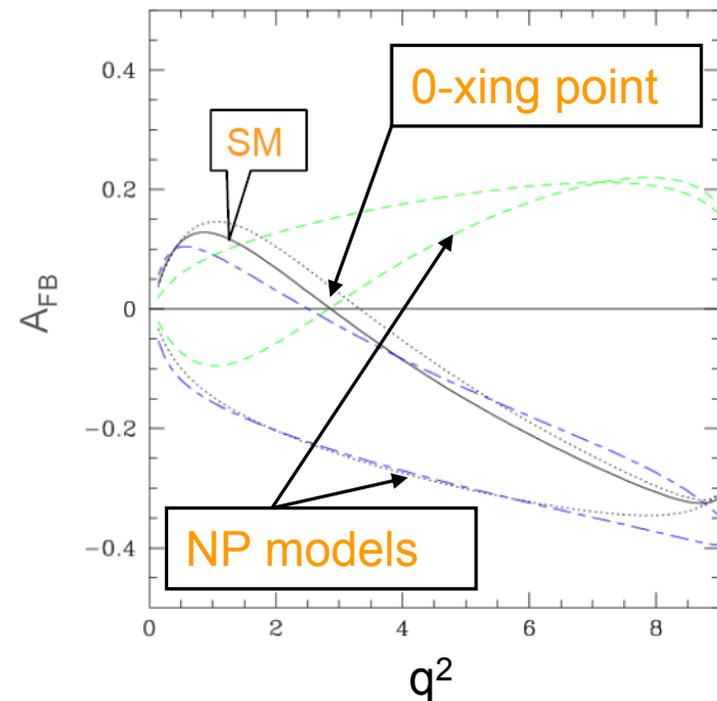
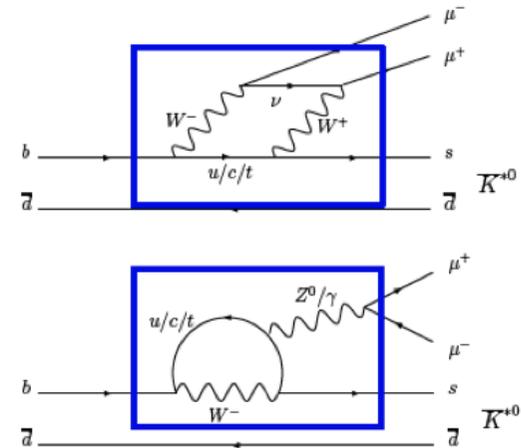
in good agreement with SM predictions

→ No evidence of NP contributions to  $C_S$  and  $C_P$



# $B_d^0 \rightarrow K^{*0} \mu \mu$ – Physics Interest

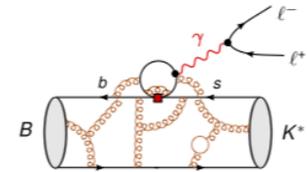
- Flavour changing neutral current  $\rightarrow$  loop process ( $\rightarrow$  sensitive to NP)
- Decay described by three angles ( $\theta_1, \phi, \theta_K$ ) and di- $\mu$  invariant mass  $q^2$
- Try to use observables where theoretical uncertainties cancel  
e.g. Forward-backward asymmetry  $A_{FB}$  of  $\theta_1$  distribution
- Zero-crossing point:  $\pm 6\%$  uncertainty



# $B_d^0 \rightarrow K^{*0} \mu \mu$ $C_i$ and form factors

- Amplitudes that describe the  $B_d^0 \rightarrow K^{*0} \mu \mu$  decay involve
  - The (effective) **Wilson Coefficients** :  $C_7^{\text{eff}}$  (photon),  $C_9^{\text{eff}}$  (vector),  $C_{10}^{\text{eff}}$  (axial-vector) and their right-handed (') counterparts
  - Seven (!) **form factors** – these are the origin of the primary theoretical uncertainties

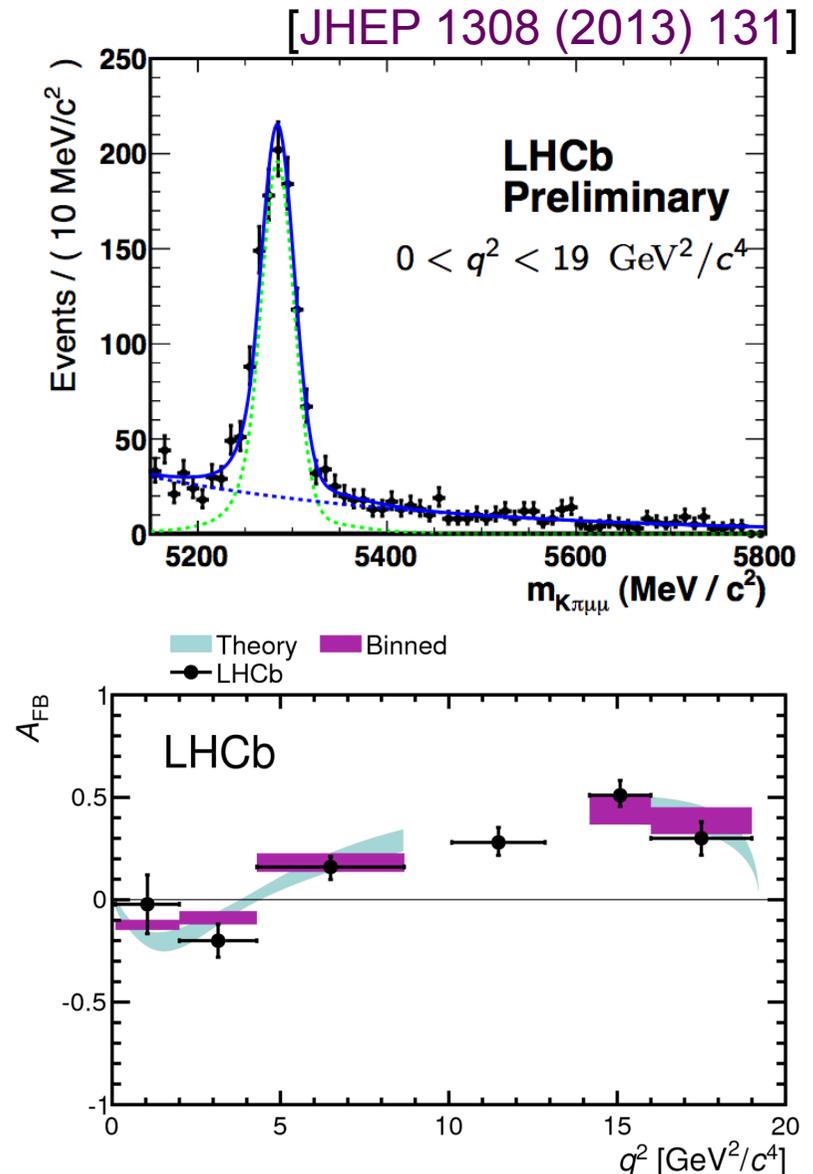
$$\begin{aligned}
 A_{\perp}^{L(R)} &= N\sqrt{2\lambda} \left\{ [(C_9^{\text{eff}} + C_9^{\prime\text{eff}}) \mp (C_{10}^{\text{eff}} + C_{10}^{\prime\text{eff}})] \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} (C_7^{\text{eff}} + C_7^{\prime\text{eff}}) T_1(q^2) \right\} \\
 A_{\parallel}^{L(R)} &= -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left\{ [(C_9^{\text{eff}} - C_9^{\prime\text{eff}}) \mp (C_{10}^{\text{eff}} - C_{10}^{\prime\text{eff}})] \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{2m_b}{q^2} (C_7^{\text{eff}} - C_7^{\prime\text{eff}}) T_2(q^2) \right\} \\
 A_0^{L(R)} &= -\frac{N}{2m_{K^*}\sqrt{q^2}} \left\{ [(C_9^{\text{eff}} - C_9^{\prime\text{eff}}) \mp (C_{10}^{\text{eff}} - C_{10}^{\prime\text{eff}})] [(m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*}) A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}}] \right. \\
 &\quad \left. + 2m_b (C_7^{\text{eff}} - C_7^{\prime\text{eff}}) [(m_B^2 + 3m_{K^*} - q^2) T_2(q^2) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(q^2)] \right\}
 \end{aligned}$$



- BFs have relatively large theoretical uncertainties from form factors
- Angular observables much smaller theory uncertainties

# 1<sup>st</sup> generation measurements

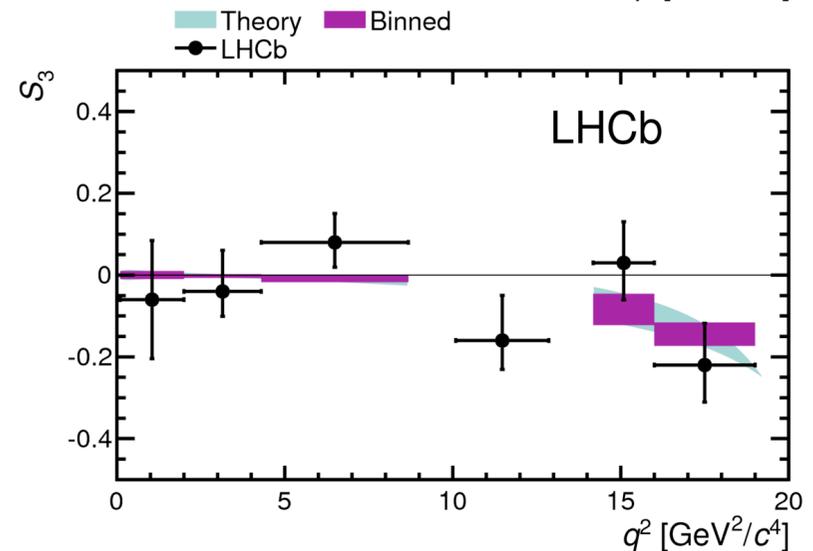
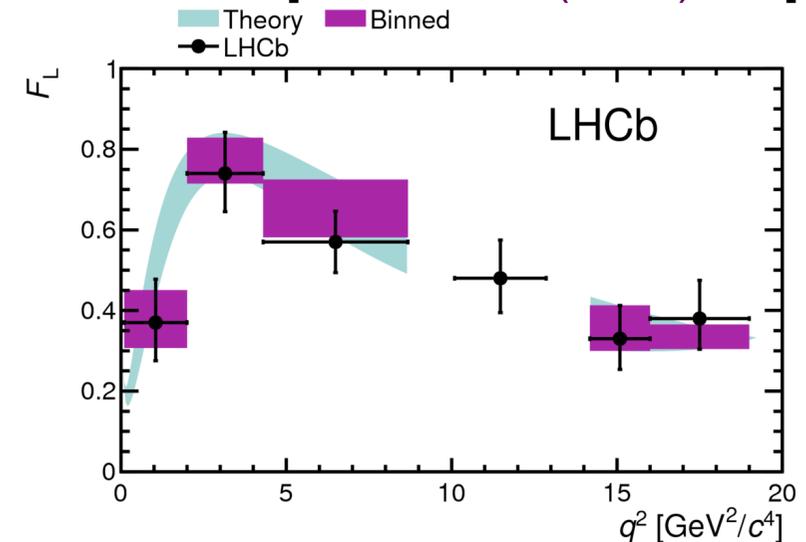
- With 2011 data found  $900 \pm 34$  signal events (BaBar + Belle + CDF  $\sim 600$ )
- $B/S \approx 0.25$
- World's most precise measurements of angular observables
- The world's 1<sup>st</sup> measurement of zero-crossing point at  $4.9^{+1.1}_{-1.3} \text{ GeV}^2/c^4$   
→ “a textbook confirmation of the SM”
- Seems theorists have good control of form factor uncertainties



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[JHEP 1308 (2013) 131]



# Form-factor independent obs.

- At low and high  $q^2$ , there are relations between the various form factors (at leading order) that allow a number of form-factor independent observables to be constructed
- E.g. in the region  $1 < q^2 < 6 \text{ GeV}^2$ , relations reduce the seven form-factors to just two – allows to form quantities like

$$P'_5 \sim \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^R A_{\perp}^{R*})}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2 + |A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)}}$$

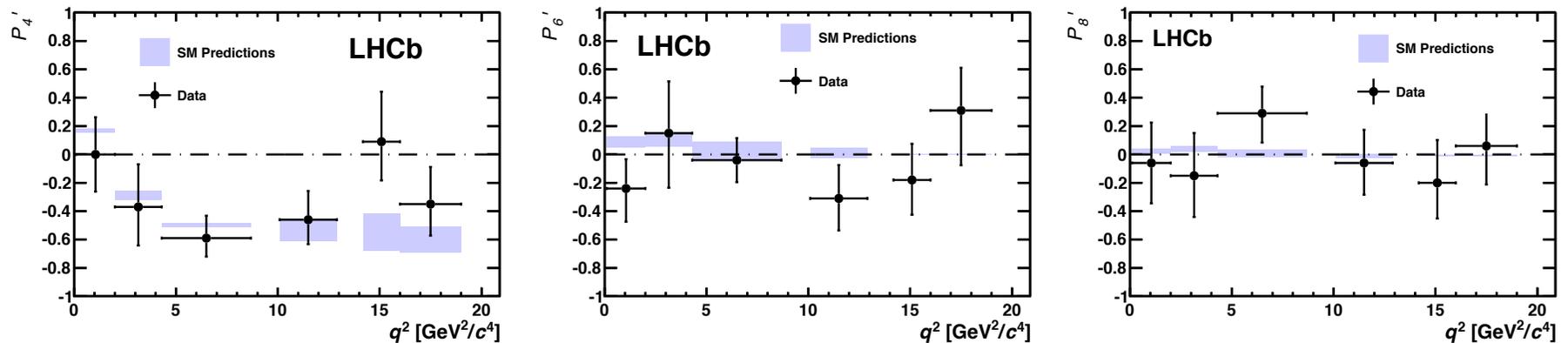
which are form-factor independent *at leading order*

- In fact can form a complete basis ( $P^{(')}$  series) in which there are six form-factor independent and two form-factor dependent observables ( $F_L$  and  $A_{FB}$ )
- Updated analysis measuring  $P^{(')}$  series of observables gave a surprise...

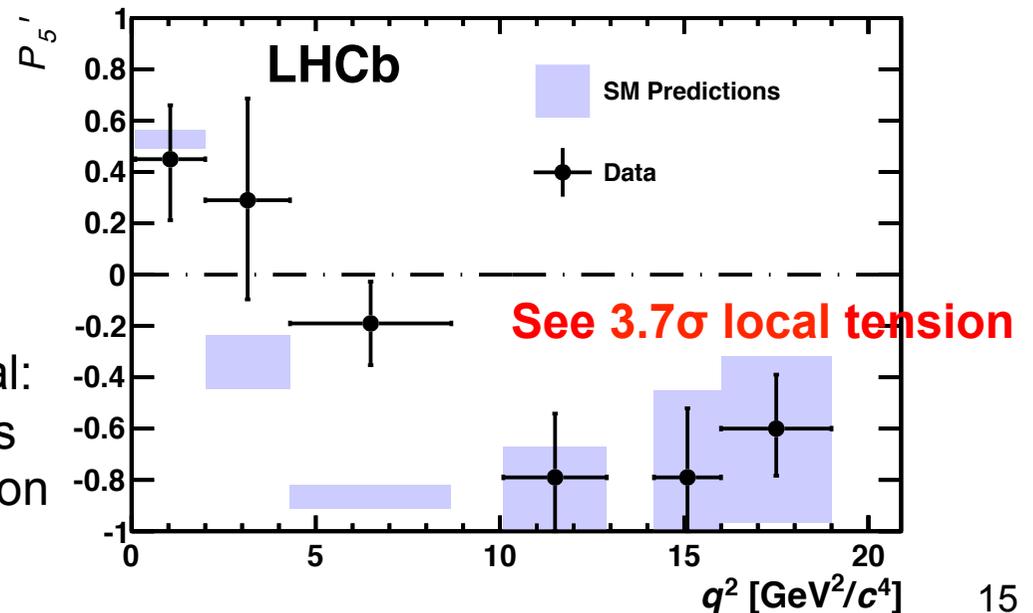
# $B_d^0 \rightarrow K^{*0} \mu^+ \mu^- - P(\prime)$ series

[Phys. Rev. Lett. 111 (2013) 191801]

- Good agreement with predictions for  $P_4'$ ,  $P_6'$ ,  $P_8'$  observables

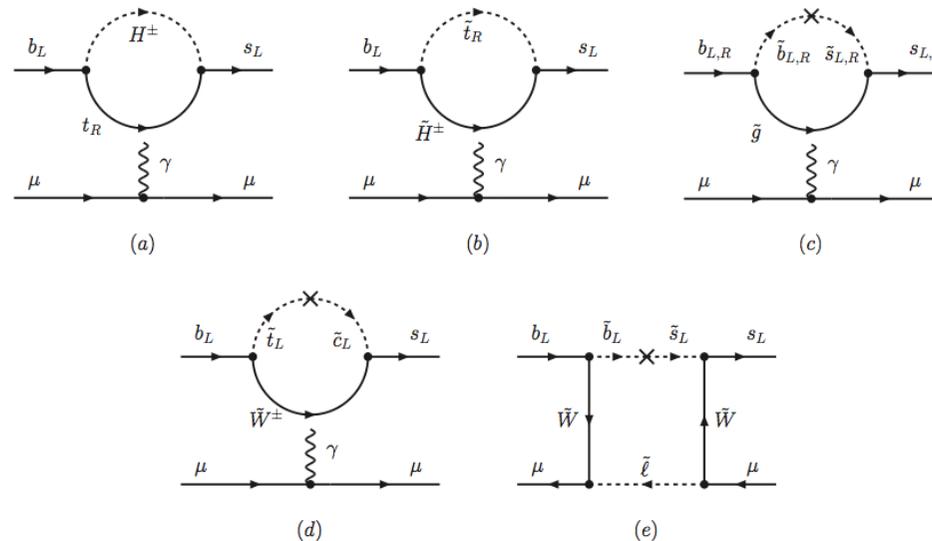


- 0.5% probability to see such a deviation with 24 independent measurements
- Finding a consistent NP explanation looks highly non-trivial: prev.  $B_d^0 \rightarrow K^{*0} \mu \mu$  observables plus  $B^0 \rightarrow \mu \mu$ ,  $B \rightarrow K \mu \mu$ ,  $B \rightarrow X_s \gamma$  depend on same short-distance physics



# $B_d^0 \rightarrow K^{*0} \mu\mu$ – theoretical view

- Need a new vector contribution  $\rightarrow$  adjusts  $C_9$  Wilson Coefficient
- Very difficult to generate in SUSY models [[arXiv:1308.1501](https://arxiv.org/abs/1308.1501)] :  
*“[ $C_9$  remains] SM-like throughout the viable MSSM parameter space, even if we allow for completely generic flavour mixing in the squark section”*



- Models with composite Higgs/extra dimensions have same problem
- **Could generate observed deviation with a  $Z'$**

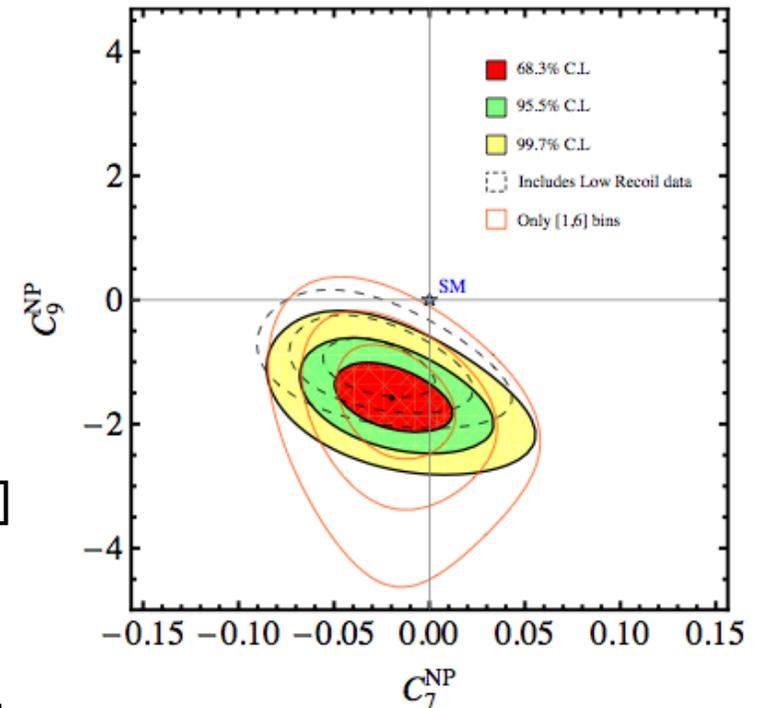
# $B_d^0 \rightarrow K^{*0} \mu \mu$ – theoretical view

- Theoretical analyses conclude deviation observed does **not** create any tension with other flavour observables
- e.g. [arXiv:1307.5683] consistent with negative NP contribution to  $C_9$  :  $\Delta C_9 \sim -1$
- Preferred value of  $C_9$  can be translated into NP scale in a model independent way but the answer depends on what else is considered in the fit e.g.

$$M_{Z'} \in [5.7, 6.9] \text{ TeV} \quad [\text{arXiv:1310.1082}]$$

$$\Lambda_{9^{(\prime)}} \simeq (35 \text{ TeV}) \left( \frac{1.0}{|C_9^{(\prime)}|} \right)^{1/2}$$

$$\Lambda_{9^{(\prime)}}^{\text{loop}} \simeq (2.8 \text{ TeV}) \left( \frac{1.0}{|C_9^{(\prime)}|} \right)^{1/2} \quad [\text{arXiv:1308.1501}]$$



# $B_d^0 \rightarrow K^{*0} \mu \mu$ – theoretical view

- While some theorists are very excited, some are less keen...

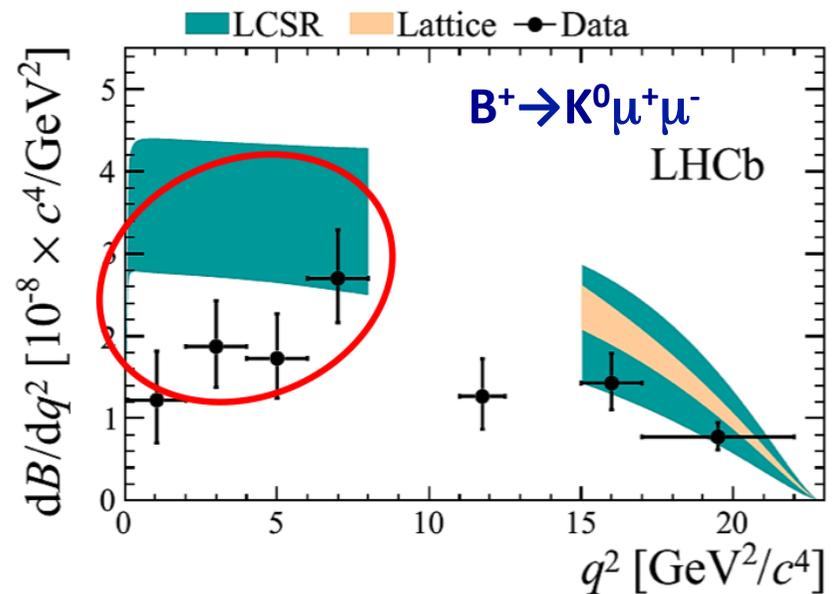
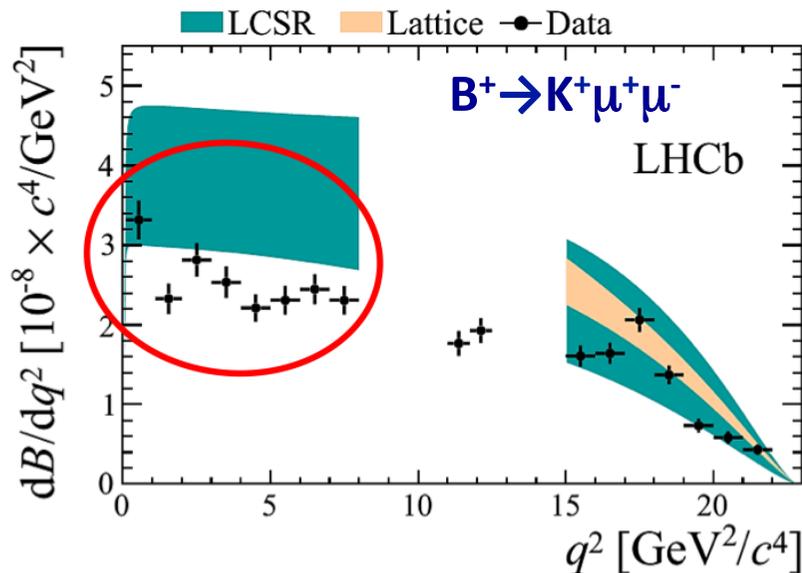
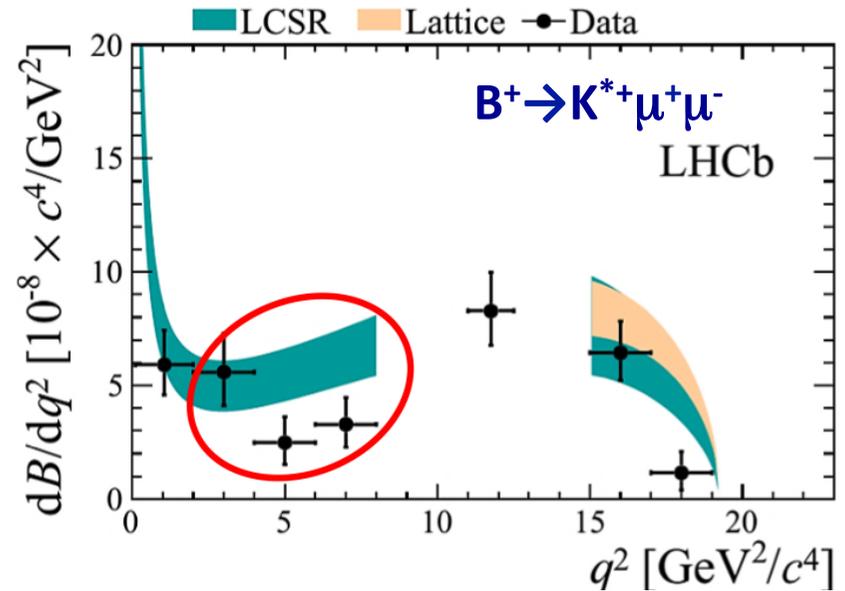


Ugly face of  $B \rightarrow K^* \mu^+ \mu^-$

# Adding the branching fractions...

- If we did have such a vector contribution we'd expect low branching fractions for other  $b \rightarrow s \mu \mu$  decays with different spectator quark

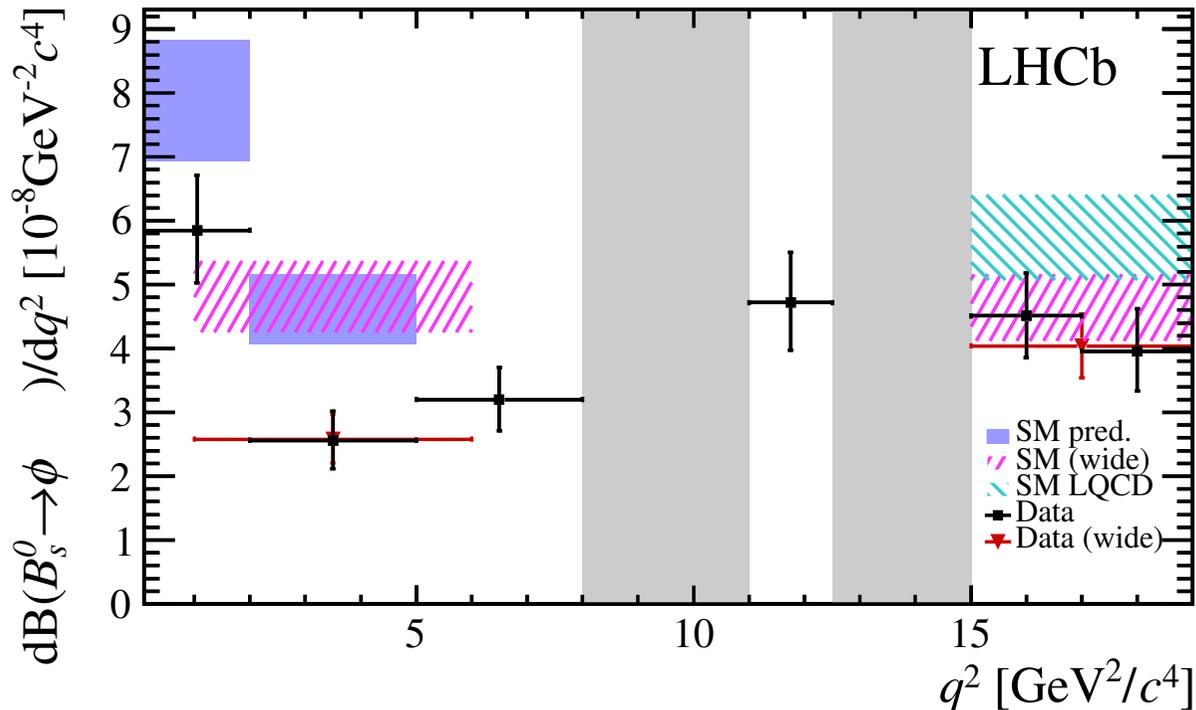
[JHEP 06 (2014) 133]



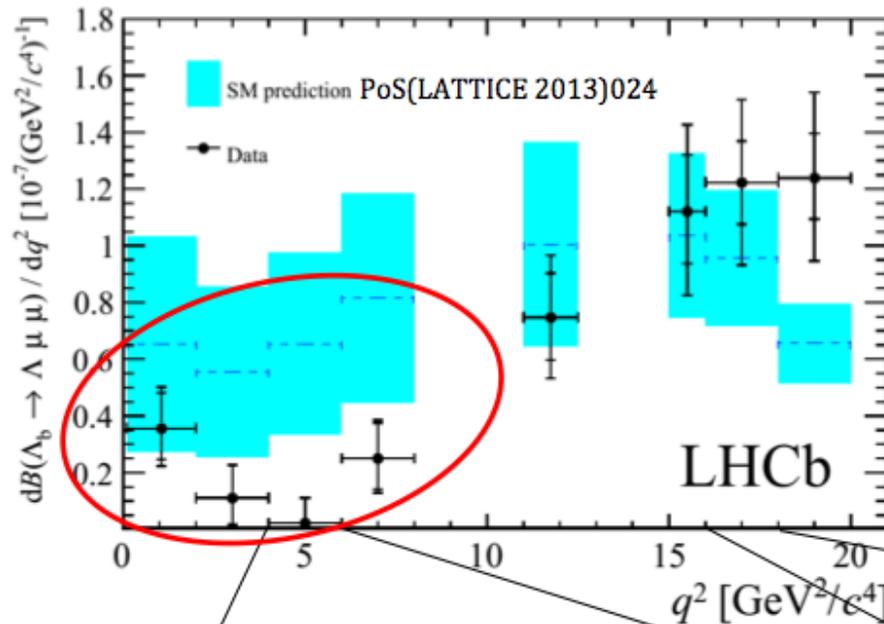
$$B_s^0 \rightarrow \phi \mu^+ \mu^-$$

- Measurements of  $B_s^0 \rightarrow \phi \mu^+ \mu^-$  show a similar trend in the low  $q^2$  region
  - Narrow  $\phi$  resonance gives clean signal
  - This measurement alone is  $3.3\sigma$  from SM prediction in  $1.0 < q^2 < 6.0 \text{ GeV}^2$

[JHEP09 (2015) 179]

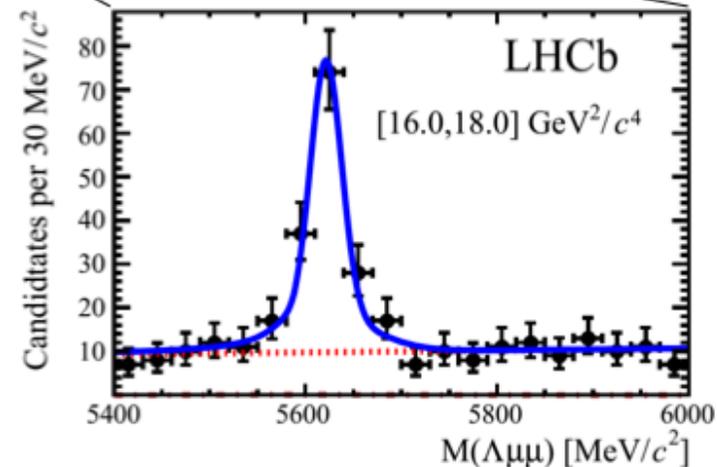
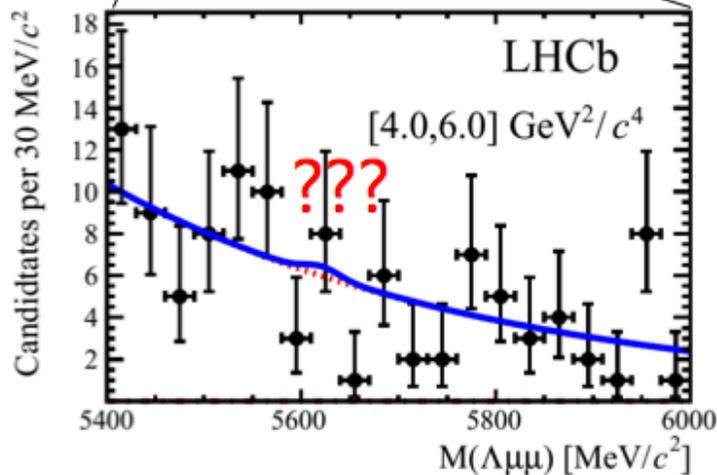


$$\Lambda_b \rightarrow \Lambda^0 \mu^+ \mu^-$$



- Have  $\sim 300 \Lambda_b \rightarrow \Lambda^0 \mu^+ \mu^-$  candidates at LHCb
- Establish evidence for signal  $0.1 < q^2 < 2.0 \text{ GeV}^2/c^4$  for 1<sup>st</sup> time, no significant signal in  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$

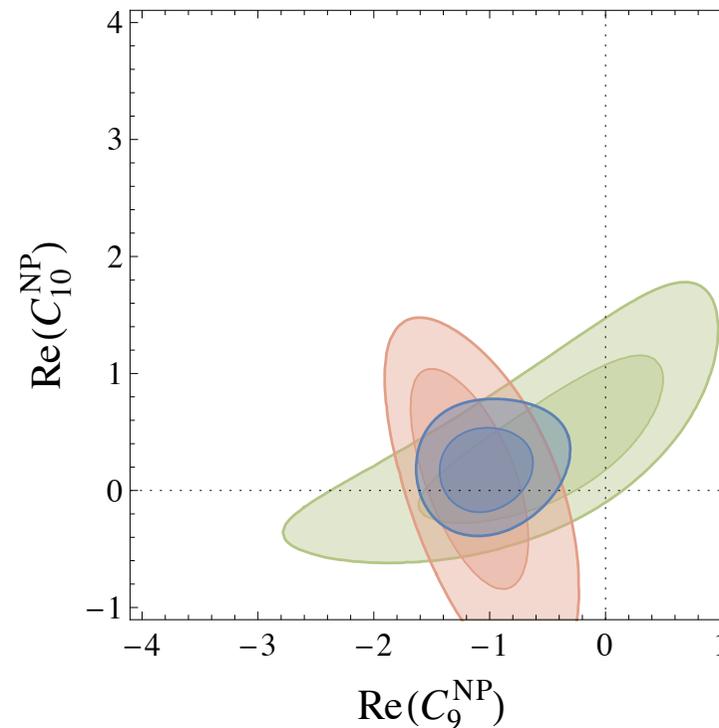
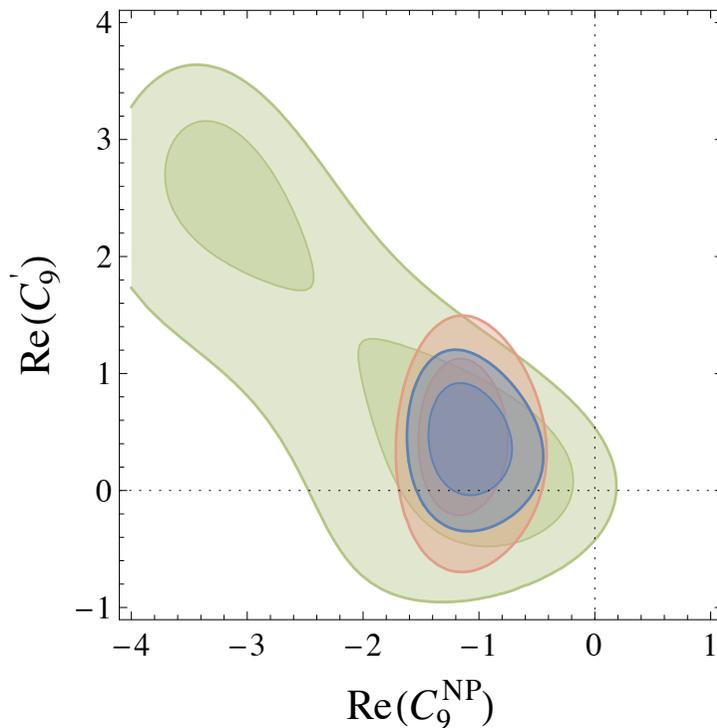
[JHEP 06 (2015) 115]



# Global fit to angular and BF data

- Fit the **angular** and **branching fraction** data :

[arXiv:1405.5182]



→ **BF data also favours same NP solution :  $\Delta C_9 \sim -1$  ;**

Can't tell if a two  $C_i$  solution preferred (e.g. V-A, impact  $B^0 \rightarrow \mu^+ \mu^-$ )

# The plot thickens: $R_K$

- The ratio of  $b \rightarrow s \mu \mu$  and  $b \rightarrow s e e$  branching fractions,  $R_K$ , is a theoretically pristine quantity

$$R_K = B(B^+ \rightarrow K^+ \mu^+ \mu^-) / B(B^+ \rightarrow K^+ e^+ e^-)$$

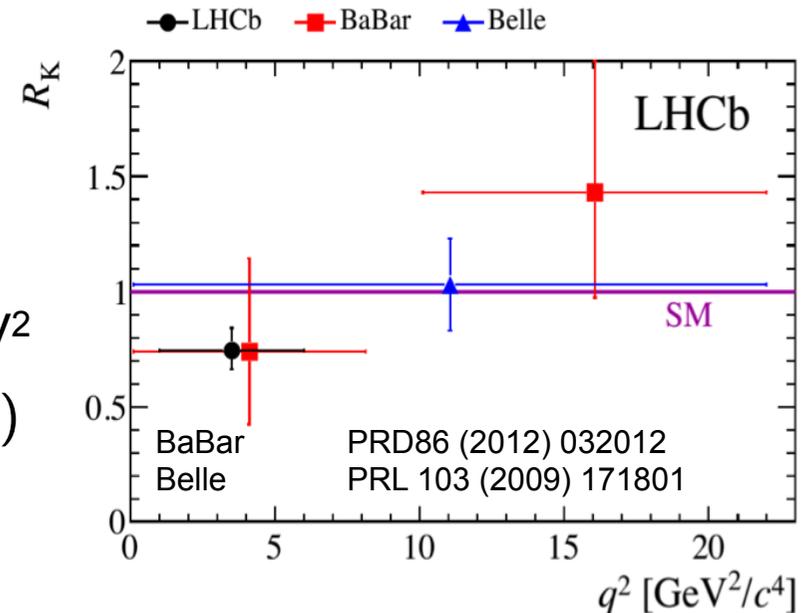
- Precisely predicted in SM,

$$R_K = 1.00030^{+0.00010}_{-0.00007}$$

- LHCb measurement in  $1.0 < q^2 < 6.0 \text{ GeV}^2$

$$R_K = 0.745^{+0.090}_{-0.074} (\text{stat})^{+0.036}_{-0.036} (\text{syst})$$

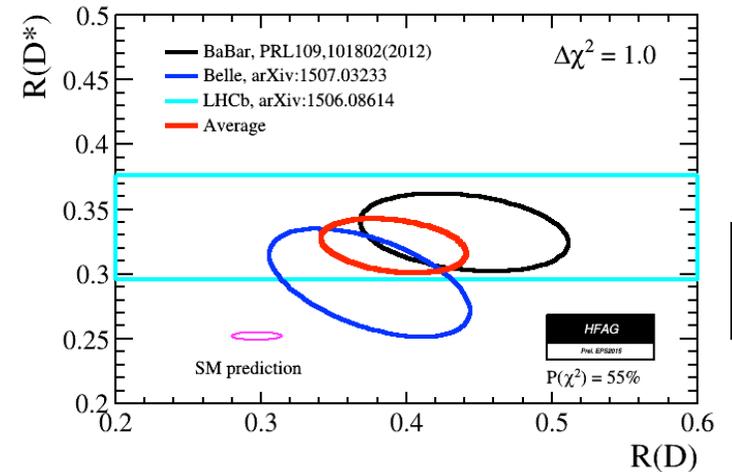
→  **$2.6\sigma$  from SM prediction**



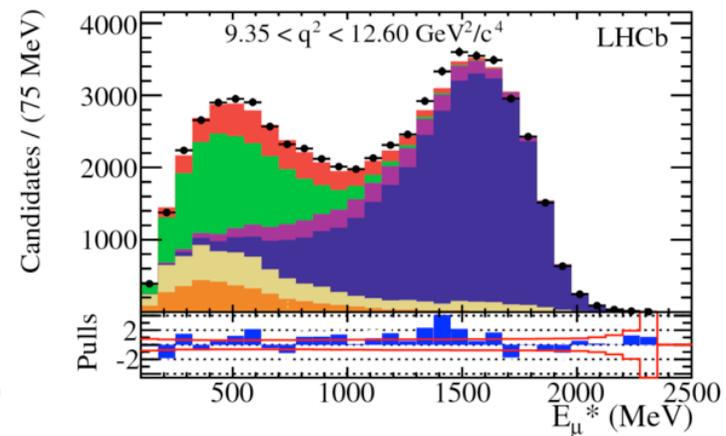
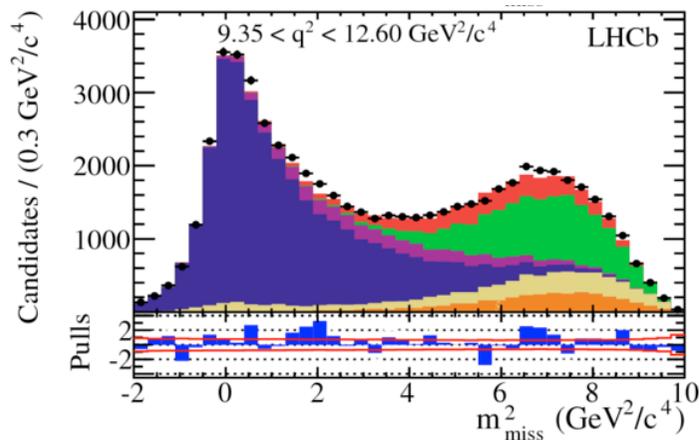
- Large number of theory models on the market pointing out this is consistent with  $\Delta C_9^{ee}=0$ ,  $\Delta C_9^{\mu\mu}=-1$  (latter consistent with  $B_d^0 \rightarrow K^{*0} \mu \mu$ )

# A short aside : $R_D^*$

- Note we also see an anomalous effect in the ratio of **tree-level** branching fractions  
 $R_D^* = B(B_d^0 \rightarrow D^{*+} \tau \nu) / B(B_d^0 \rightarrow D^{*+} \mu \nu)$
- Reconstruct the tauonic decay through  $\tau \rightarrow \mu \nu \nu$ , final state has three neutrinos!
- Confirms effect seen in  $R_D, R_D^*$  at BaBar/Belle, combined significance  $3.9\sigma$



[Phys.Rev.Lett. 115(2015)112001]



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- A tour of existing LHCb rare decay measurements
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  - Mention a couple of other anomalous results
- (Very) latest  $B_d^0 \rightarrow K^{*0} \mu\mu$  angular results
  - compatibility with SM
  - Updated global fits
- Some remarks about the future



# Full Run-I $B_d^0 \rightarrow K^{*0} \mu\mu$ update

- Our full run-I  $B_d^0 \rightarrow K^{*0} \mu\mu$  update recently published [[JHEP 02 \(2016\) 104](#)], dataset 3× larger than previous analysis
- For first time made full angular fit involving all angular terms → **complete set observables (and correlations)**
- Finer  $q^2$  binning → more shape information(\*), cross-check with a second (less precise) method
- First measurement of CP asymmetries, measurements of zero-crossing points by determining amplitudes as fn  $q^2$
- Will try and give a feeling for how the measurement is made...

(\* ) As well as low branching fractions,  $\Delta C_9 \sim -1$  would give a shift in  $A_{FB}$  26

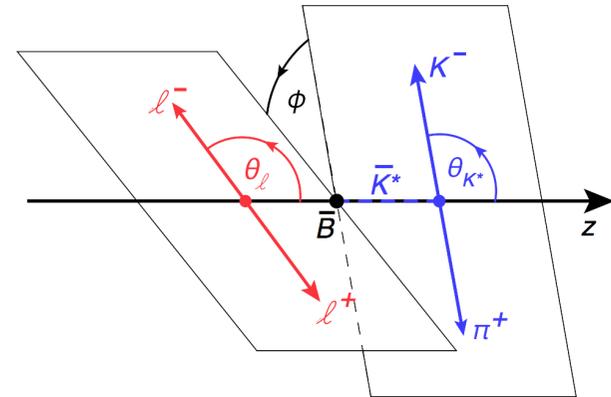
# Differential decay rate

- Decay described by di- $\mu$  invariant mass  $q^2$  and three decay angles  $\vec{\Omega} = (\cos \theta_l, \cos \theta_K, \phi)$

- Differential decay rate given

$$\frac{d^4\Gamma[\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_j I_j(q^2) f_j(\vec{\Omega})$$

$$\frac{d^4\bar{\Gamma}[B^0 \rightarrow K^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_j \bar{I}_j(q^2) f_j(\vec{\Omega})$$



- $I_j$  terms – eleven  $q^2$  dependent angular observables  
Can be expressed as bi-linear combinations of six complex decay amplitudes  $\mathcal{A}_{0,\parallel,\perp}^{\text{L,R}}$
- $f_j(\vec{\Omega})$  terms – combinations of spherical harmonics

# Angular observables

- Can define CP-averaged and CP-asymmetric observables

$$S_j = (I_j + \bar{I}_j) / \left( \frac{d\Gamma}{dq^2} + \frac{d\bar{\Gamma}}{dq^2} \right)$$

$$A_j = (I_j - \bar{I}_j) / \left( \frac{d\Gamma}{dq^2} + \frac{d\bar{\Gamma}}{dq^2} \right)$$

- Additional suffix **s/c** sometimes added to indicate  $\sin^2 \theta_K$  or  $\cos^2 \theta_K$  dependence;  $S_{1c} = F_L$ ;  $3/4 S_{6s} = A_{FB}$
- For large  $q^2$ ,  $\mu$ 's effectively massless – relations between different  $S_j$  terms, 11  $\rightarrow$  8 CP-averaged observables
- Further observables, optimised to reduce FF uncertainties, can be built from  $F_L$ ,  $S_3$ - $S_9$  e.g.  $P_5' = S_5 / \sqrt{F_L(1-F_L)}$

# CP-averaged angular distn

- CP-averaged angular distribution then given

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_P &= \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ &\quad + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l \\ &\quad - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \quad (!) \\ &\quad + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi \\ &\quad + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \\ &\quad \left. + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right] \end{aligned}$$

- For the 1<sup>st</sup> time, account for the effect of the  $K\pi$  system being in an S-wave configuration rather than  $K^{*0}$  P-wave

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_{S+P} &= (1 - F_S) \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_P \\ &\quad + \frac{3}{16\pi} F_S \sin^2 \theta_\ell \\ &\quad + \frac{9}{32\pi} (S_{11} + S_{13} \cos 2\theta_\ell) \cos \theta_K \quad (!! ) \\ &\quad + \frac{9}{32\pi} (S_{14} \sin 2\theta_\ell + S_{15} \sin \theta_\ell) \sin \theta_K \cos \phi \\ &\quad + \frac{9}{32\pi} (S_{16} \sin \theta_\ell + S_{17} \sin 2\theta_\ell) \sin \theta_K \sin \phi \end{aligned}$$

Determine  $A_i$  by flipping the sign in front of the corresponding angular terms for  $B^0$  decays while leaving unchanged for  $\bar{B}^0$  decays

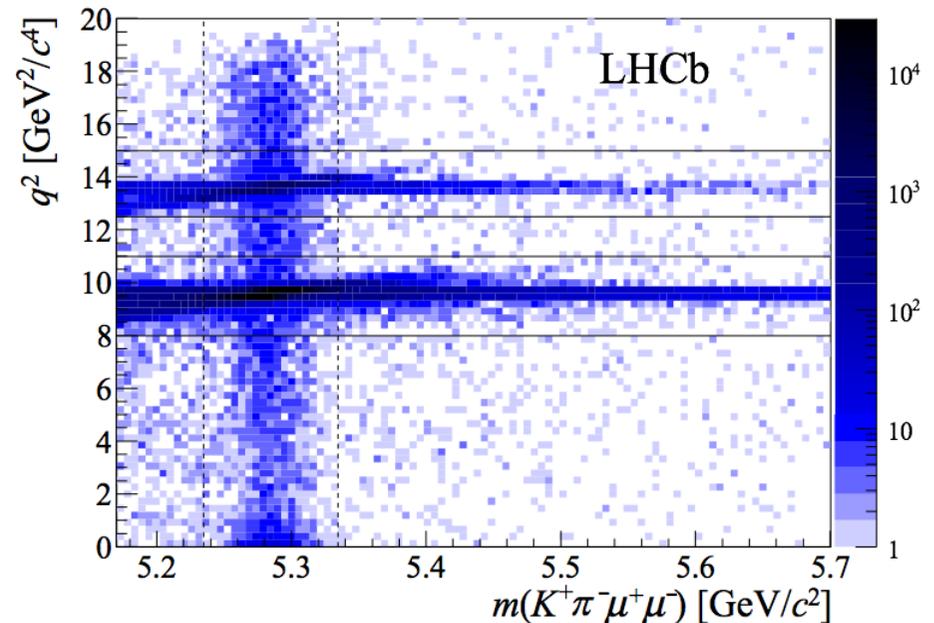
- two new amplitudes and six additional angular terms (explicitly included as nuisance parameters)

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ signal selection

- Selection uses range of PID, kinematic and isolation quantities in a Boosted Decision Tree

- Veto  $B^0 \rightarrow K^{*0} J/\psi$  and  $B^0 \rightarrow K^{*0} \psi(2S)$  decays, as well as a number of peaking backgrounds :

- evidence for  $\phi(1020)$  at low  $q^2$   
→ exclude  $0.98, < q^2 < 1.1 \text{ GeV}^2$
- Consider e.g.  $\Lambda_b \rightarrow p K^- \mu^+ \mu^-$ ;  
 $B_s \rightarrow \phi \mu^+ \mu^-$ ;  $B^{0,+} \rightarrow K^{*0,+} \mu^+ \mu^- \dots$

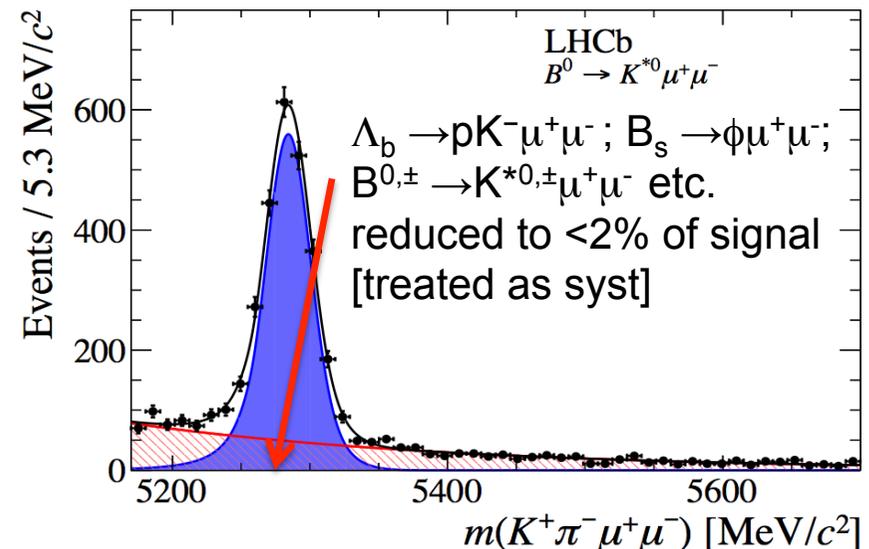


- After selection, signal clearly visible as vertical band  
Clean enough to allow finer  $q^2$  binning than for  $1 \text{ fb}^{-1}$

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ signal selection

- Signal  $K\pi\mu\mu$  mass model
  - sum of two Gaussians with power law tail on low mass-side
  - defined using  $B^0 \rightarrow K^{*0} J/\psi$  control channel (correct for  $q^2$  dependence using simulation)
  - Combinatorial background modelled with falling exponential

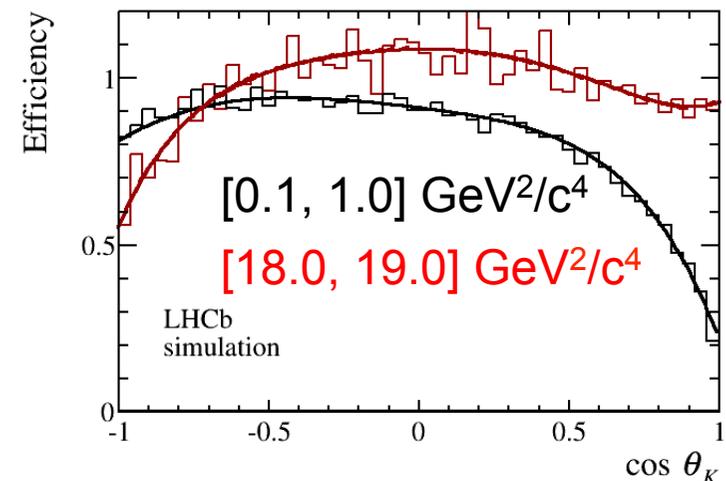
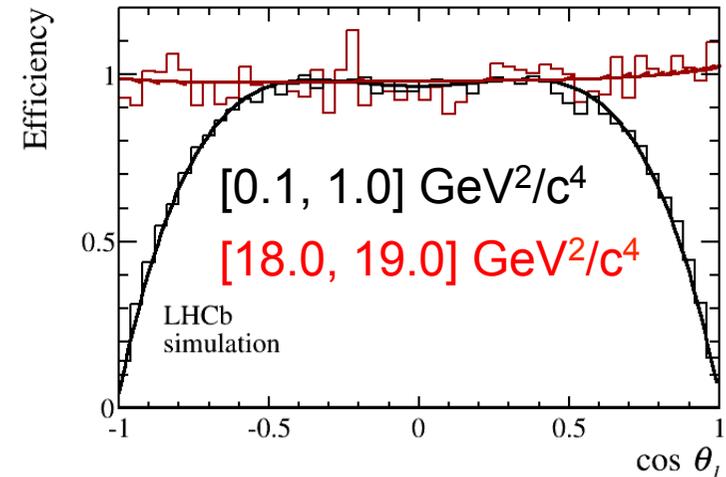
- $K\pi$  mass model :
  - Rel. Breit Wigner for P-wave
  - LASS for S-wave
  - Linear model for bkgnd



- Find  $2398 \pm 57$  signal events in  $0.1 < q^2 < 19.0 \text{ GeV}^2/c^4$   
( $624 \pm 30$  events in  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$ )

# Correcting for the efficiency

- Detector and selection distort the angular and  $q^2$  distribution
  - Momentum/IP requirements
- Compute 4D efficiency function,  $\varepsilon$ , using simulated events
  - $\varepsilon(\cos \theta_l, \cos \theta_K, \phi, q^2)$
- Function of all underlying variables  $\rightarrow$  can determine with a phase-space simulation



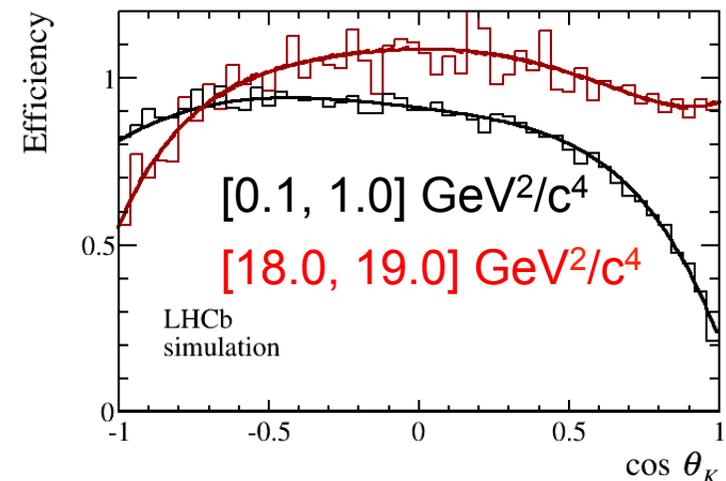
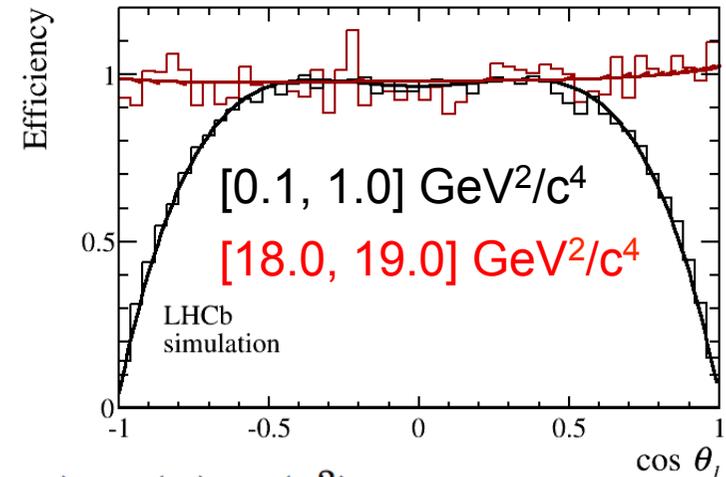
# Correcting for the efficiency

- Acceptance is **not** assumed to factorise in the decay angles
- Parameterised,

$$\varepsilon(\cos \theta_l, \cos \theta_K, \phi, q^2) = \sum_{klmn} c_{klmn} P_k(\cos \theta_l) P_l(\cos \theta_K) P_m(\phi) P_n(q^2)$$

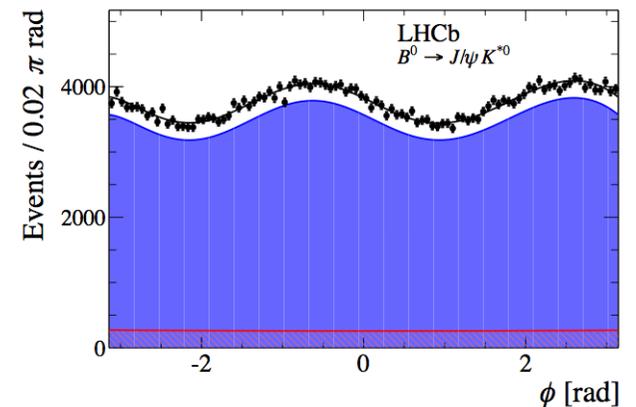
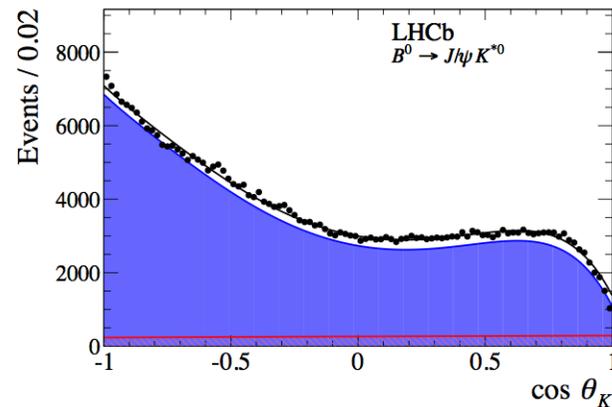
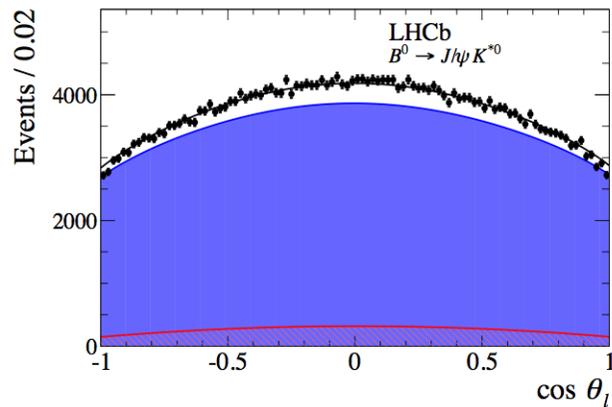
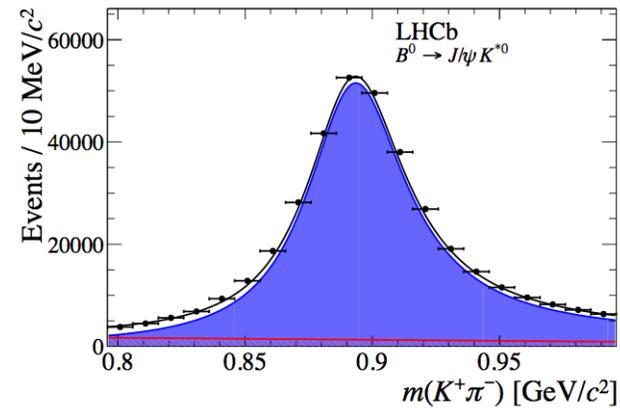
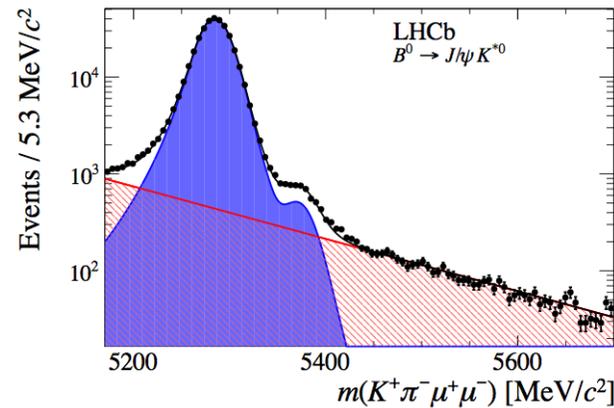
- $P_i(x)$  are Legendre polynomials of order  $i$  ( $x$  rescaled  $-1 \rightarrow 1$ )
- For  $\cos \theta_l, \cos \theta_K, \phi, q^2$  use up-to and including 4<sup>th</sup>, 5<sup>th</sup>, 6<sup>th</sup>, 5<sup>th</sup> order polynomials

- Coeff  $c_{klmn}$  determined using a principal moments analysis



# $B^0 \rightarrow K^{*0} J/\psi$ angular fit

- Reproduce angular observables measured elsewhere  
[PRD 88 (2013) 052002]



# Likelihood fit

- In each  $q^2$  bin, unbinned maximum likelihood fit to  $m_{K\pi\mu\mu}$  and three decay angles, plus a simultaneous fit to  $m_{K\pi}$
- Angular distribution
  - Signal – large expression showed before
  - Bkgrd – second order polynomials in  $\cos \theta_l, \cos \theta_K, \phi$
- Application of acceptance,  $\varepsilon$ 
  - Narrow  $q^2$  bins, multiply angular pdf by acceptance at bin centre [syst.]
  - Wide  $1.1 < q^2 < 6.0 \text{ GeV}^2$  and  $15.0 < q^2 < 19.0 \text{ GeV}^2$  bins –  $\varepsilon$  varies significantly across bin, weight candidates by  $\varepsilon^{-1}$ , correct for coverage
- Feldman-Cousins used to determine parameter uncertainties
  - Nuisance parameters (e.g. other angular parameters, signal fraction, background parameters...) treated with plug-in method

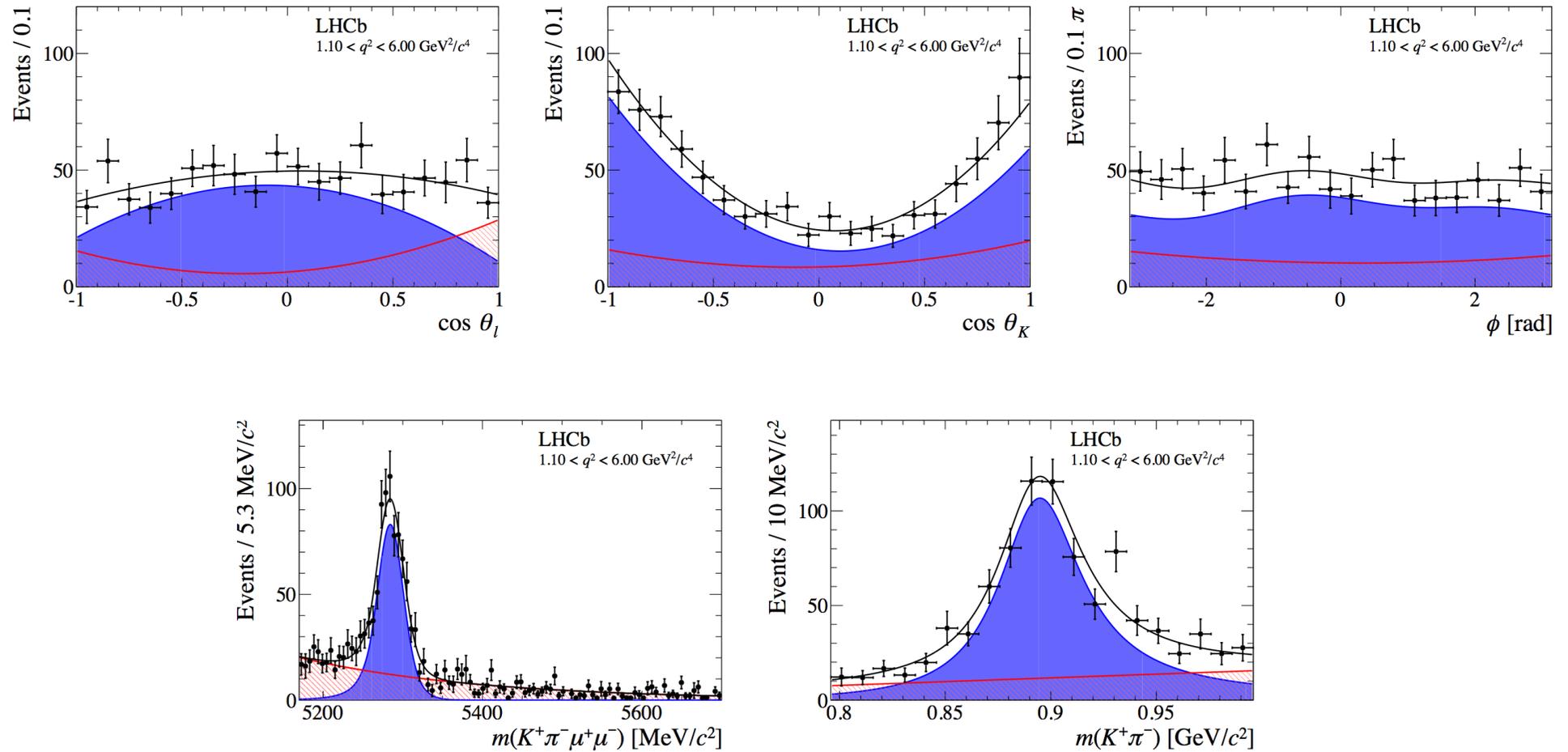
# Systematics

- Evaluated using high statistics pseudoexpts where vary approach and look at difference in angular observables
- Signal – main effects from angular acceptance :
  - Statistical uncert. from simulation [re-evaluate using cov.]
  - Residual data-simulation differences [reweight for diffs,re-eval.]
  - Uncert. associated with parameterisation [increase order polyn.]
  - Uncertainty from evaluating acceptance at fixed  $q^2$  point  
[alter point used]
- Background
  - Angular model [increase order polyn.]
- Bias from higher  $K^*$  states negligible

# Systematics

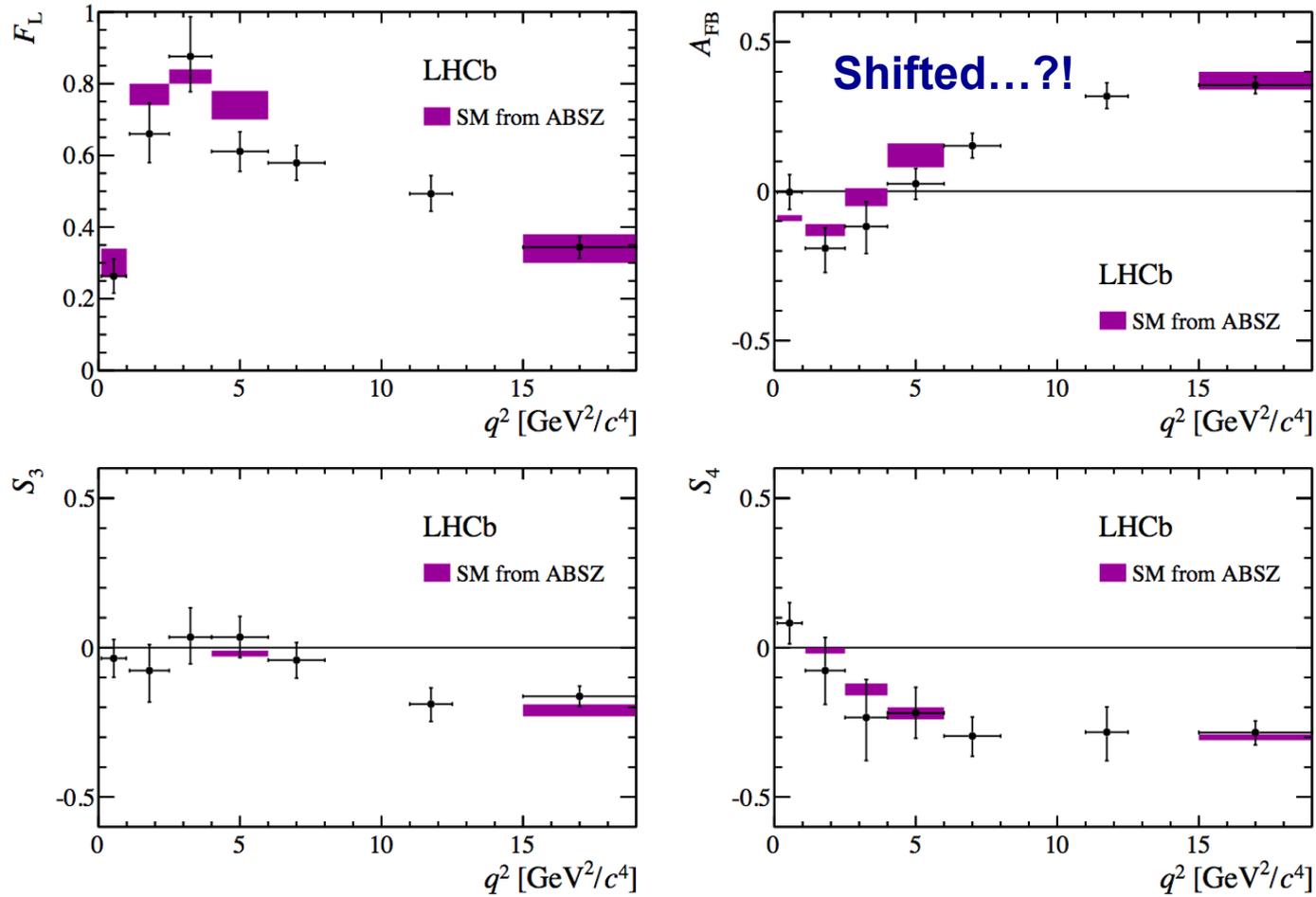
- Include angular distribution of residual peaking bkgrds
- Mass modelling
  - $m_{K\pi\mu\mu}$  – drop power law tails
  - $m_{K\pi}$  – radius used in Breit Wigner for P-wave; LASS  $\rightarrow$  isobar
- [For amplitude fit] S-wave amplitudes constant with  $q^2 \rightarrow$  assume same  $q^2$  dependence as long. P-wave amplitude
- Production/detection asymmetries give negligible contribution to  $A_i$ 's
- In general, syst. significantly smaller than stat.
  - e.g.  $F_L(A_{FB})$  – syst 30 (20)% of stat. [largest  $p_\pi$  mismatch]

# Fit projection $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$

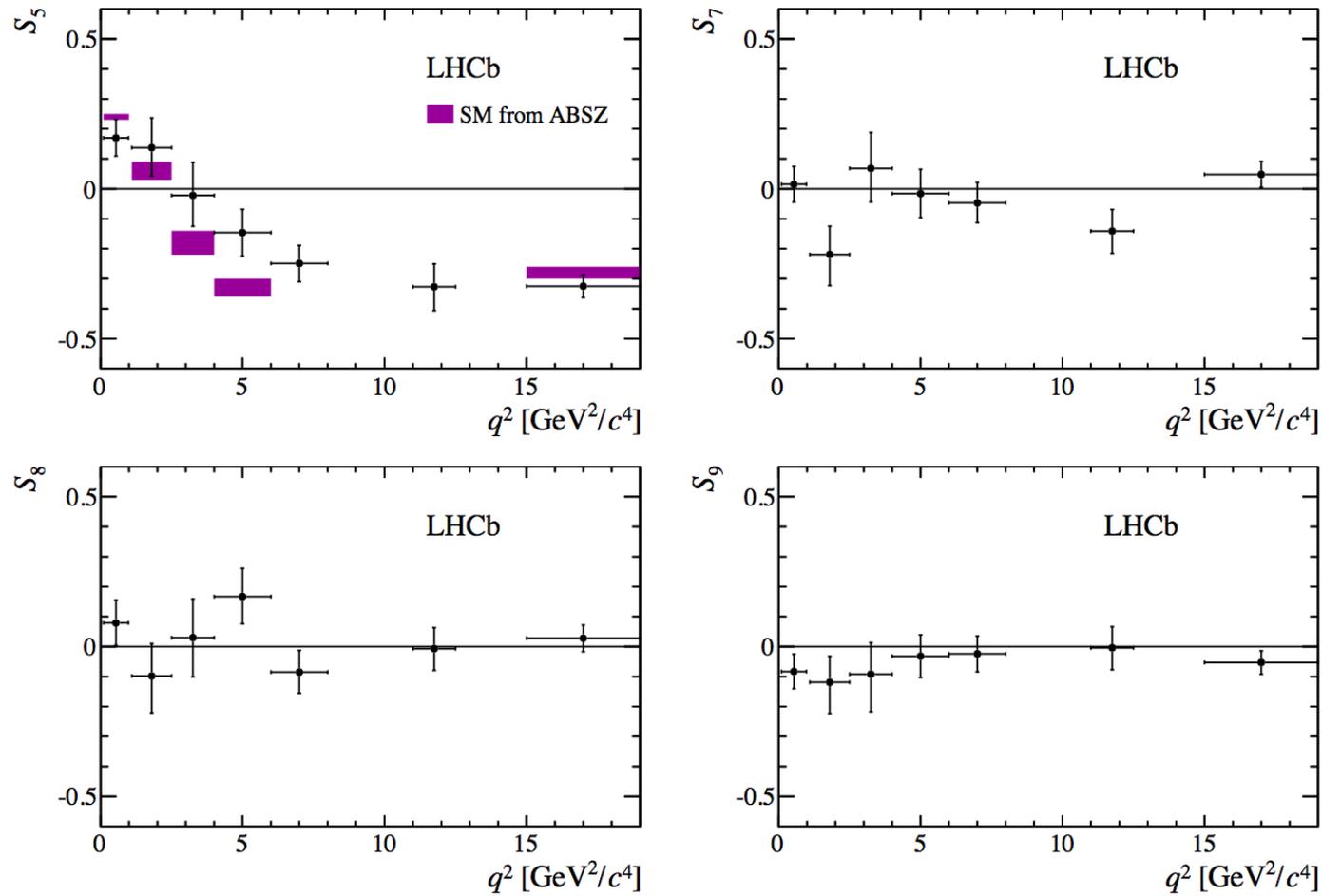


NB: weighted candidates

# Results: Likelihood, CP-avgd

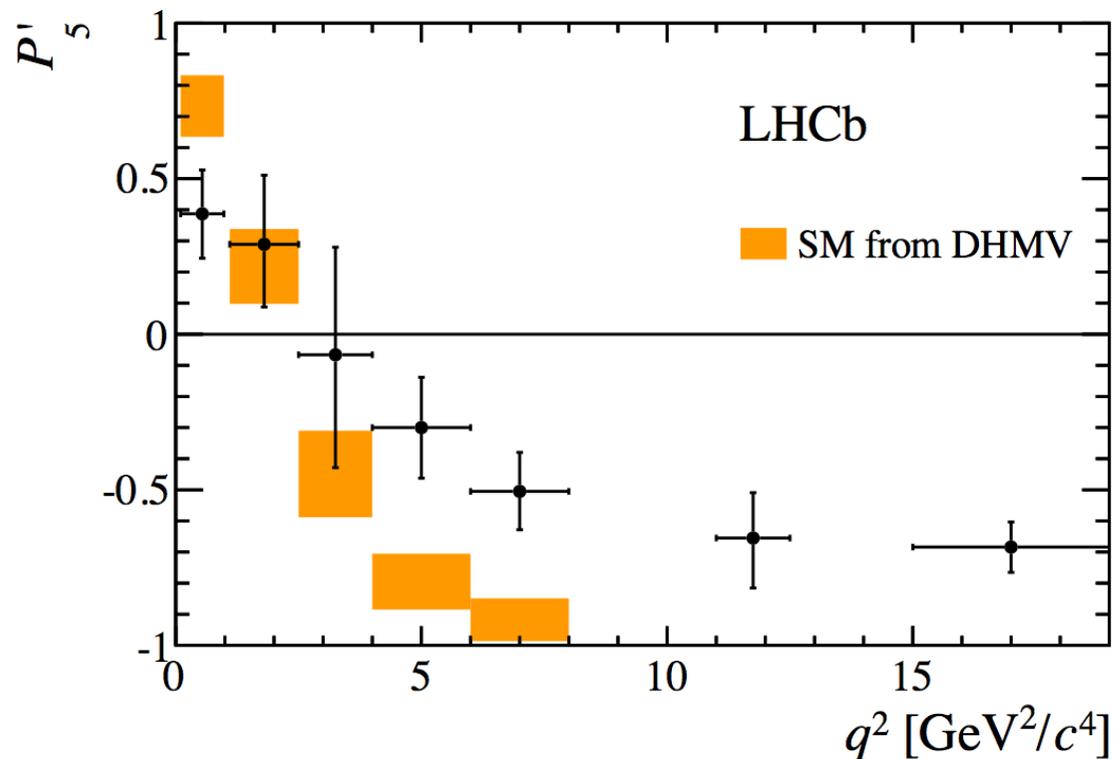


# Results: Likelihood, CP-avgd



# Results: Likelihood, CP-avgd

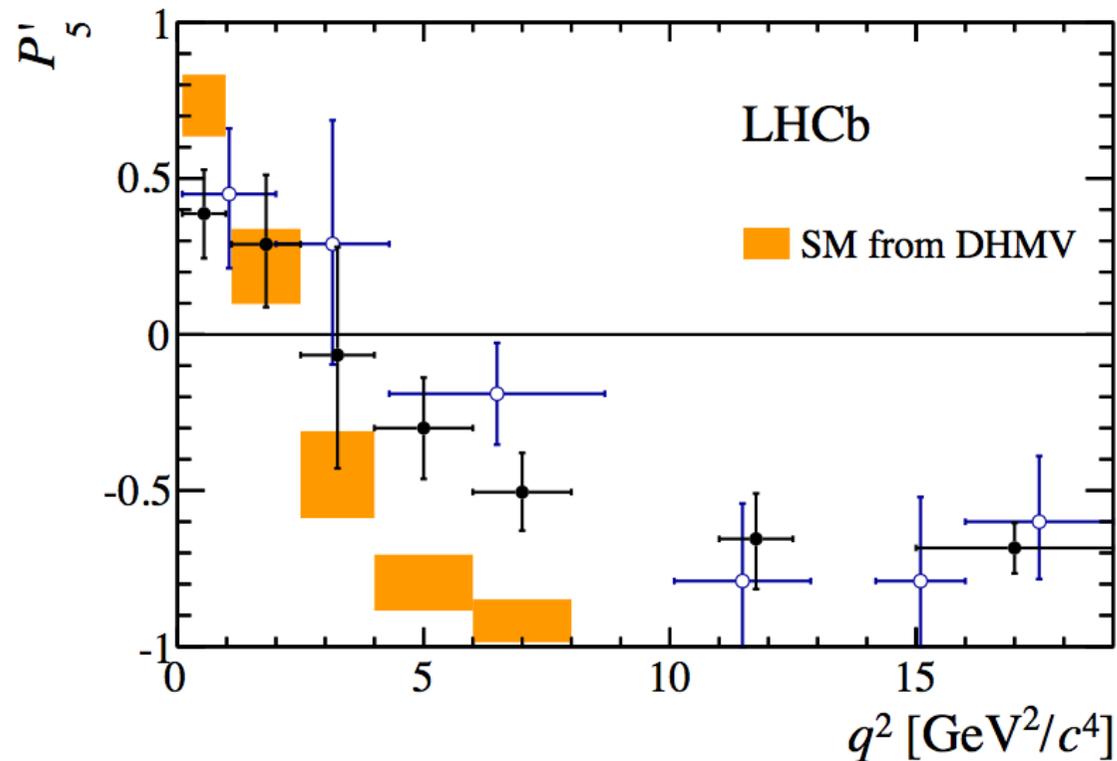
- Tension seen in  $P_5'$  in  $1\text{fb}^{-1}$  data confirmed with  $3\text{fb}^{-1}$ :



- $4.0 < q^2 < 6.0$  and  $6.0 < q^2 < 8.0$   $\text{GeV}^2/c^4$  bins each show deviations of  $2.8\sigma$  and  $3.0\sigma$  respectively

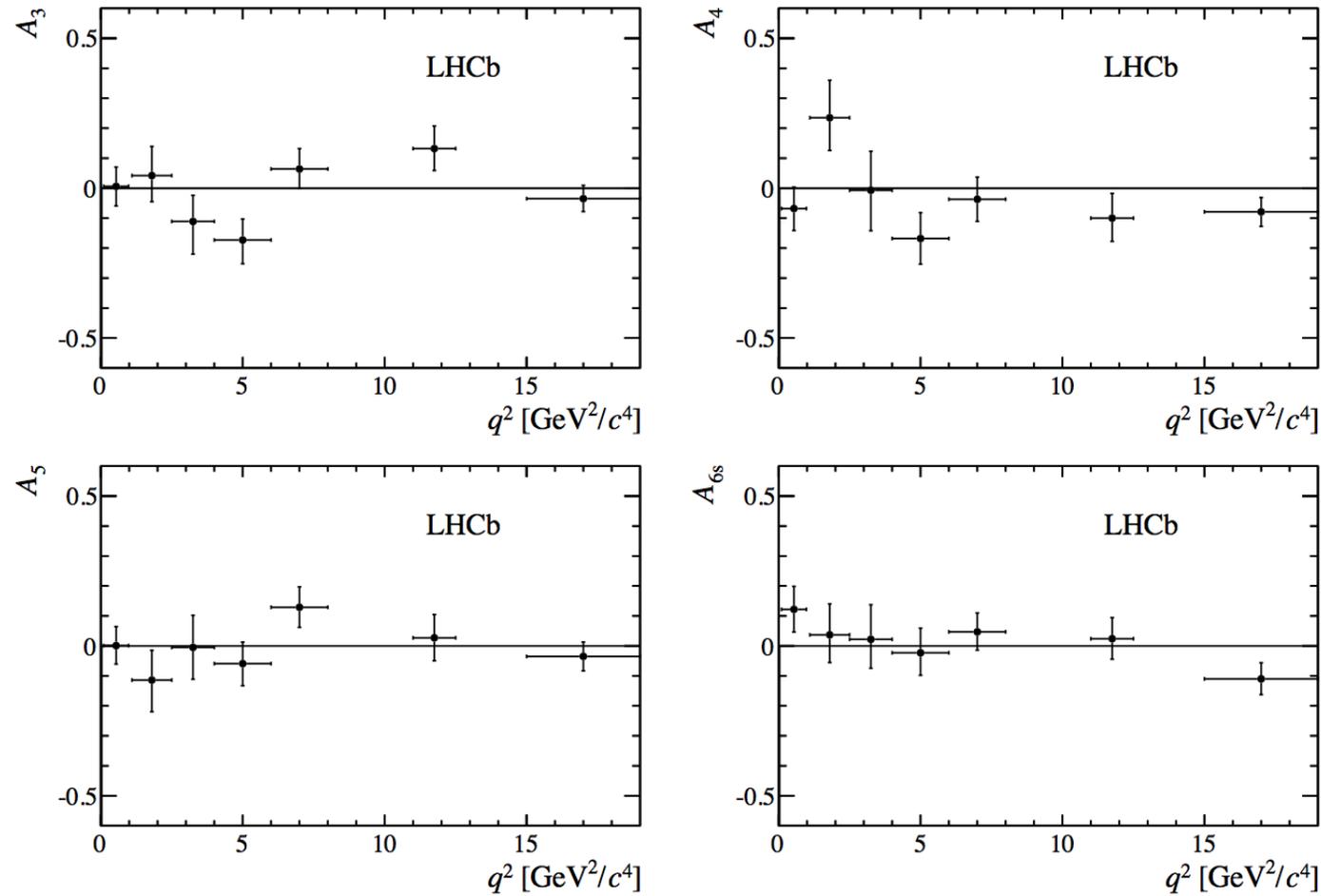
# Results: Likelihood, CP-avgd

- Tension seen in  $P_5'$  in  $1\text{fb}^{-1}$  data confirmed with  $3\text{fb}^{-1}$ :

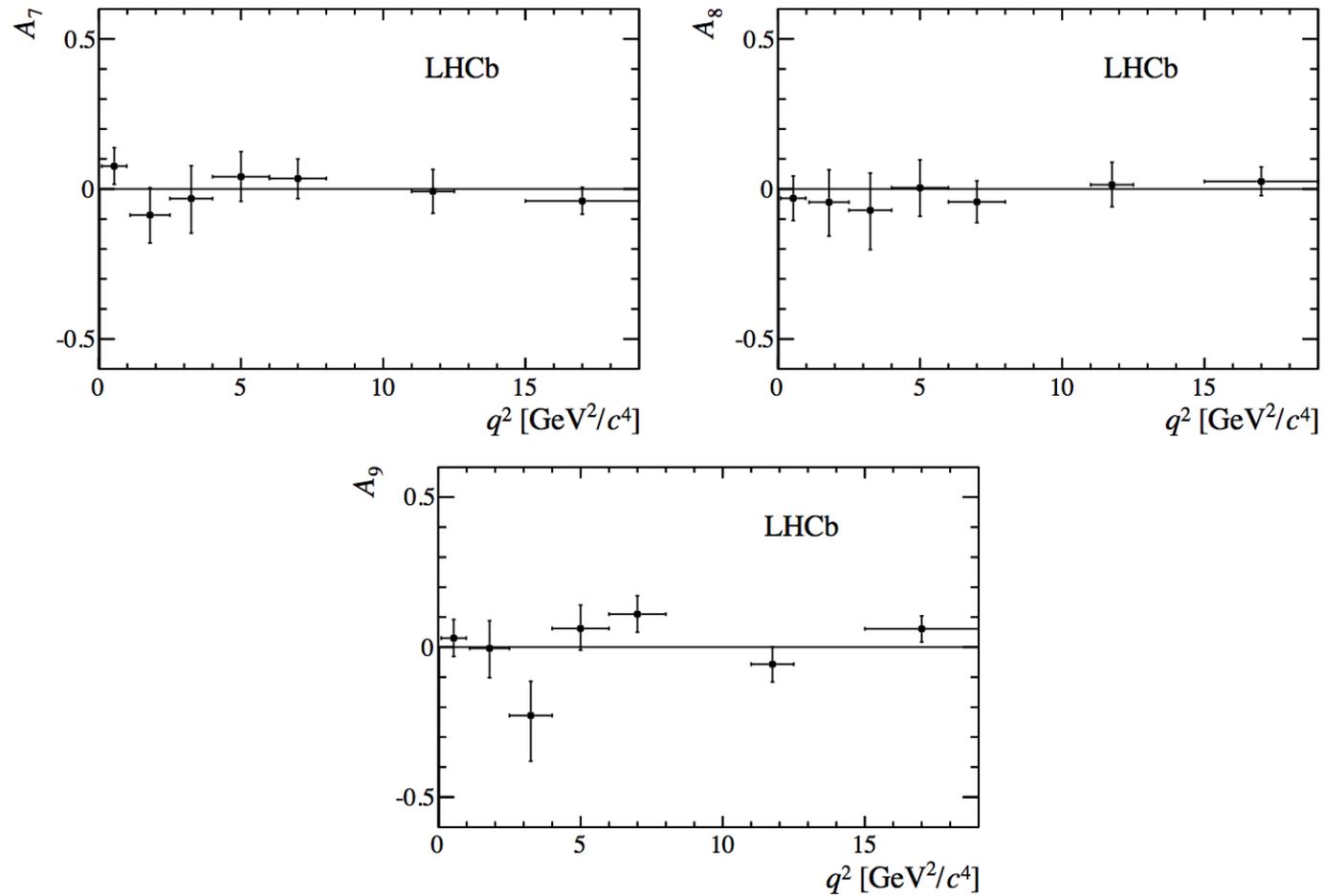


- $4.0 < q^2 < 6.0$  and  $6.0 < q^2 < 8.0$  GeV<sup>2</sup>/c<sup>4</sup> bins each show deviations of  $2.8\sigma$  and  $3.0\sigma$  respectively

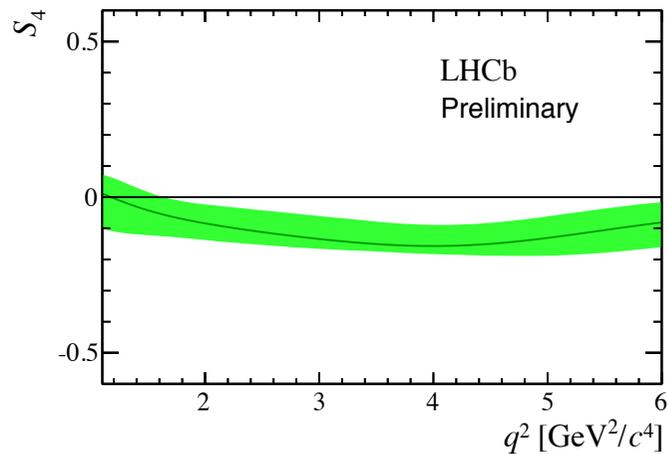
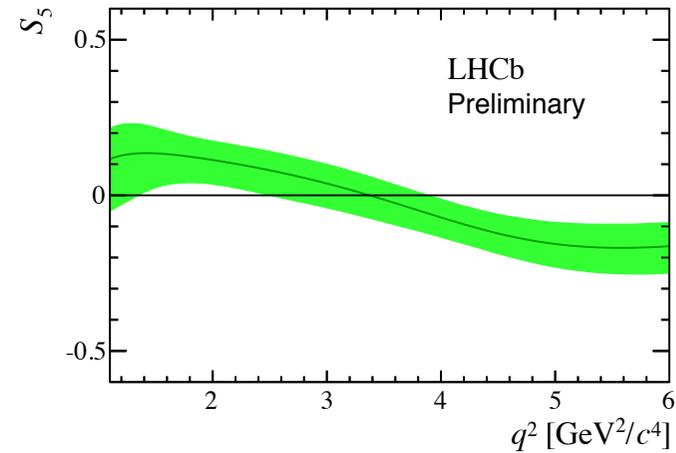
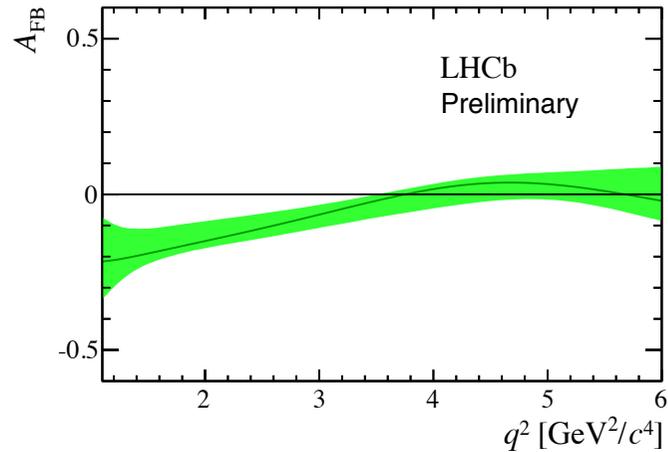
# Results: Likelihood, CP-asymm



# Results: Likelihood, CP-asymm



# Zero-crossing points



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Zero crossing points:

$$q_0^2(S_4) < 2.65 \text{ GeV}^2/c^4 \quad @ 95\% \text{ CL}$$

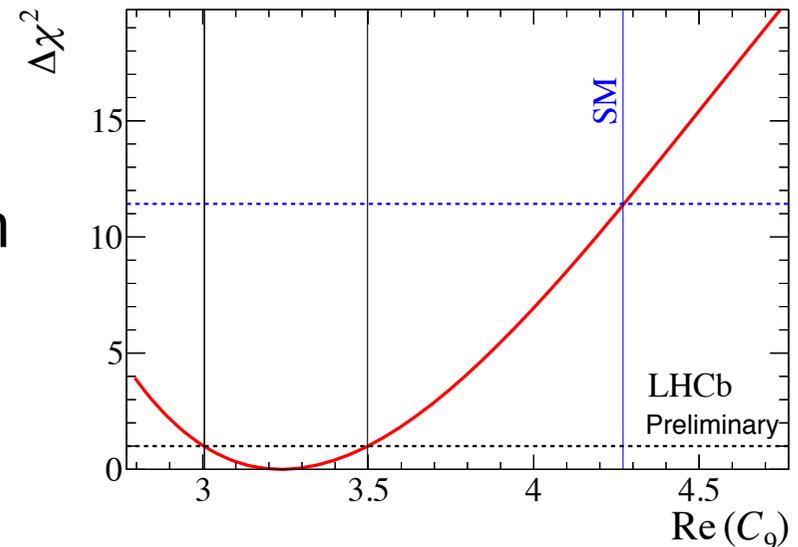
$$q_0^2(S_5) \in [2.49, 3.95] \text{ GeV}^2/c^4 \quad @ 68\% \text{ CL}$$

$$q_0^2(A_{\text{FB}}) \in [3.40, 4.87] \text{ GeV}^2/c^4 \quad @ 68\% \text{ CL}$$

# Compatibility with the SM

- Use EOS software to check compatibility of CP-averaged angular measurements with SM
- Make  $\chi^2$  fit to  $F_L$ ,  $A_{FB}$  and  $S_3-S_9$  in  $q^2$  range  $<8.0 \text{ GeV}^2$  and in wide bin  $15.0 < q^2 < 19.0 \text{ GeV}^2$
- Consider only modification to  $\text{Re}(C_9^{\text{eff}})$

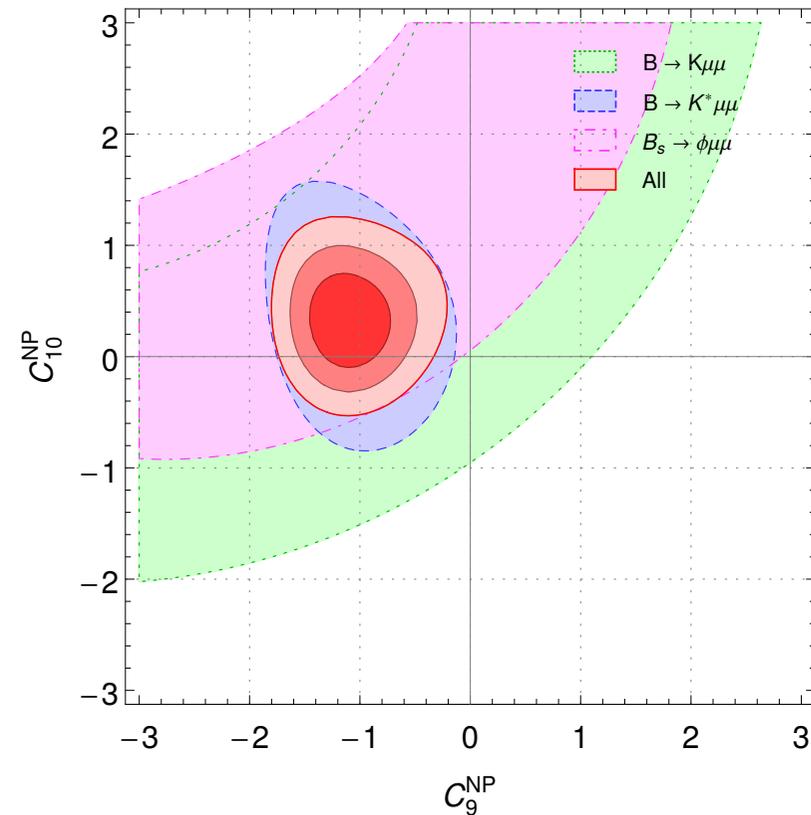
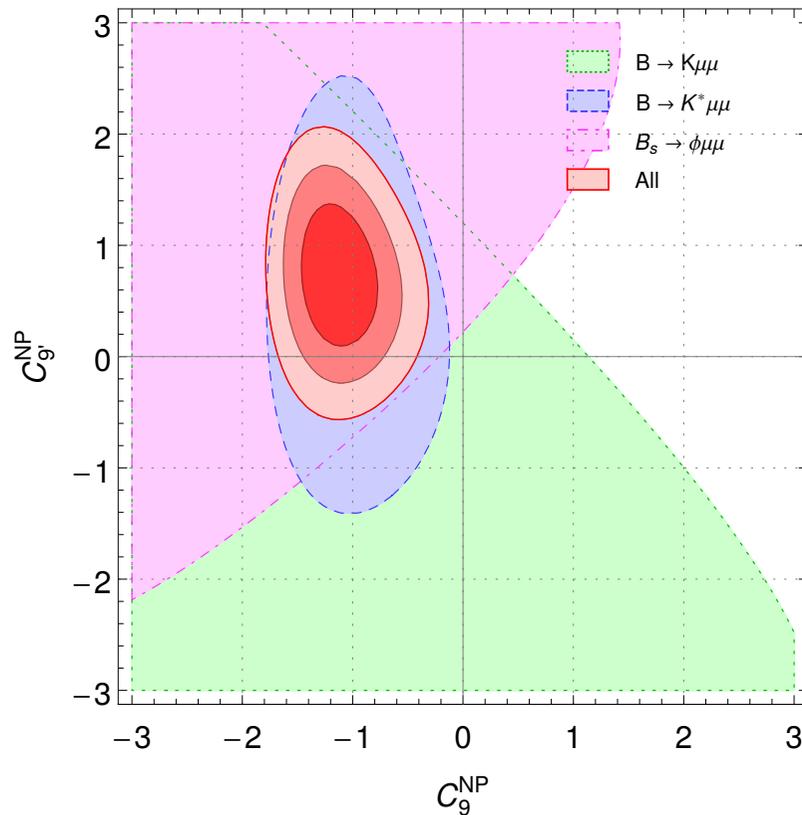
- Find LHCb **CP-averaged angular data *alone***  $3.4\sigma$  from SM predictions



# A global fit to all the $b \rightarrow s\mu\mu$ data

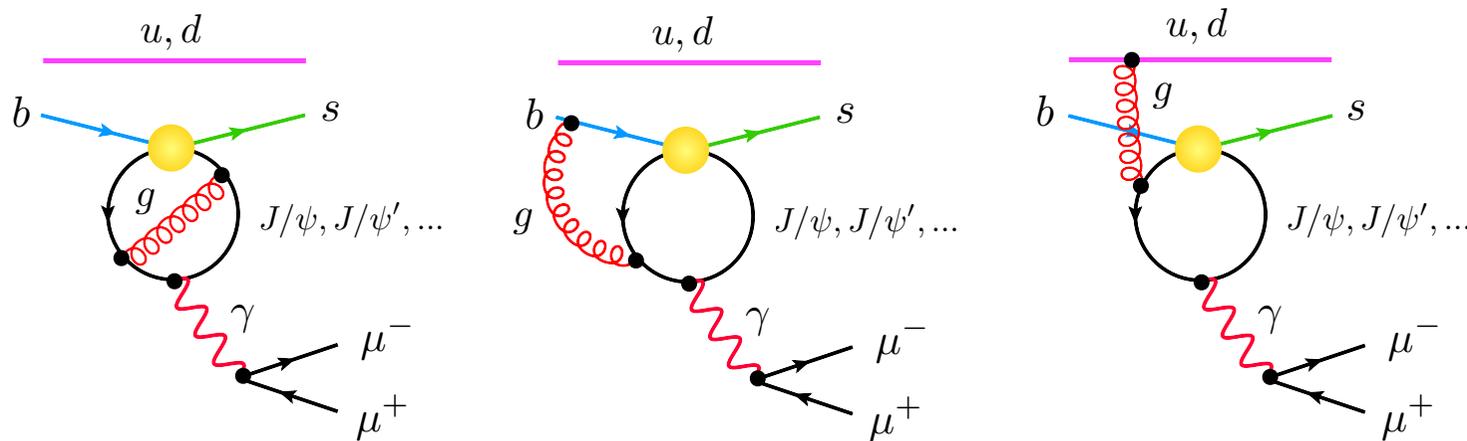
- Global fit to all the (preliminary, Moriond)  $b \rightarrow s\mu\mu$  data gives a solution  **$4.5\sigma$  from SM ... !**

[arXiv:1510.04239]

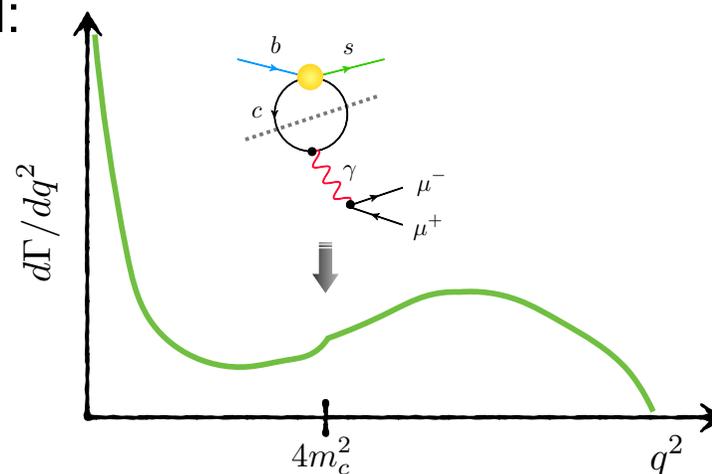


# Could the SM errors be wrong?

- Largest individual uncertainty on  $P_5'$  from  $c\bar{c}$ -loop effects

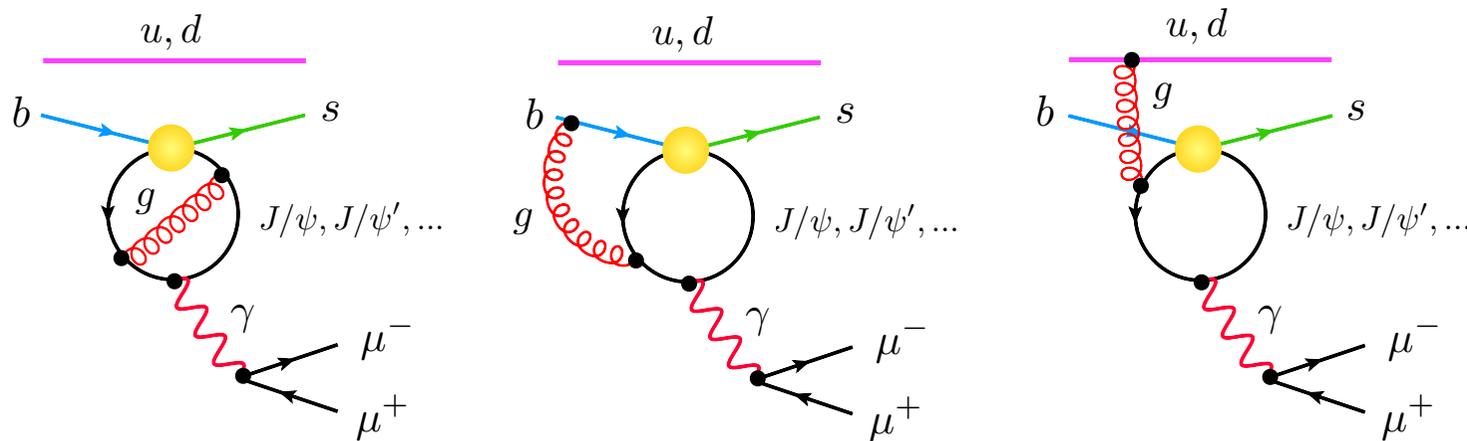


- In an ideal world:

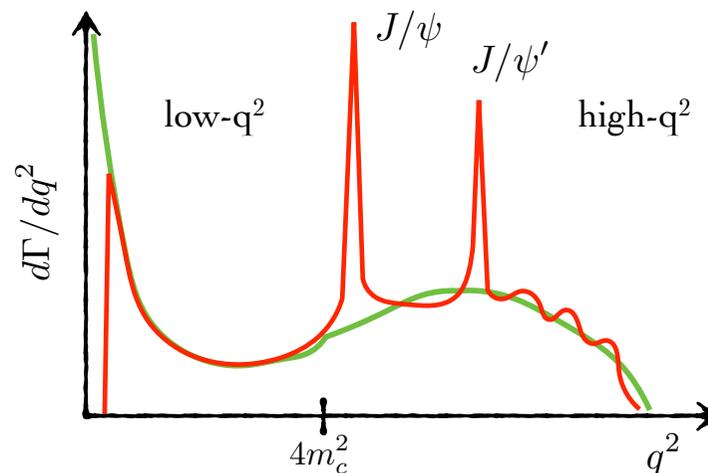


# Could the SM errors be wrong?

- Largest individual uncertainty on  $P_5'$  from  $c\bar{c}$ -loop effects



- But in reality:

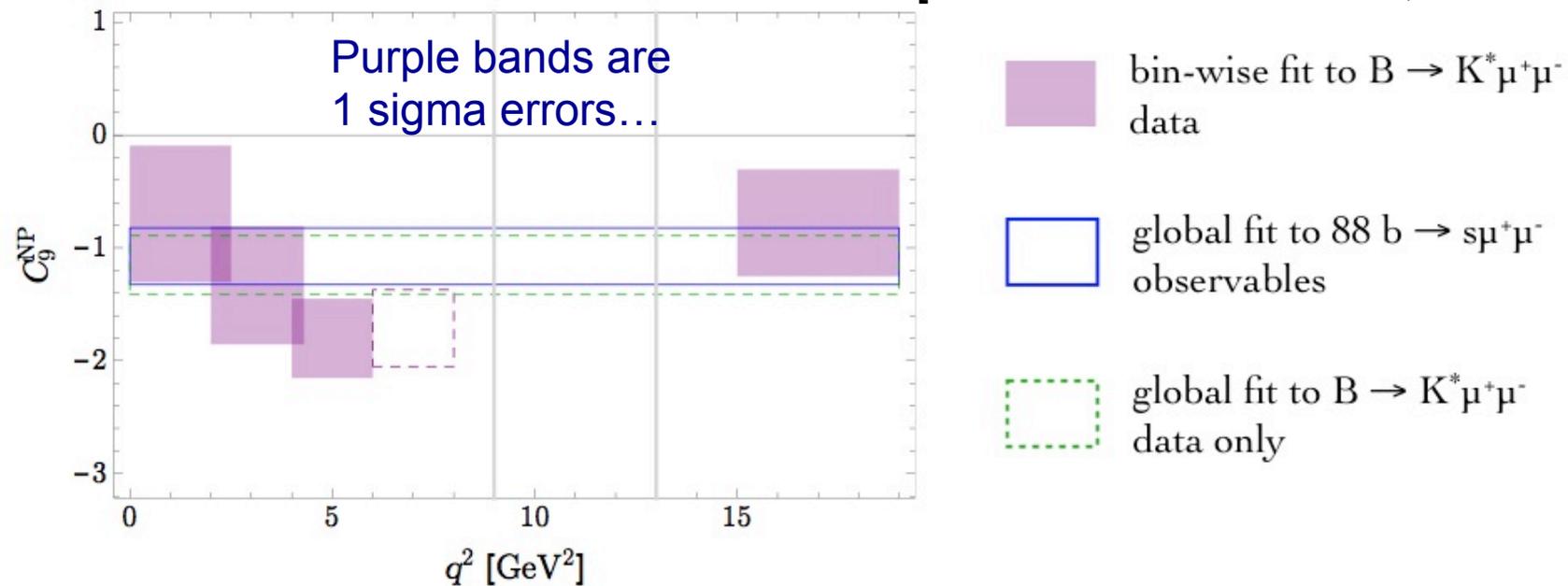


Note however that can't just effect  $P_5'$ - would see correlated effect in other observables

# Could the SM errors be wrong?

- Try and test for this :
  - If anomalies are due to NP then would expect best-fit values for  $C_9$  to be  $q^2$  independent
  - If instead effect grows towards resonance, could be a  $c\bar{c}$  effect

[Altmannshofer & Straub, 1503.06199]



- If is to be explained by  $c\bar{c}$ , effect needs to “unexpectedly large”

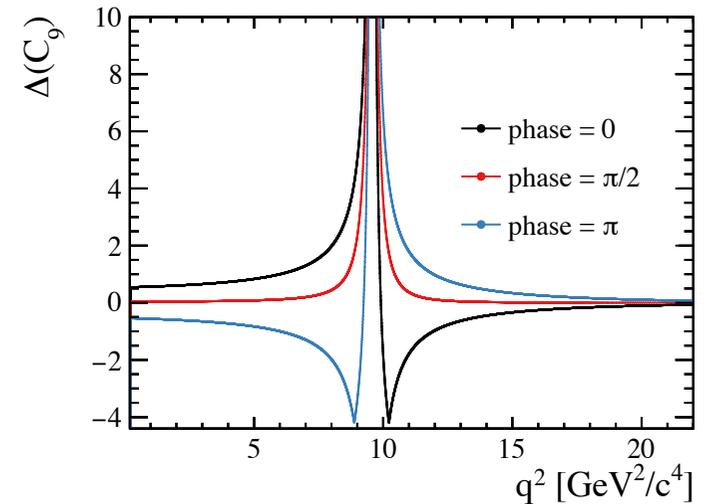
# Outline

- A tour of existing LHCb rare decay measurements
  - $B^0 \rightarrow \mu\mu$  branching fraction measurements
  - $B_d^0 \rightarrow K^{*0} \mu\mu$  angular measurements
  - Other  $b \rightarrow s \mu\mu$  branching fraction measurements
  - Global fits to  $b \rightarrow s ll$  data
  - Mention a couple of other anomalous results
- (Very) latest  $B_d^0 \rightarrow K^{*0} \mu\mu$  angular results
  - compatibility with SM
  - Updated global fits
- Some remarks about the future

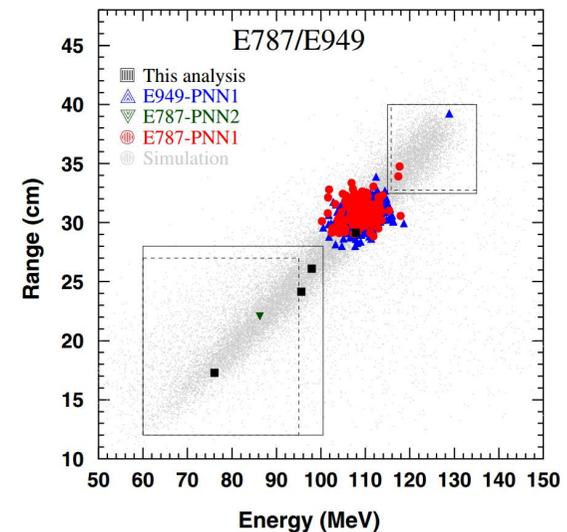


# The future

- Will improve the precision of all existing measurements with the Run-II data!
- Can also add new LHCb measurements
  - Add  $R_{K^*}$ ,  $R_\phi$ ,  $R_\Lambda$  (for  $b \rightarrow c$  equivalent  $R_D$ ,  $R_\Lambda$ , ... ), and also the  $(K^*, \phi, \Lambda) ee$  angular analyses
  - Can we measure the interference with the  $J/\psi$  ?
    - Introduce relevant resonances and try and fit the  $m_{\mu\mu}$  distribution – requires very good control of resolution



- Elsewhere:
  - Cleaner EW penguin  $B^0 \rightarrow K^{*0} \nu \nu$  will be measured at Belle2 – would expect a substantial enhancement from a  $Z'$
  - $K^+ \rightarrow \pi^+ \nu \nu$  will be measured to 10% at NA62
    - $B(K^+ \rightarrow \pi^+ \nu \nu)$  SM pred. =  $(9.11 \pm 0.72) \times 10^{-11}$
    - $B(K^+ \rightarrow \pi^+ \nu \nu)$  measured. E787/E949 =  $(17.30 \pm 11.0) \times 10^{-11}$



# Conclusions

## The LHCb Experiment: First Results and Prospects

Mitesh Patel (Imperial College London)  
The University of Birmingham, 4<sup>th</sup> May 2011

### Outline

- An extended Higgs sector? ( $B_d \rightarrow \mu^+ \mu^-$  and  $B_s \rightarrow \mu^+ \mu^-$ )
- New CP violating phases in  $B_s$  mixing? ( $\phi_s$  from  $B_s \rightarrow J/\psi \phi$ )
- New particles, couplings? (angular observables in  $B_d \rightarrow K^* \mu \mu$ )
- A whistlestop tour...
- Will try and give you a feel for the prospects in each of these areas
  - Results from 2010 data  $\sim 36 \text{ pb}^{-1}$
  - As of yesterday,  $\sim 80 \text{ pb}^{-1}$  on tape, expectation is  $\sim 200 \text{ pb}^{-1}$  for summer conferences,  $\sim 1 \text{ fb}^{-1}$  by the end of the year

- The LHCb data has shown up some intriguing anomalies that warrant further experimental and theoretical exploration
- We are eagerly awaiting the Run-II data

2